

lecture 19.1.2012

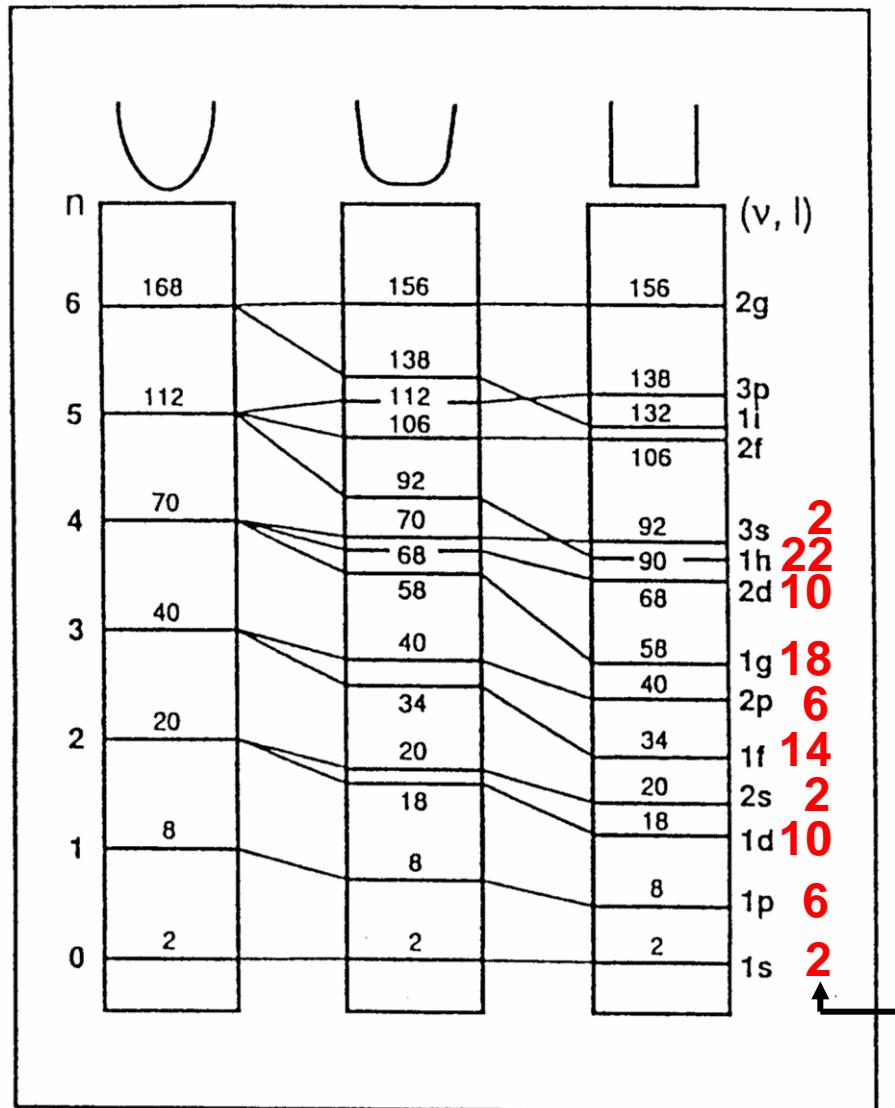
we had so far:

- binding in clusters and their appearances in mass spectra
 - d) metallic bonding

today

- more to metallic bonding
- photoelectron spectroscopy
- trends in photoionization and detachment energies

The spherical jellium model: role of the potential like in *nuclear physics*

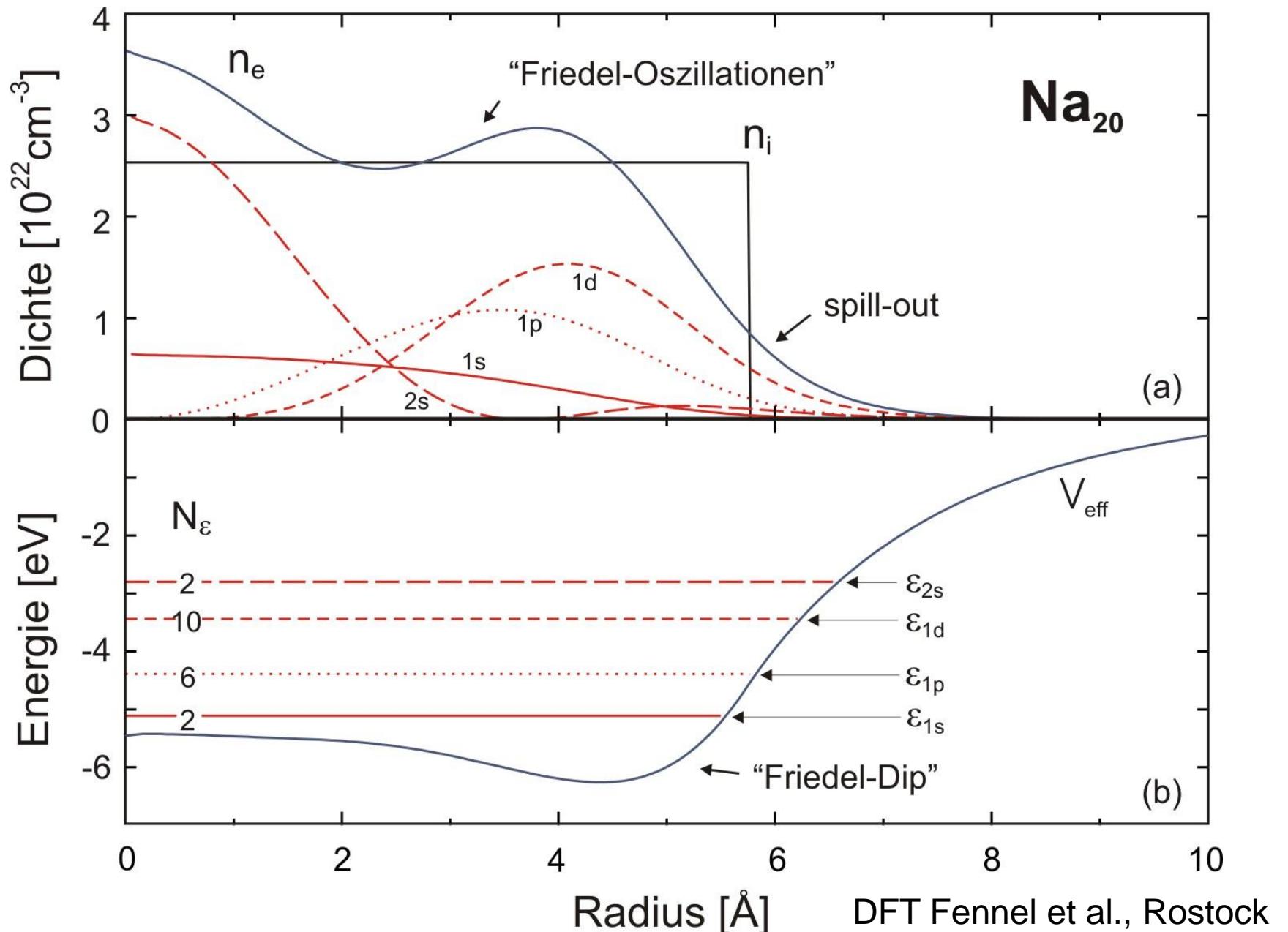


Explains the magic numbers of neutral alkali clusters :
2, 8, 20, 40, 58, 70, 92 ...

Also explains the magic numbers for divalent metals such as zinc or cadmium, at
4, 9, 10, 17, 20, 29 ... atoms.

$2(2l + 1)$
electrons

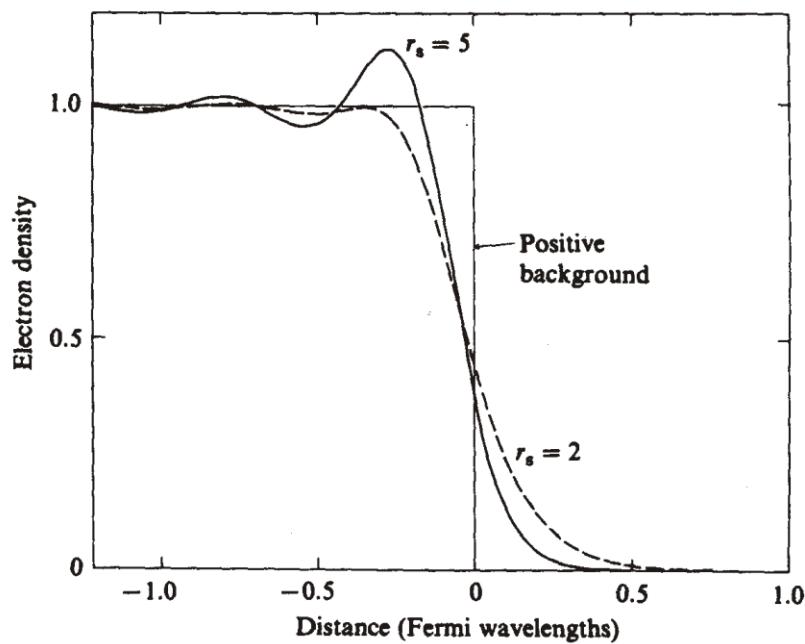
the jellium model



compare: metal surfaces - resulting electron density

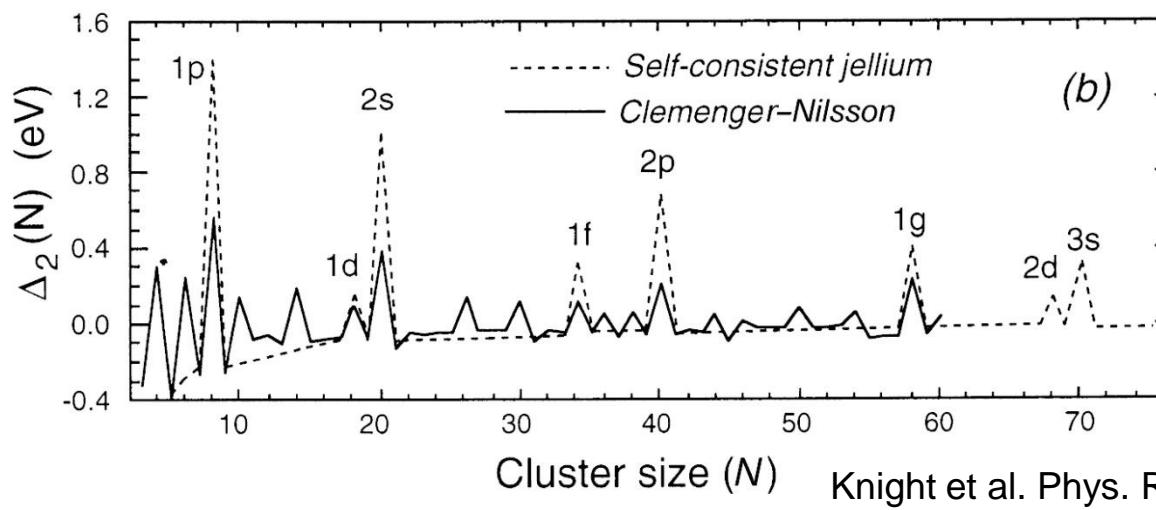
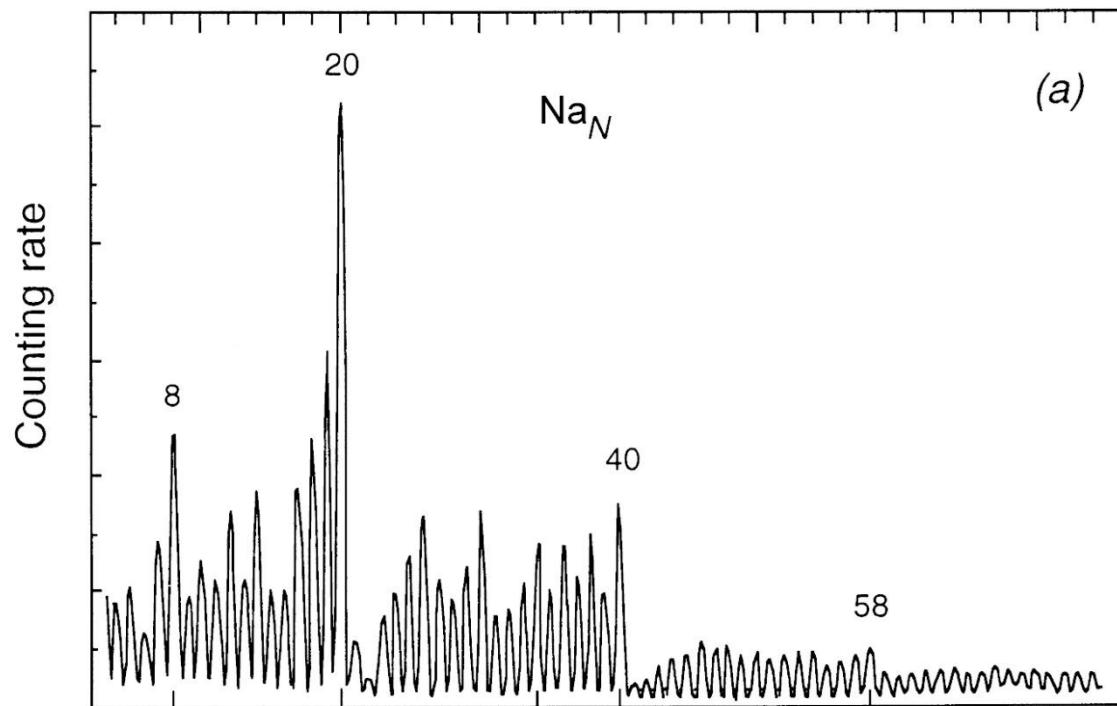
- electron density $n(z)$ shows oscillations (Friedel oszillations)
- $n(z)$ spills out beyond the ionic charge (electron spill-out)
- spill-out produces a surface dipole

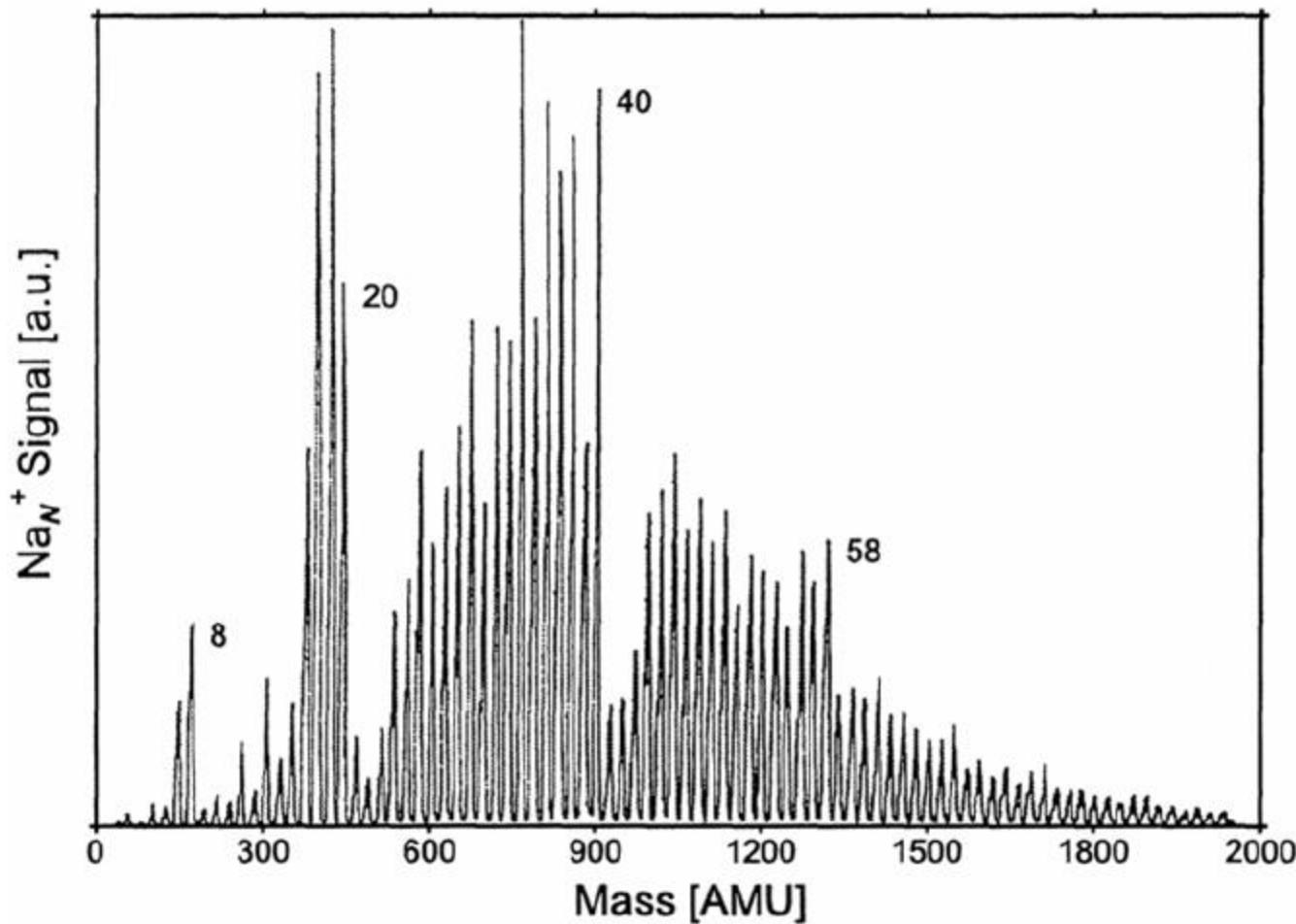
Fig. 4.2. Electron density profile at a jellium surface for two choices of the background density, r_s (Lang & Kohn, 1970).



Ursache der Oszillation:
Elektronen mit festen Wellenvektor versuchen pos. Hintergrundladung abzuschirmen; hieraus folgen leichte Verschiebungen der einzelnen Atomlagen im Bereich der Oberfläche

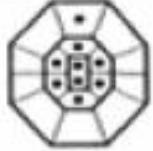
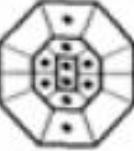
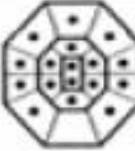
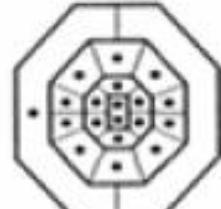
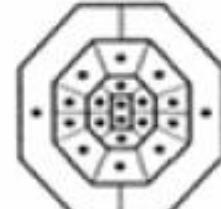
jellium fingerprint in the mass spectra





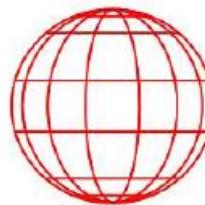
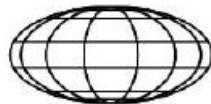
M. Kappes, R. W. Kunz, und E. Schumacher,
Chem. Phys. Lett. 91, 413(1982)

like a periodic table: the shell model for Na clusters

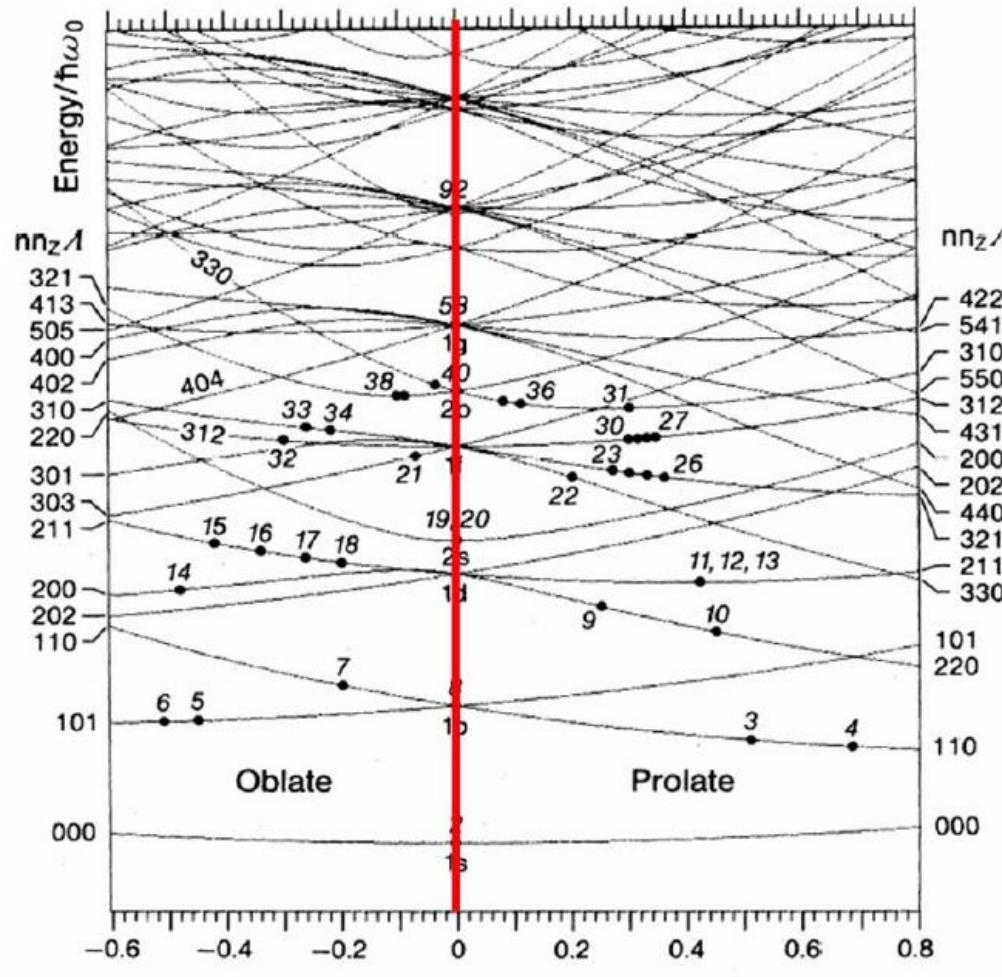
Shell	Monovalent				Closed shells
1s	 Na				 Na ₂
1p	 Na ₃	 Na ₄	—→	 Na ₇	 Na ₈
1d	 Na ₉	 Na ₁₀	—→	 Na ₁₇	 Na ₁₈
2s	 Na ₁₉				 Na ₂₀

sub shells through distortion: the Clemenger-Nielsson model

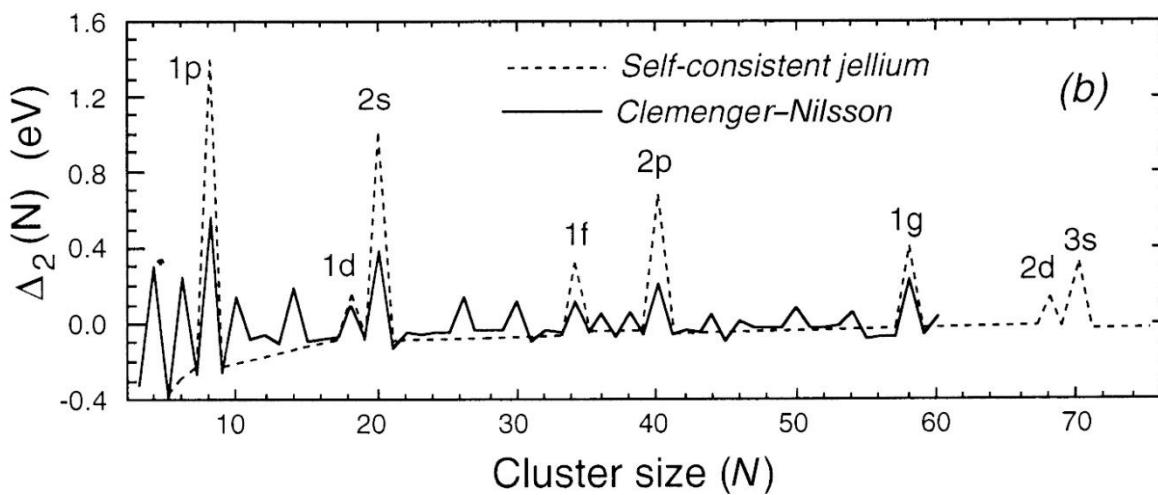
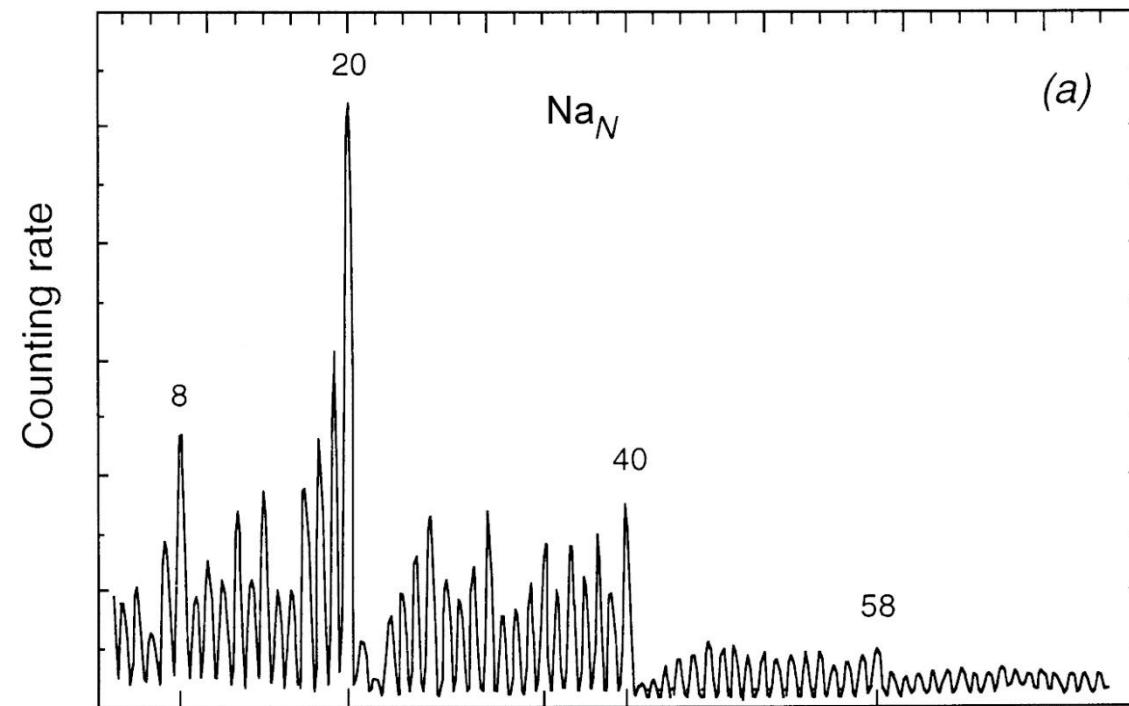
oblate
deformation



prolate
deformation

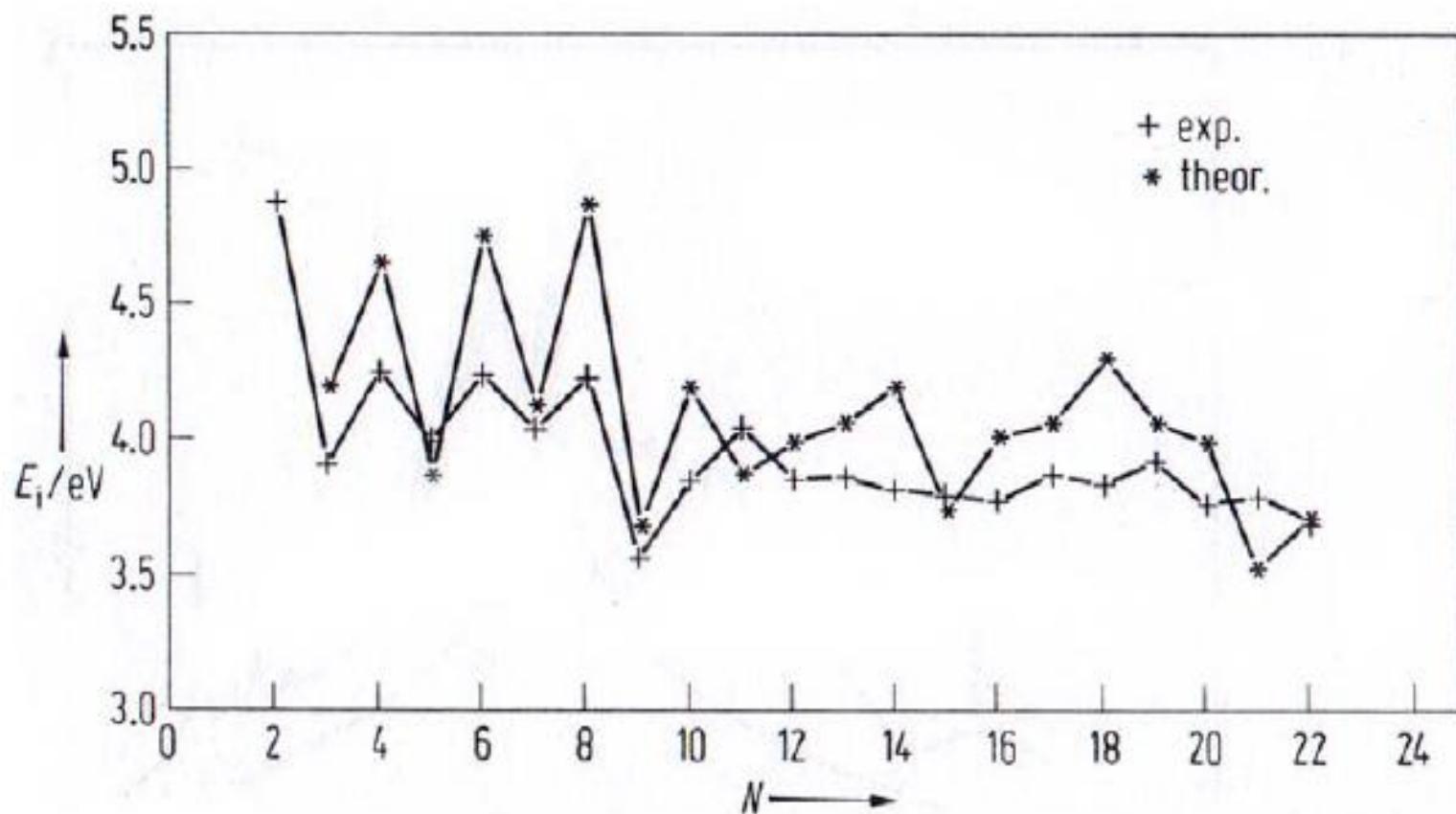


deformations explain the sub-shell closings

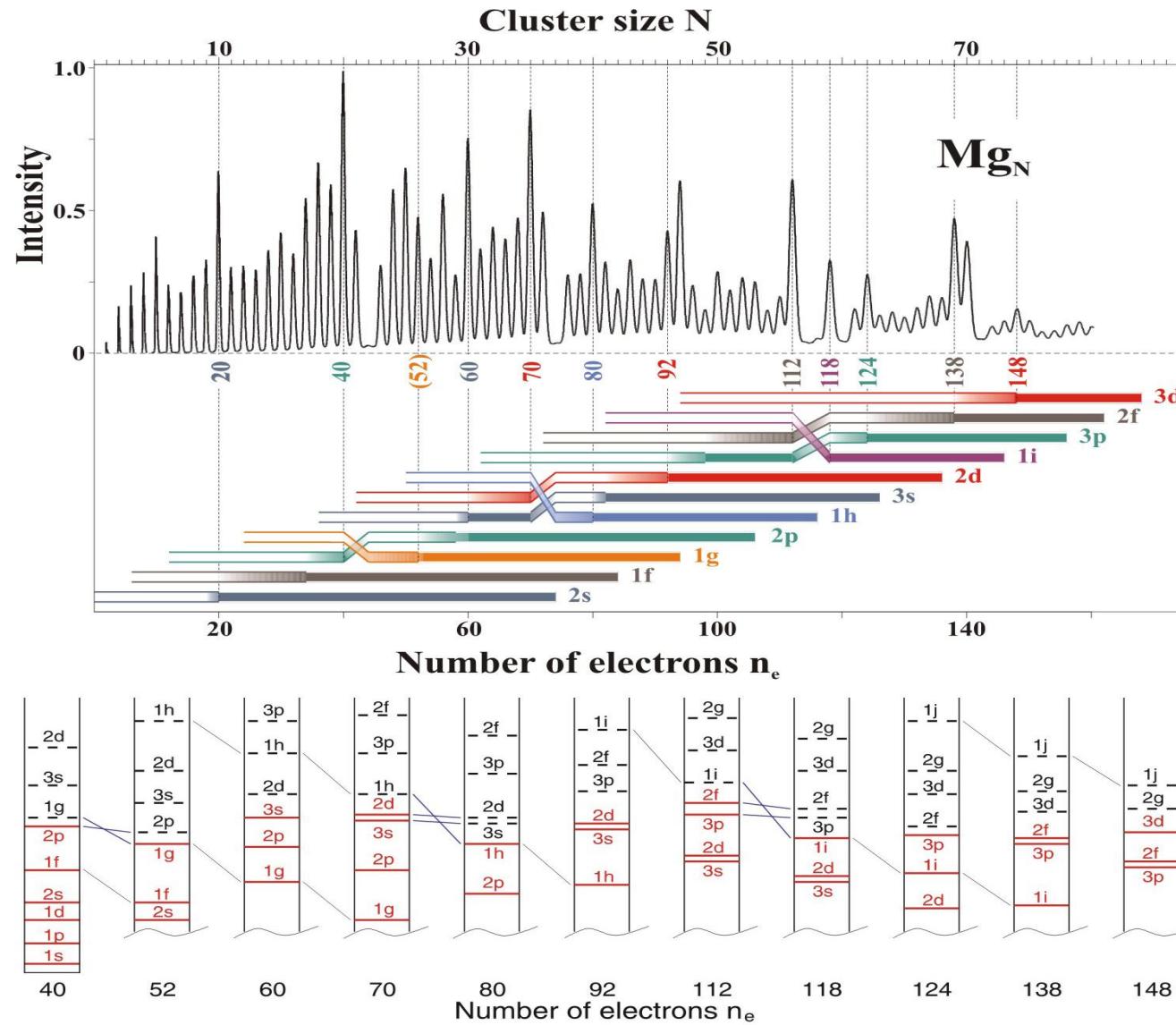


Knight et al.

early direct evidence for electronic shells: ionization energies of Na clusters

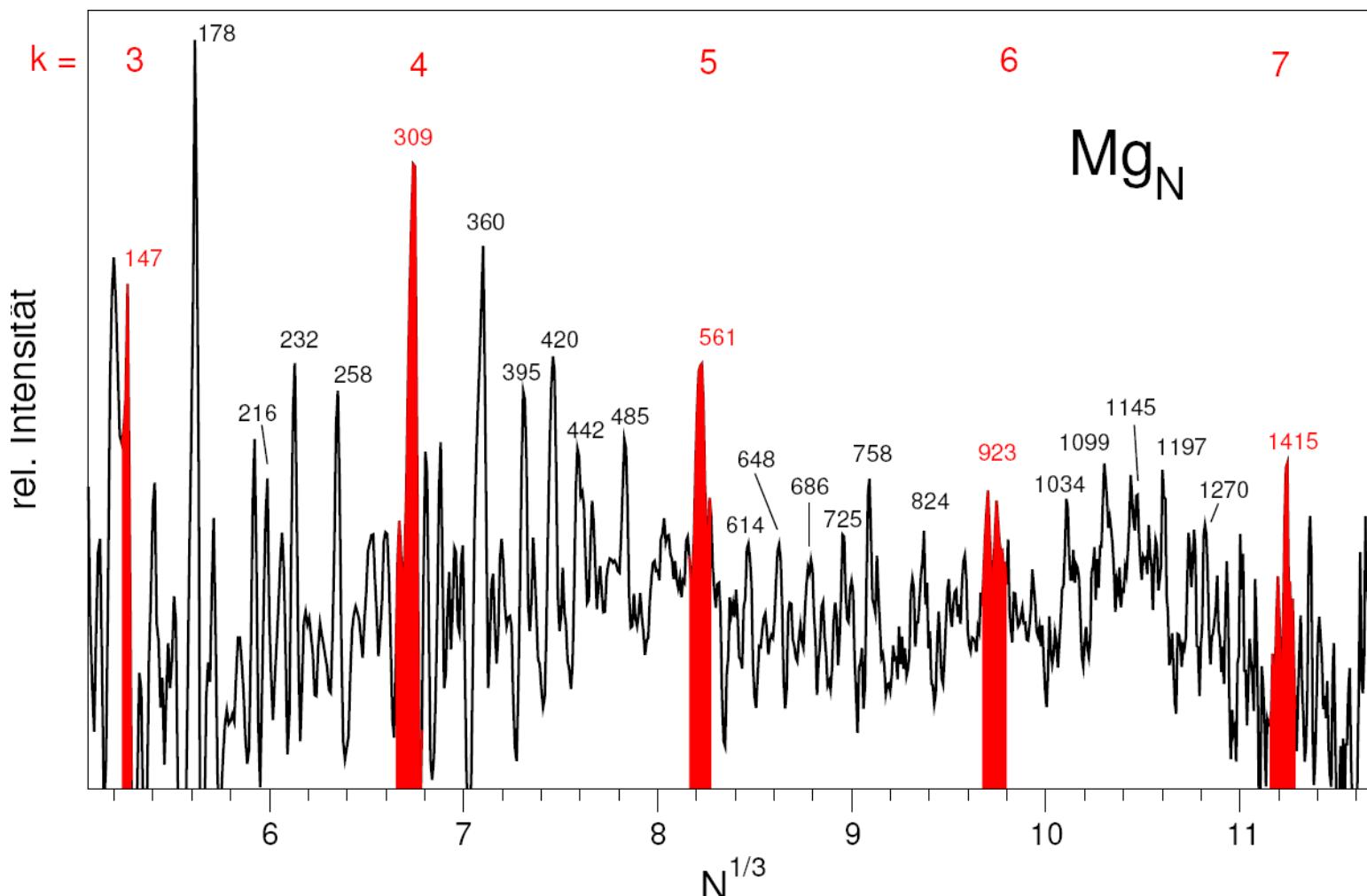


Small Magnesium clusters as another example for a jellium system.
Now each atom contributes with two electrons

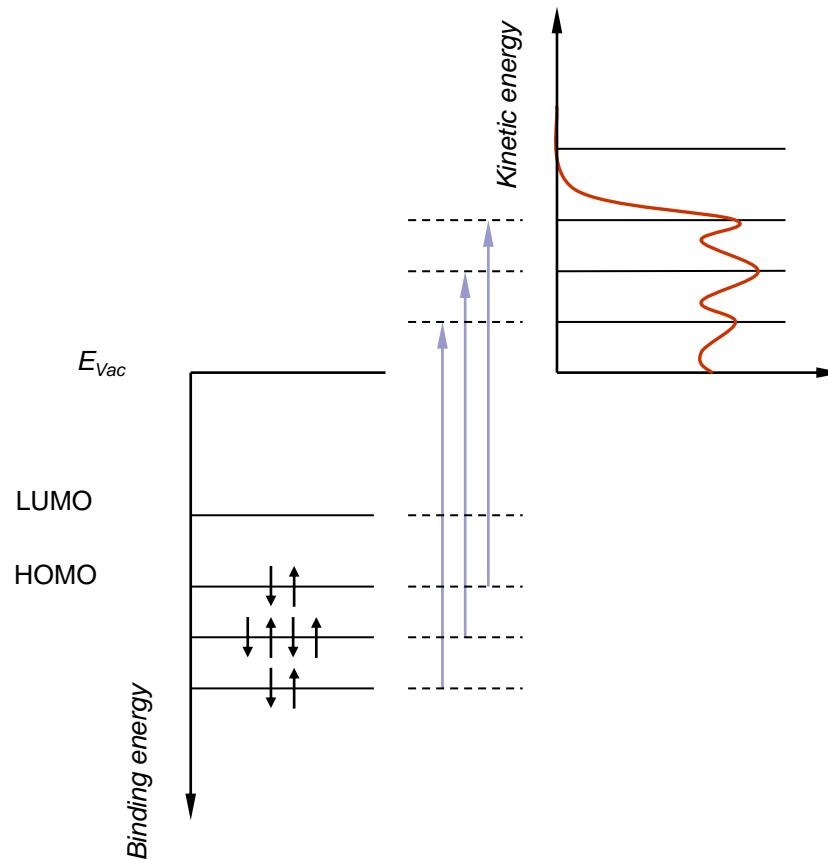


Electronic vs. geometrical shell

Example: large Mg_N show both, electronic and geom. shells



how to measure the electronic structure? by photoelectron spectroscopy



$$E_{kin} = h\nu - E_B$$

technical challenge: extremely low target density as it is necessary to work with a *charged* cluster beam. Only charged clusters can be mass selected

Magnetic bottle electron spectrometer

$$r_i = \frac{v \sin \theta_i}{\omega_i}, \quad \checkmark$$

$$\frac{\sin \theta_f}{\sin \theta_i} = \sqrt{\frac{B_f}{B_i}}$$

$$(2) \Rightarrow \frac{\Delta E}{E} \approx \frac{B_f}{B_i}$$

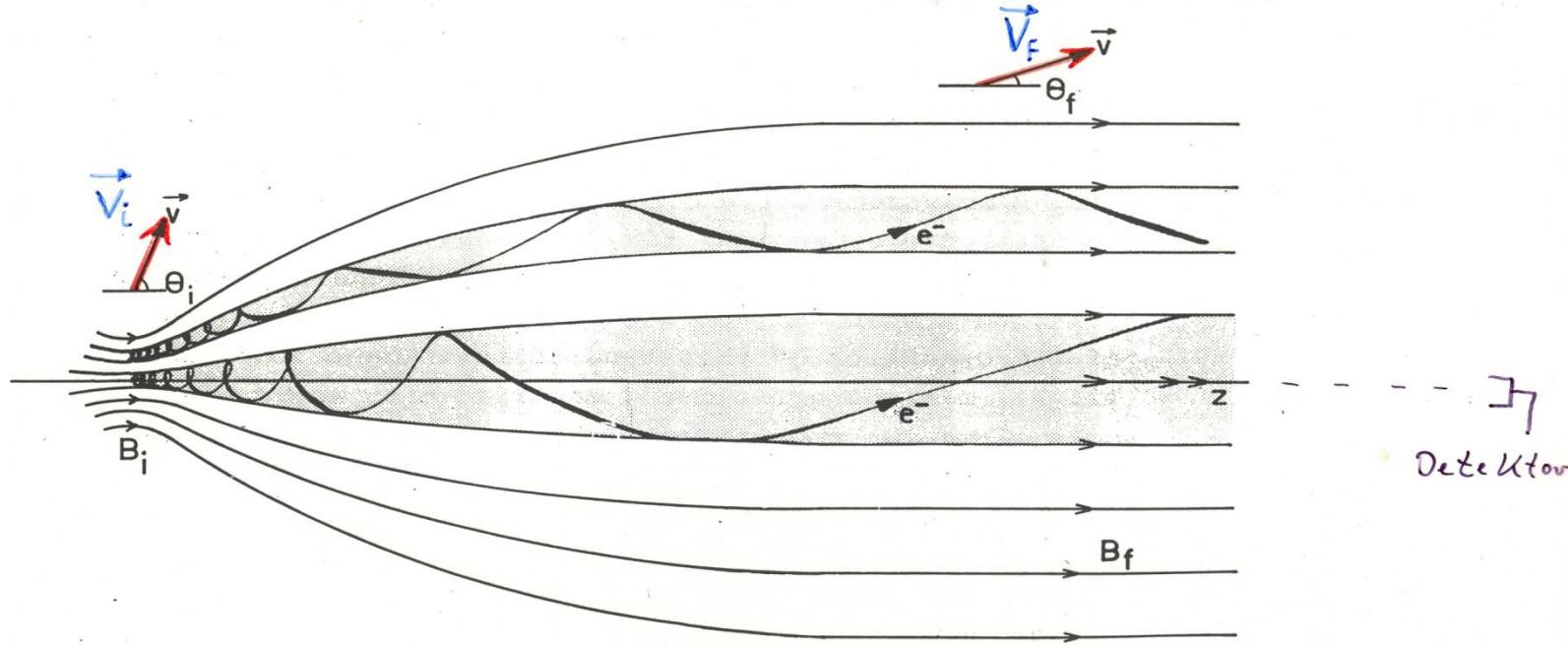


Figure 1

Schematic diagram showing the helical motion of an electron moving in a magnetic field that changes gradually from a strong field B_i to a weaker uniform field B_f . Kruit, Read

in the limit of a strong gradient and a long drift area, the flight times of electrons with the same energy are independent of the emission angle. detection efficiency of about 50 %

technical realization of a magnetic-bottle electron spectrometer

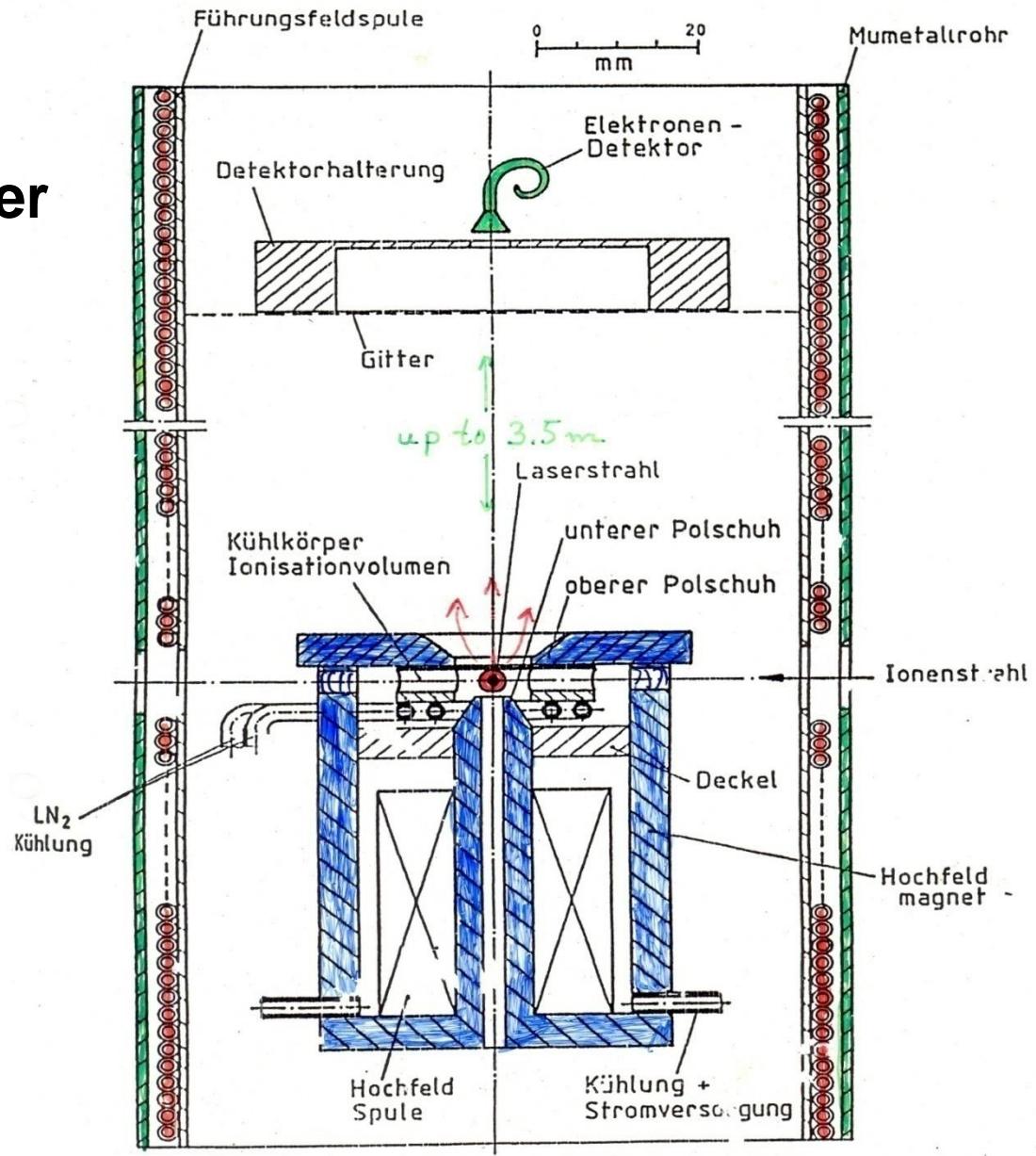
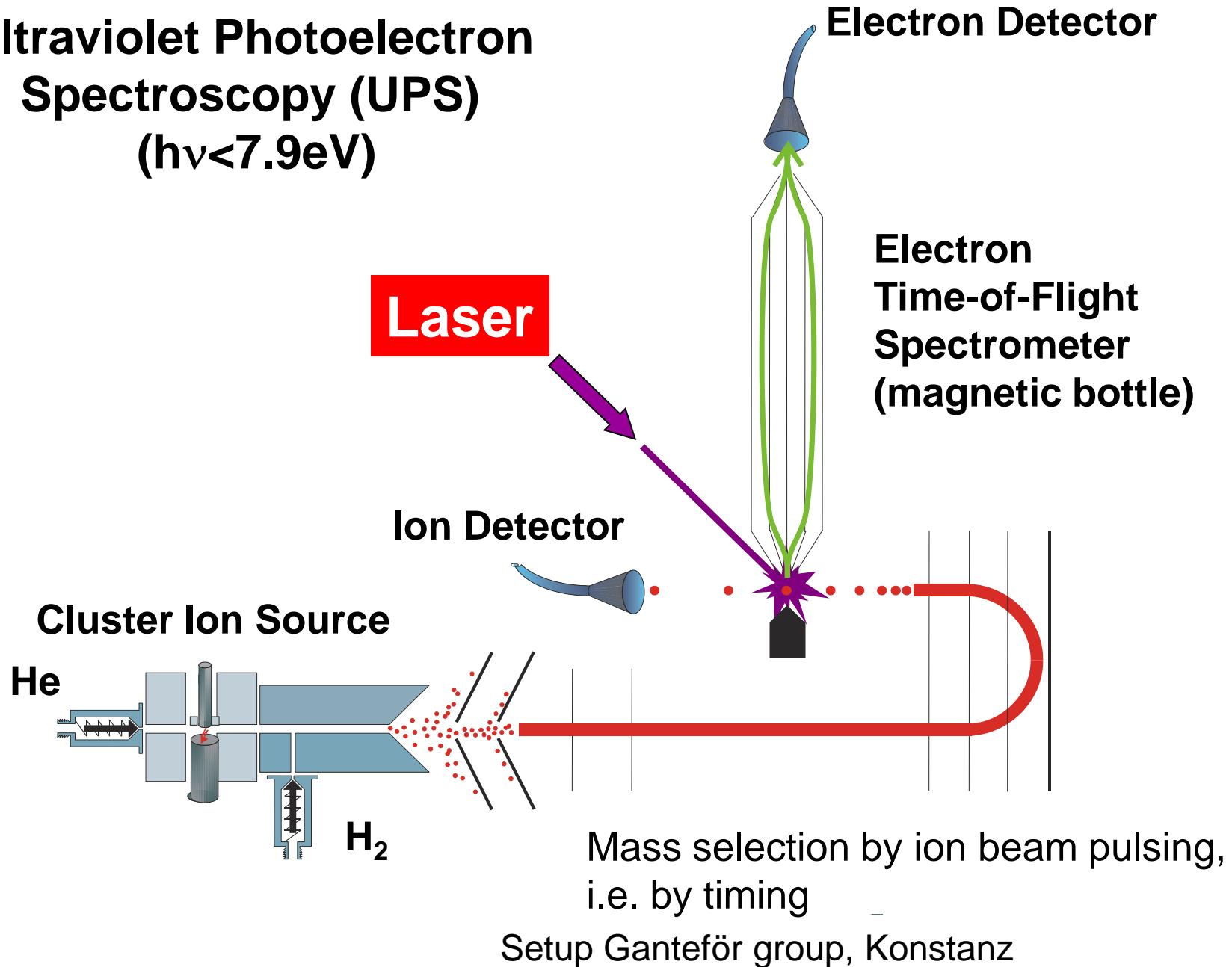
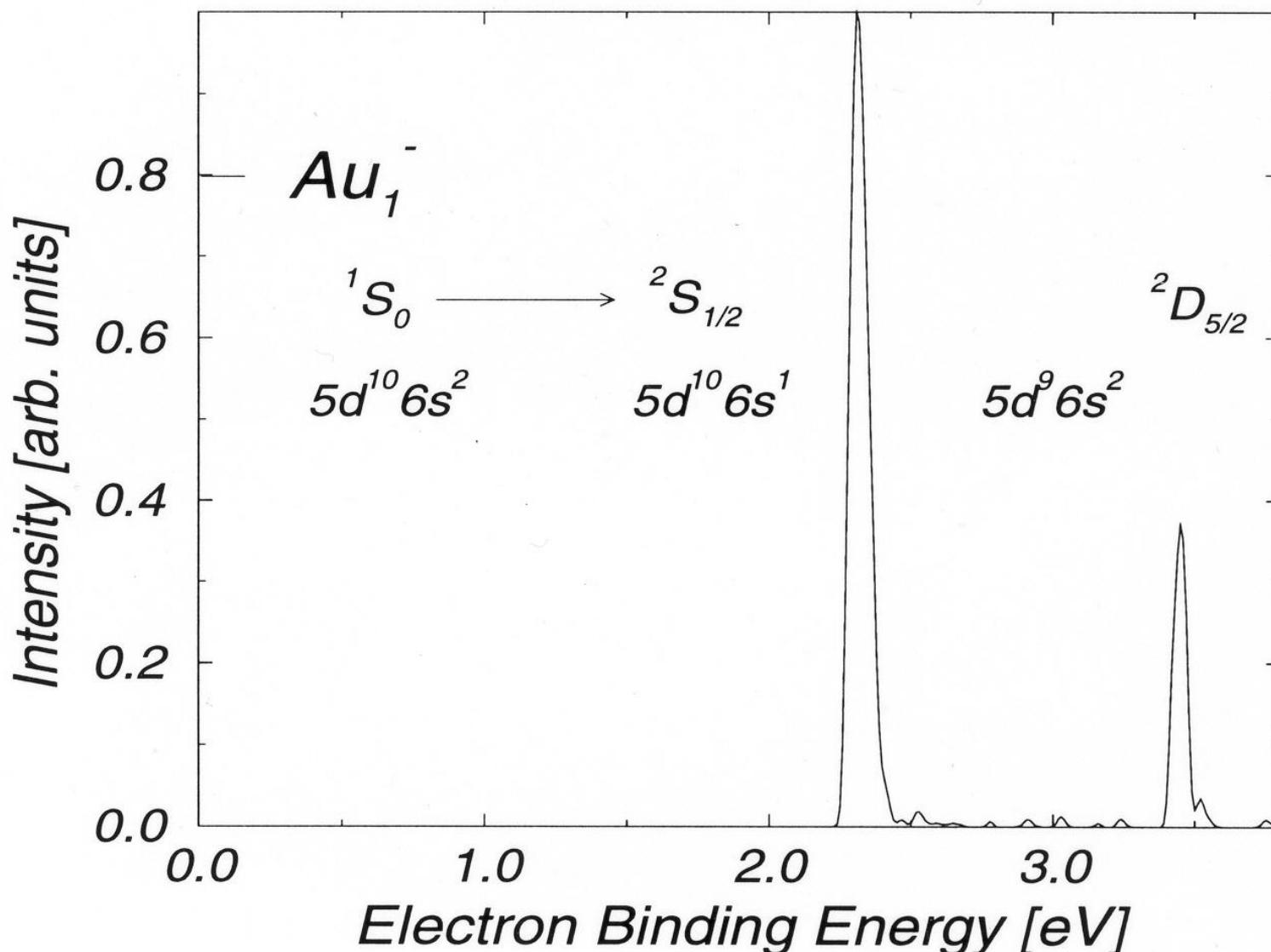


Abbildung 11: Schnitt durch den neuen Hochfeldmagneten

Ultraviolet Photoelectron Spectroscopy (UPS) ($h\nu < 7.9\text{ eV}$)

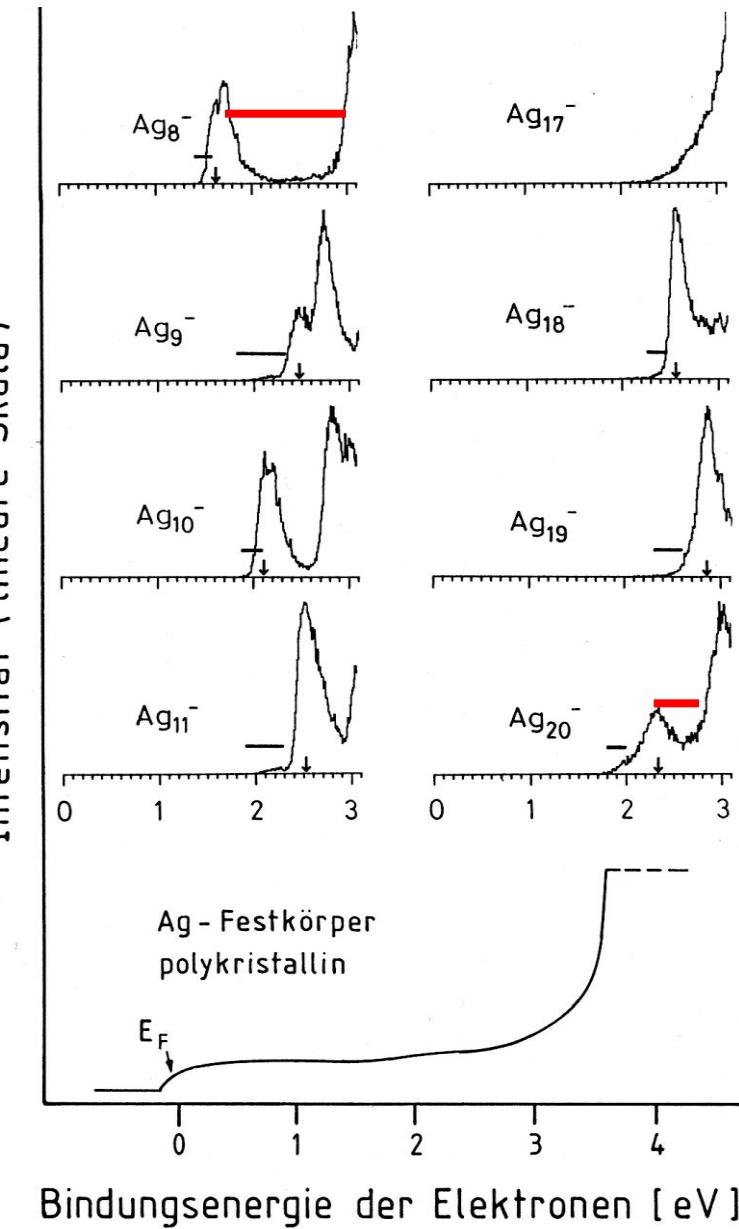
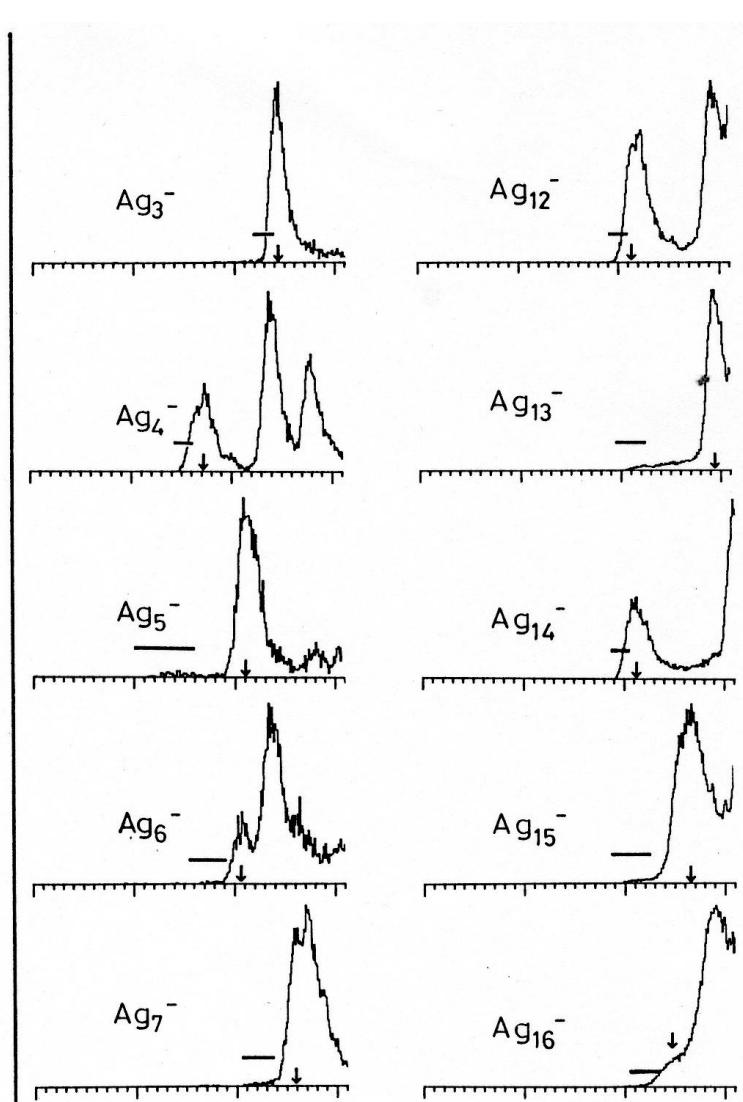


Calibration mag. bottle spectrometer with Au_1^-

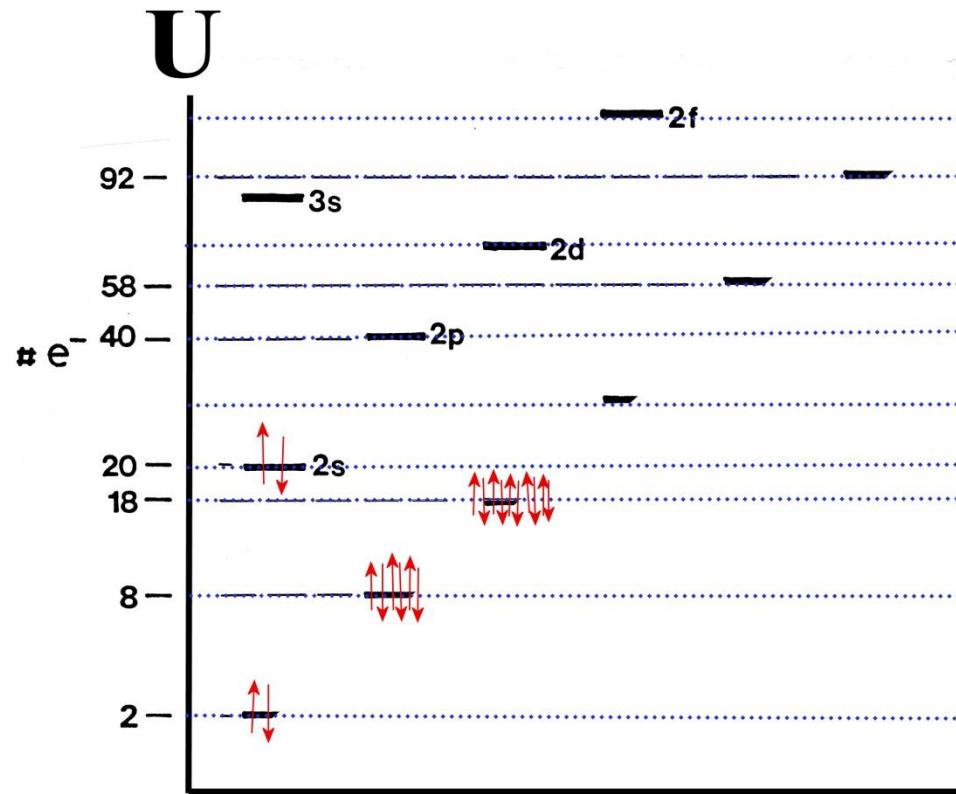


Group Meiws-Broer, Rostock

photoelectron spectra from Ag_N^-

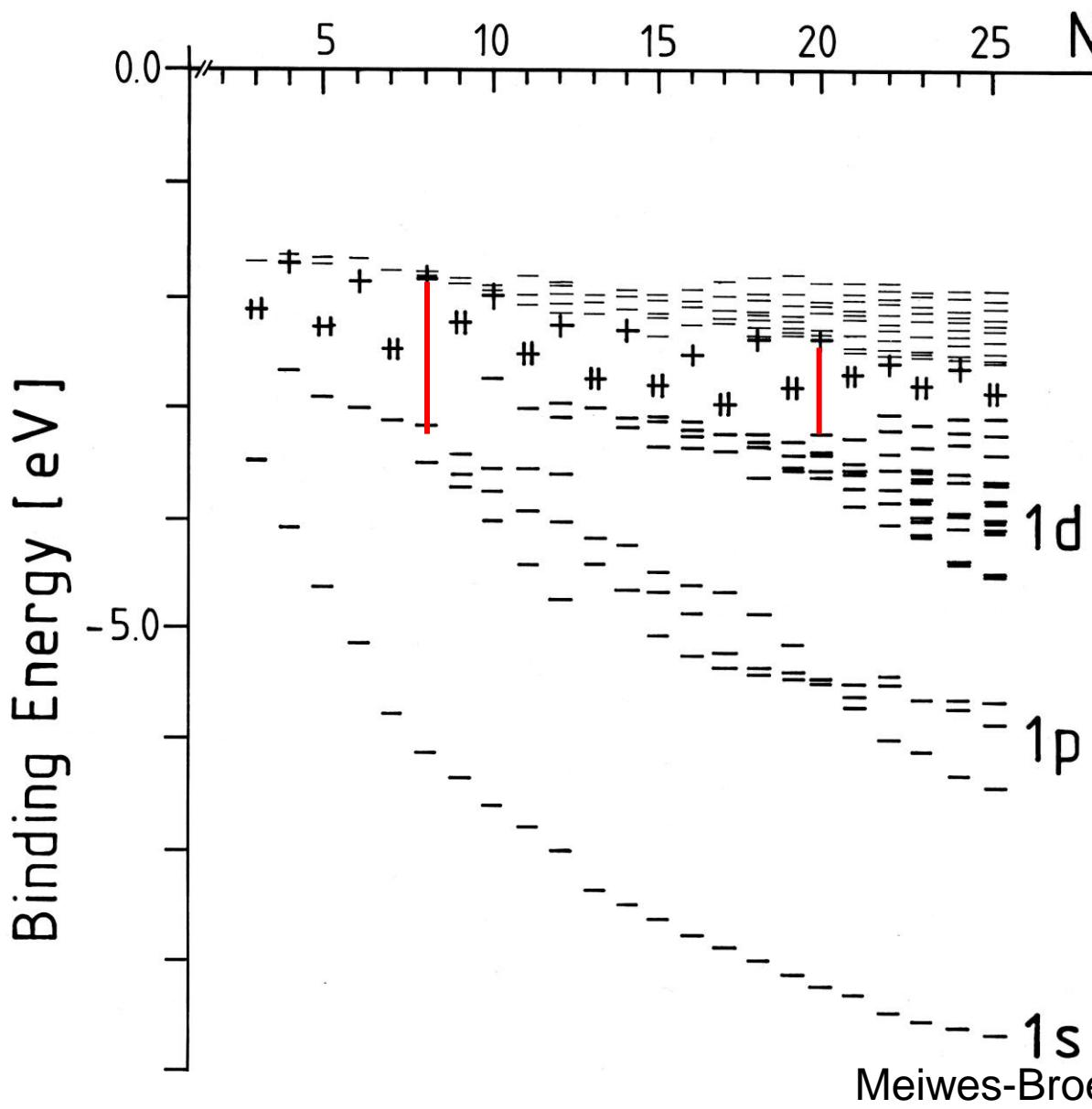


comparison with the jellium model

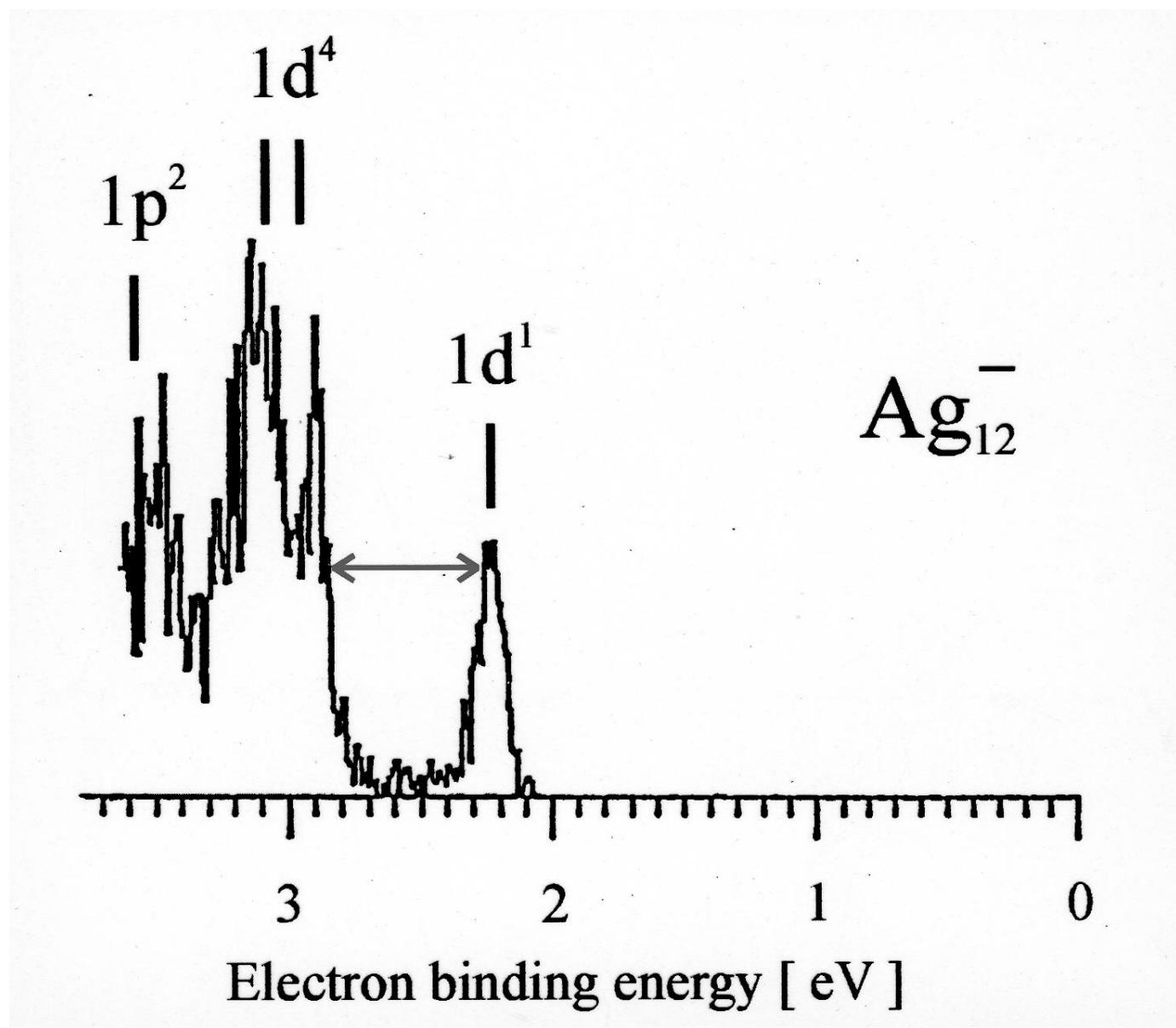


pronounced energy gaps after 8 and 20 electrons, but there are more gaps due to lifting of degeneracy

Ag_N^- effective medium theory



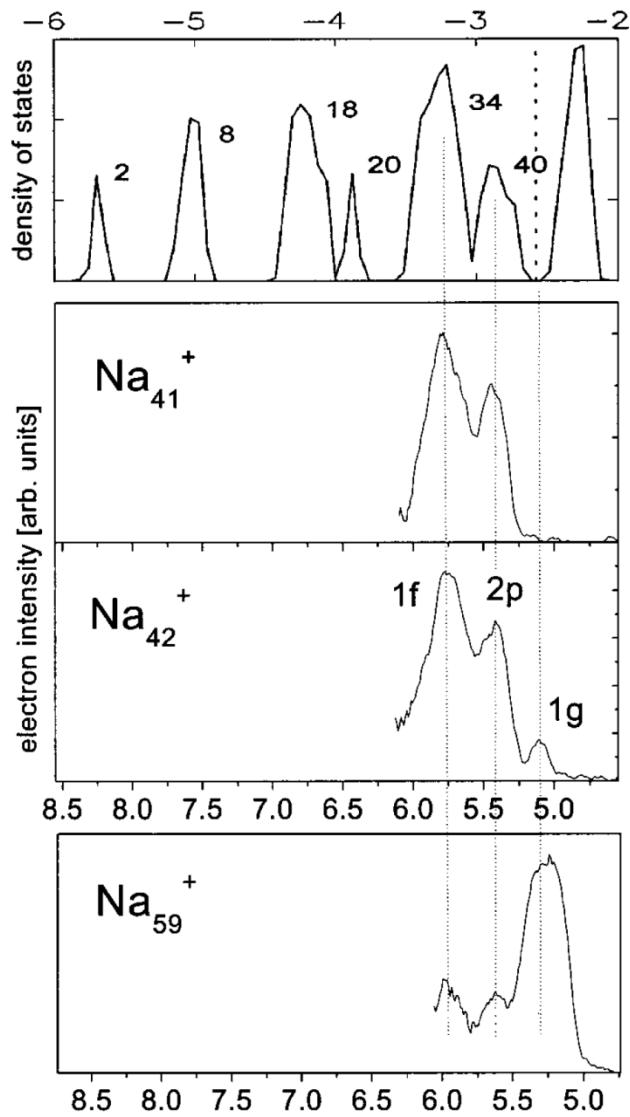
Better theory:
One-electron energy levels
of An_N^- by tight-binding
calculations within the
effective medium theory



fine details of the electronic structure can be resolved

comparison PES with jellium calculations

Density of states from
KS single-particle
energy eigenvalues

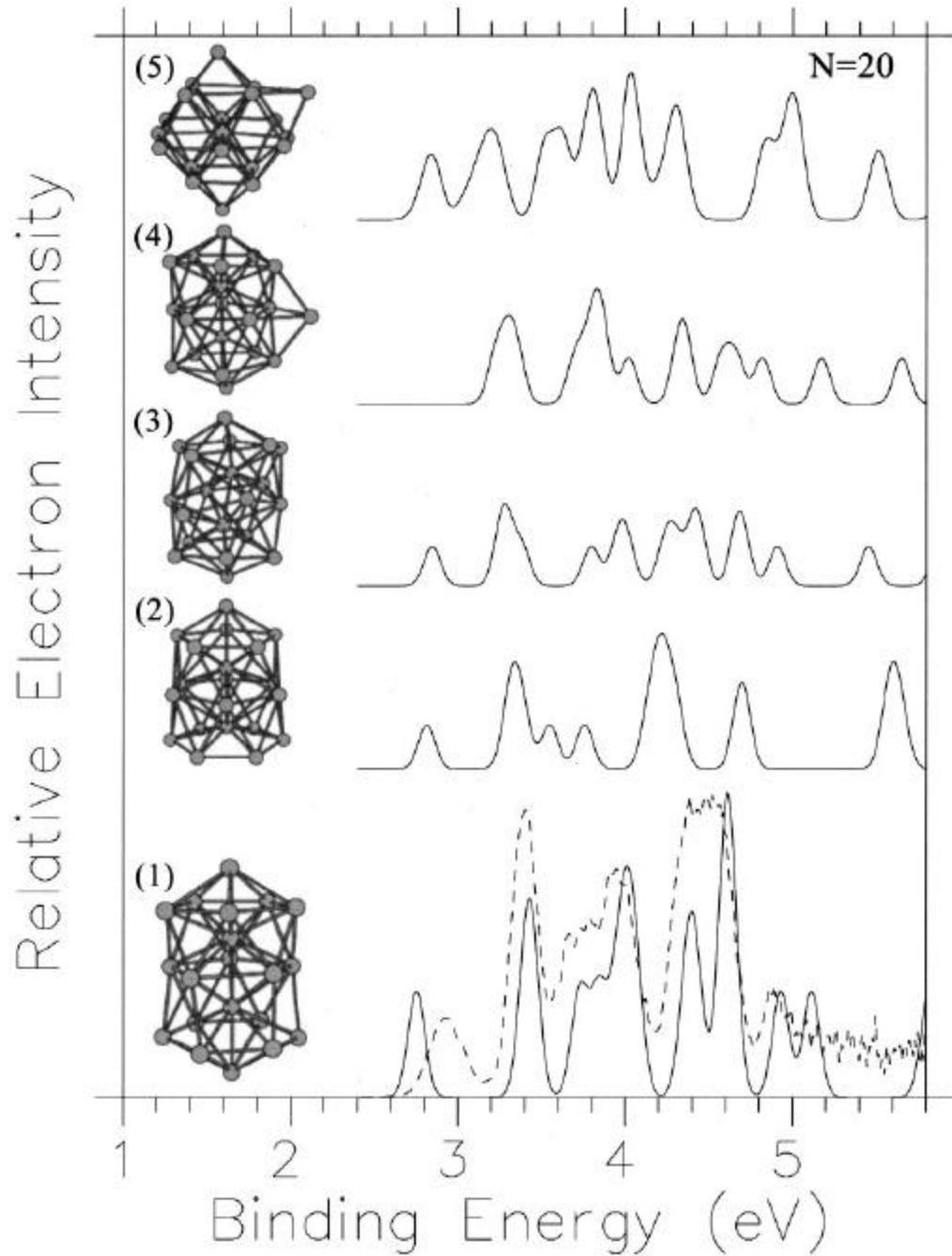


Al_{20} PES vs. calc.

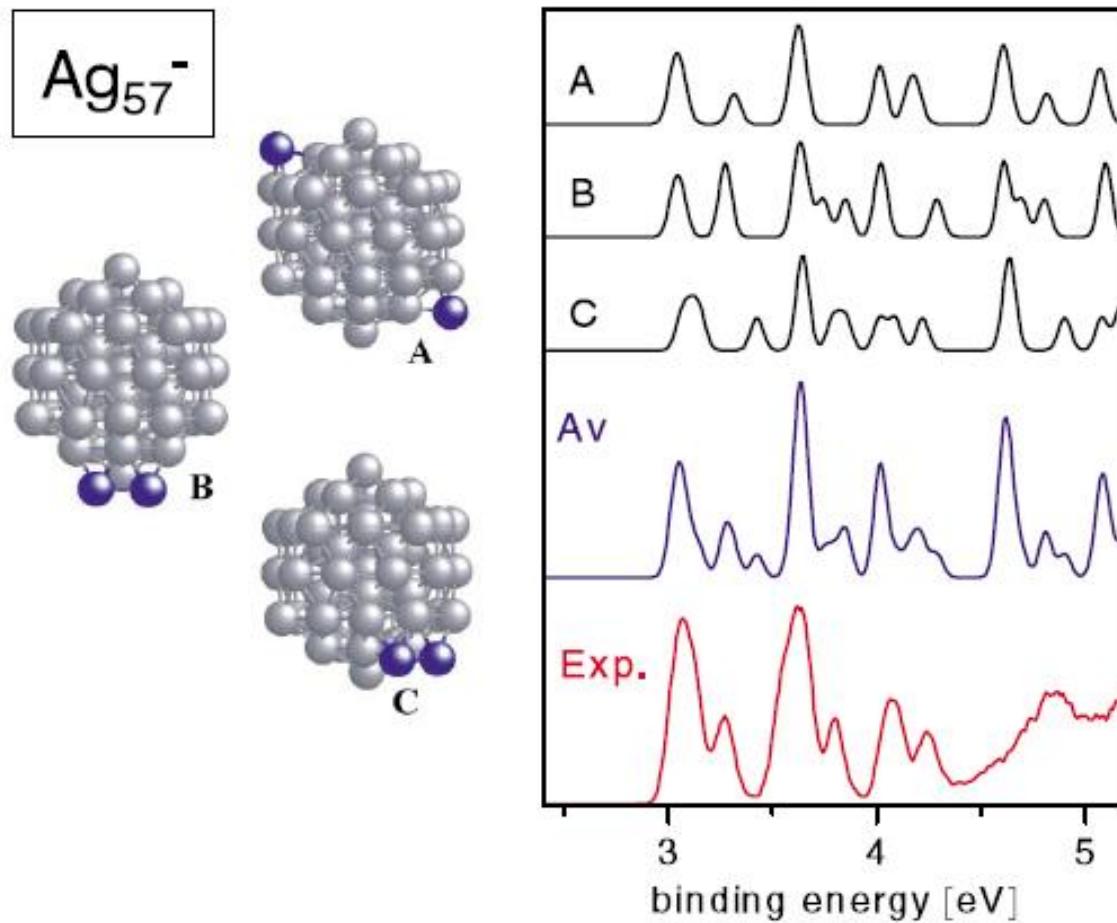
in this case:
mainly one isomer contributes

dashed curve: measured
spectrum

Akola et al., PRB 62, 13 216
(2000)



close-lying isomers



here: all three isomers contribute to the experimental spectrum

PES on coinage metal clusters

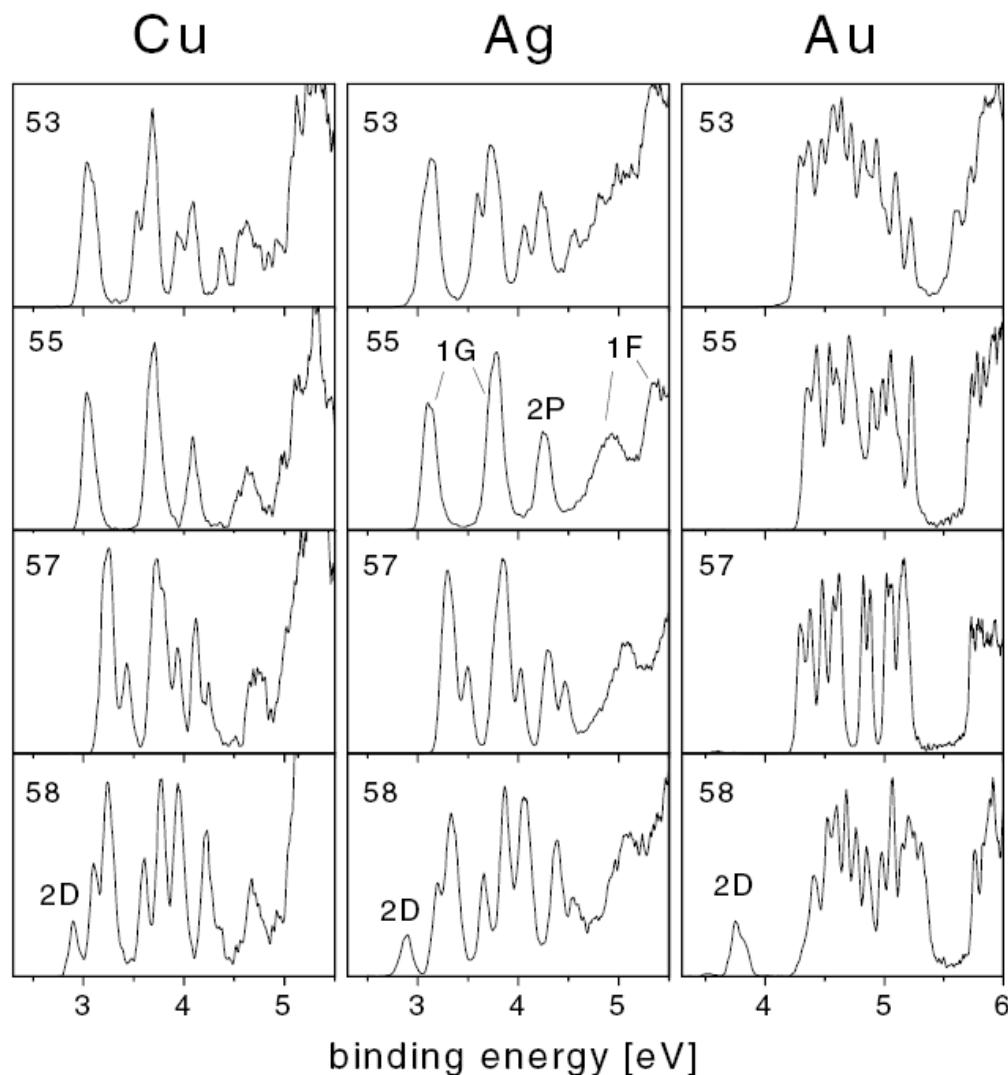
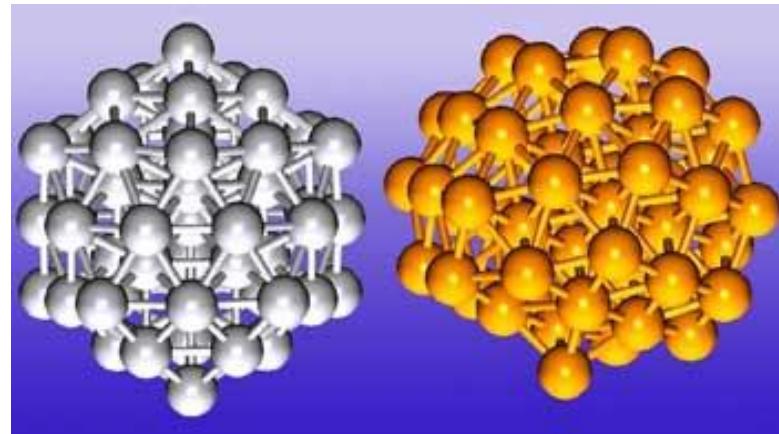


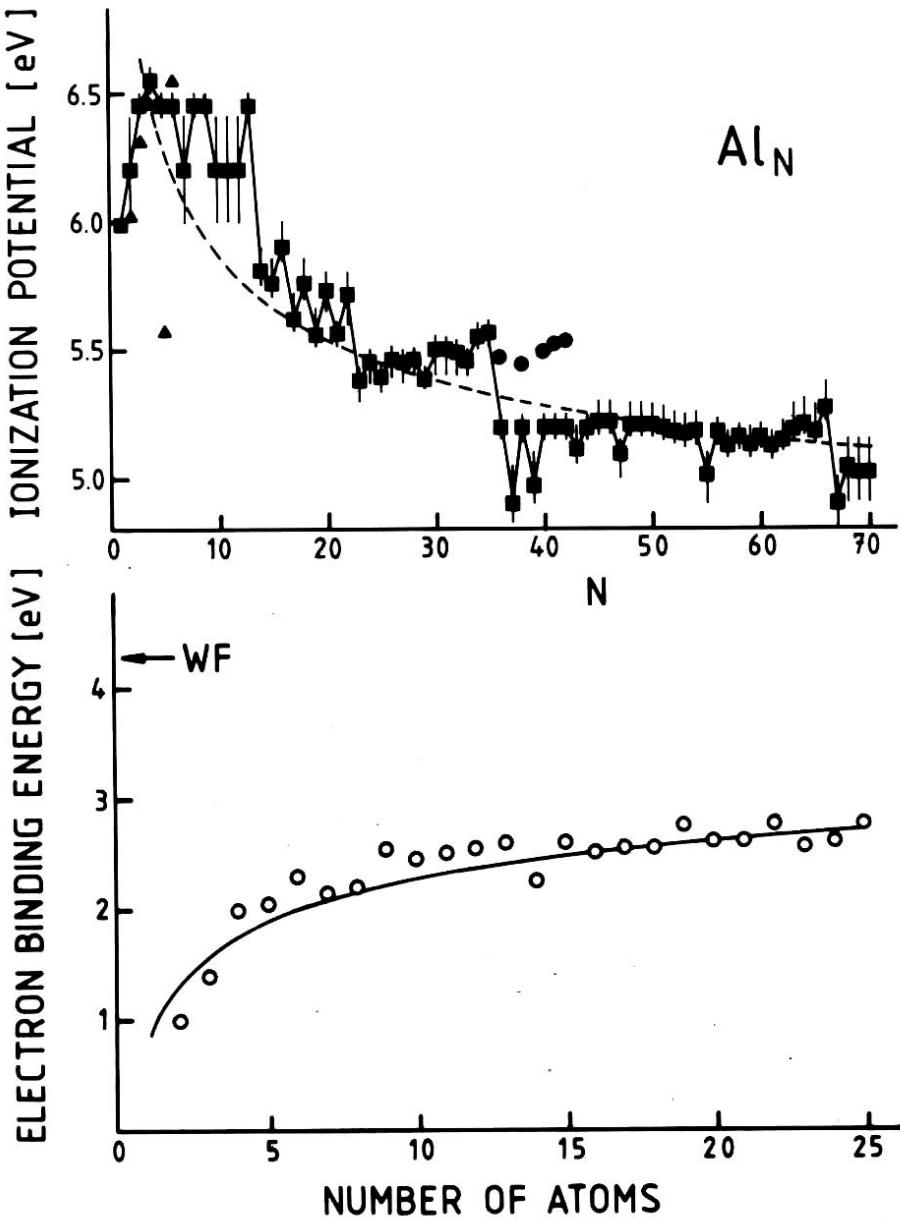
FIG. 1. Photoelectron spectra of Cu_n^- , Ag_n^- , and Au_n^- ($n = 53, 55, 57, 58$) obtained at a photon energy of 6.42 eV.



chemically similar systems may have similar PE spectra.
Exception: Gold, due to relativistic effects

Hannu Hakkinen, Michael Moseler, Oleg Kostko, Nina Morgner, Margarita Astruc Hoffmann, and Bernd v. Issendorff, PRL 93 093401(2004)

Trends in photoemission threshold energies

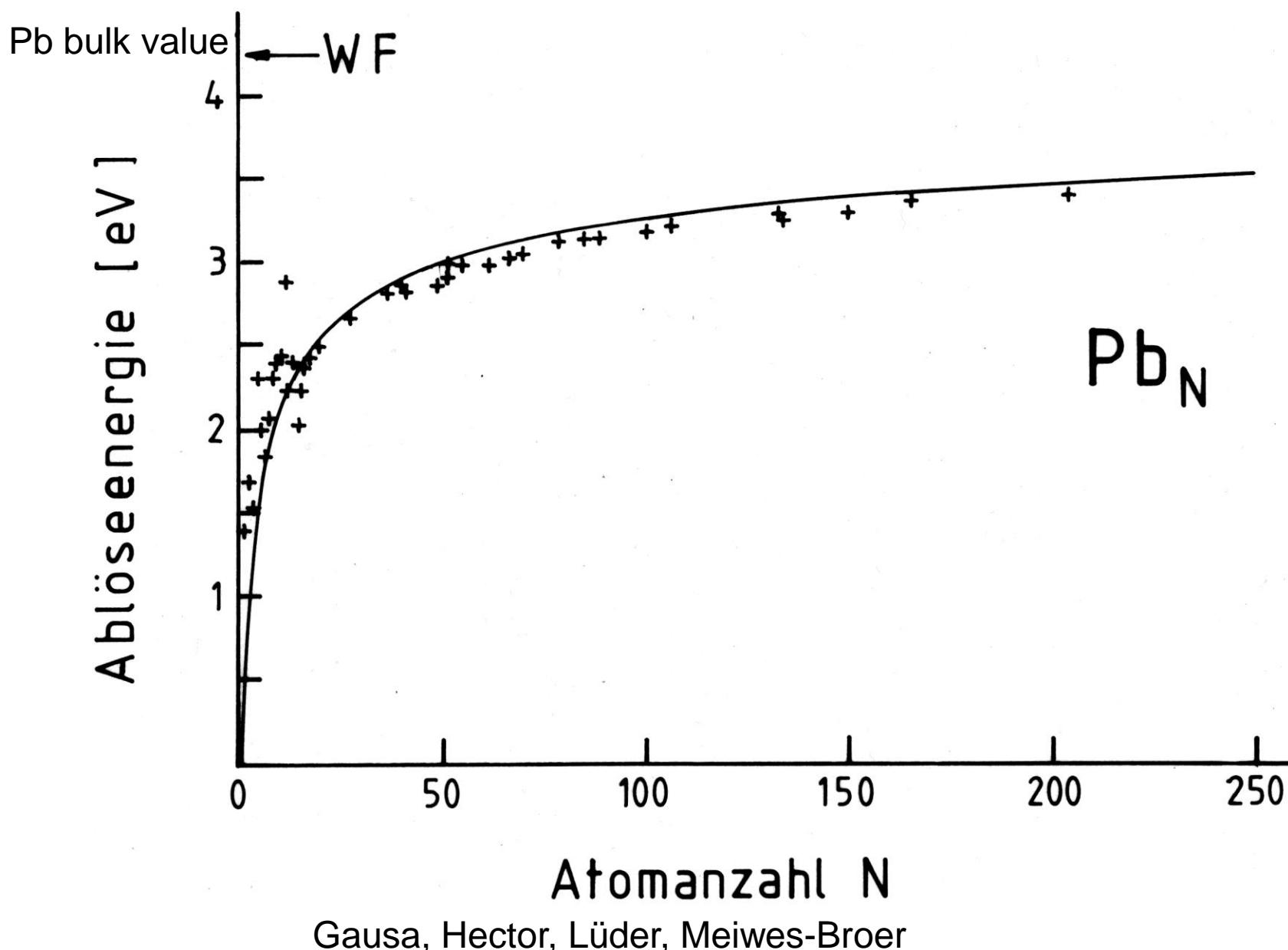


generally:

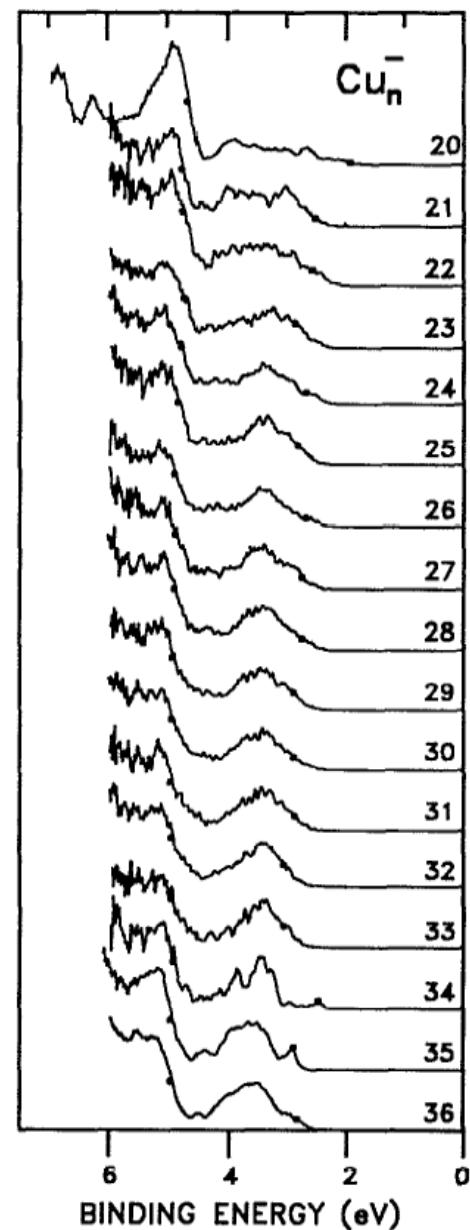
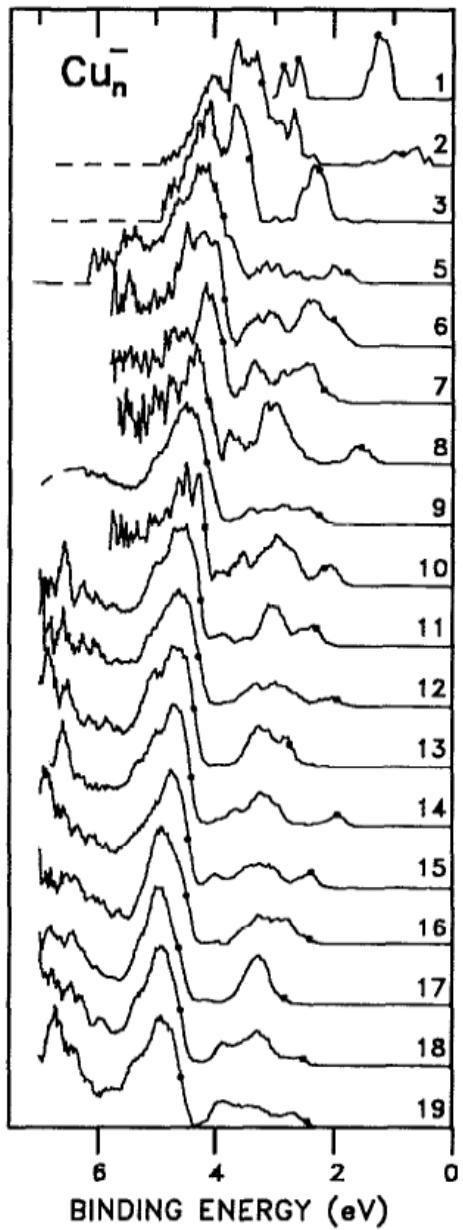
- IPs decrease with increasing N
- electron detachment en. or EAs rise with increasing N

Ionization potentials (top, by R. Whetten) and electron affinities (bottom, Meiws-Broer group) of Aluminium clusters

threshold energies: electron detachment

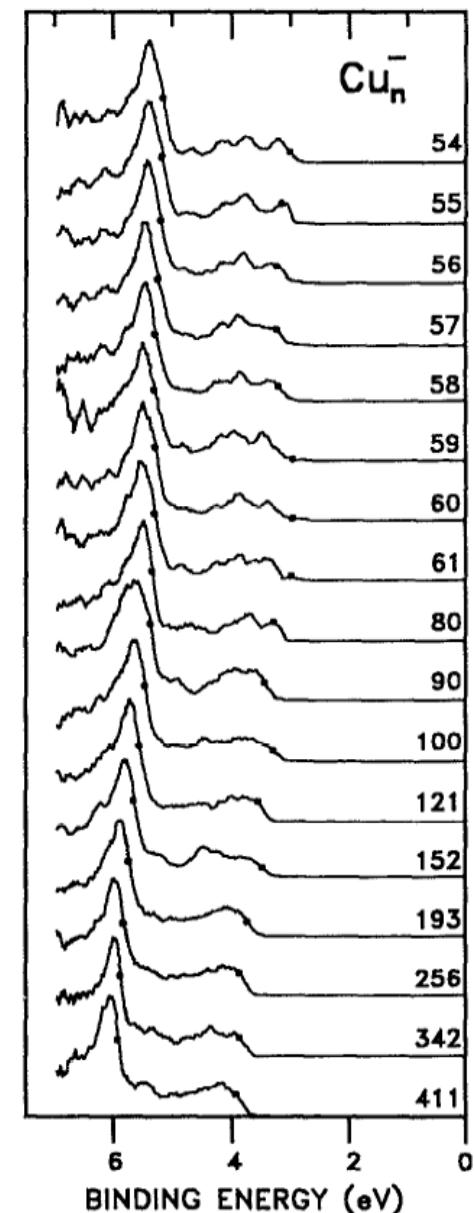
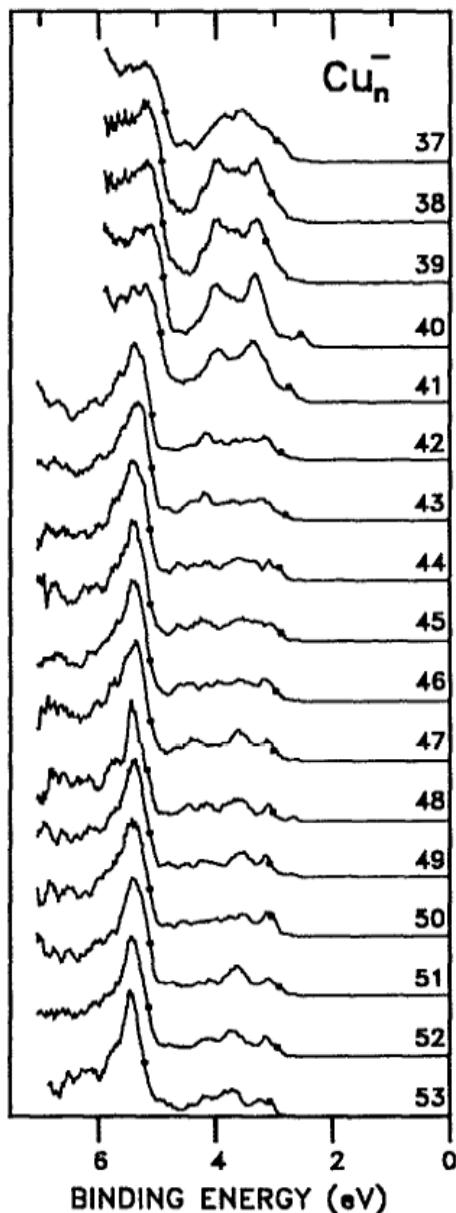


Cu_N^- PE thresholds
rise with increasing
cluster size

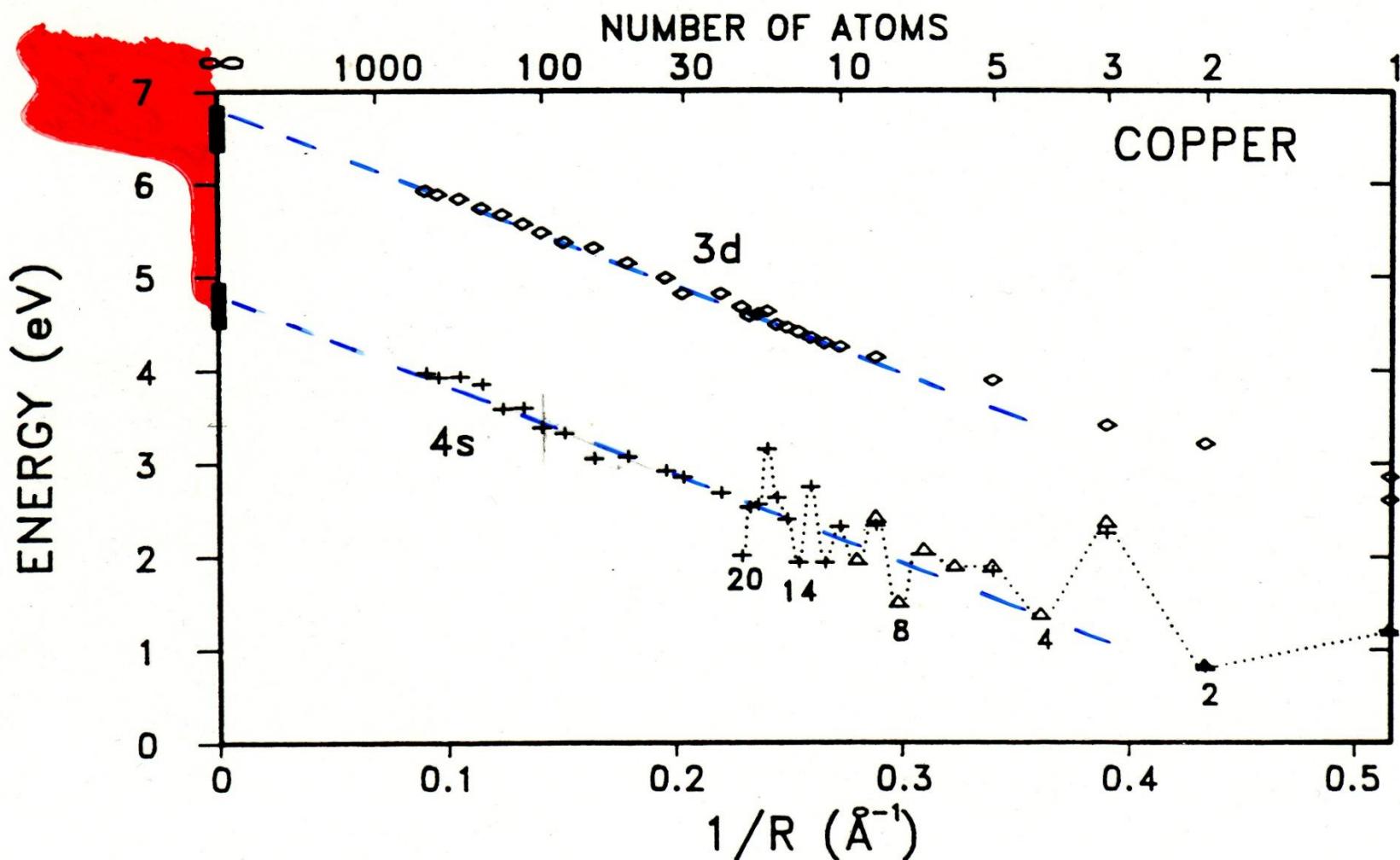


Cu_N^- PES

threshold energies
increase with N

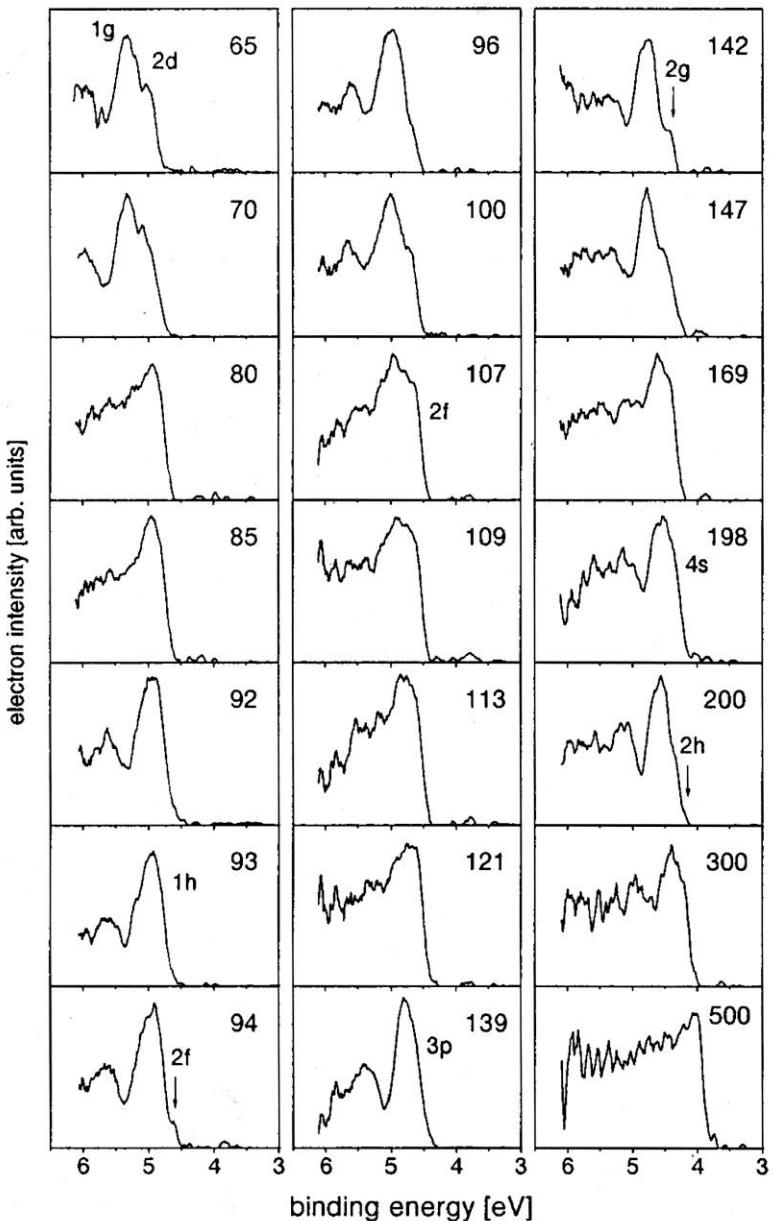


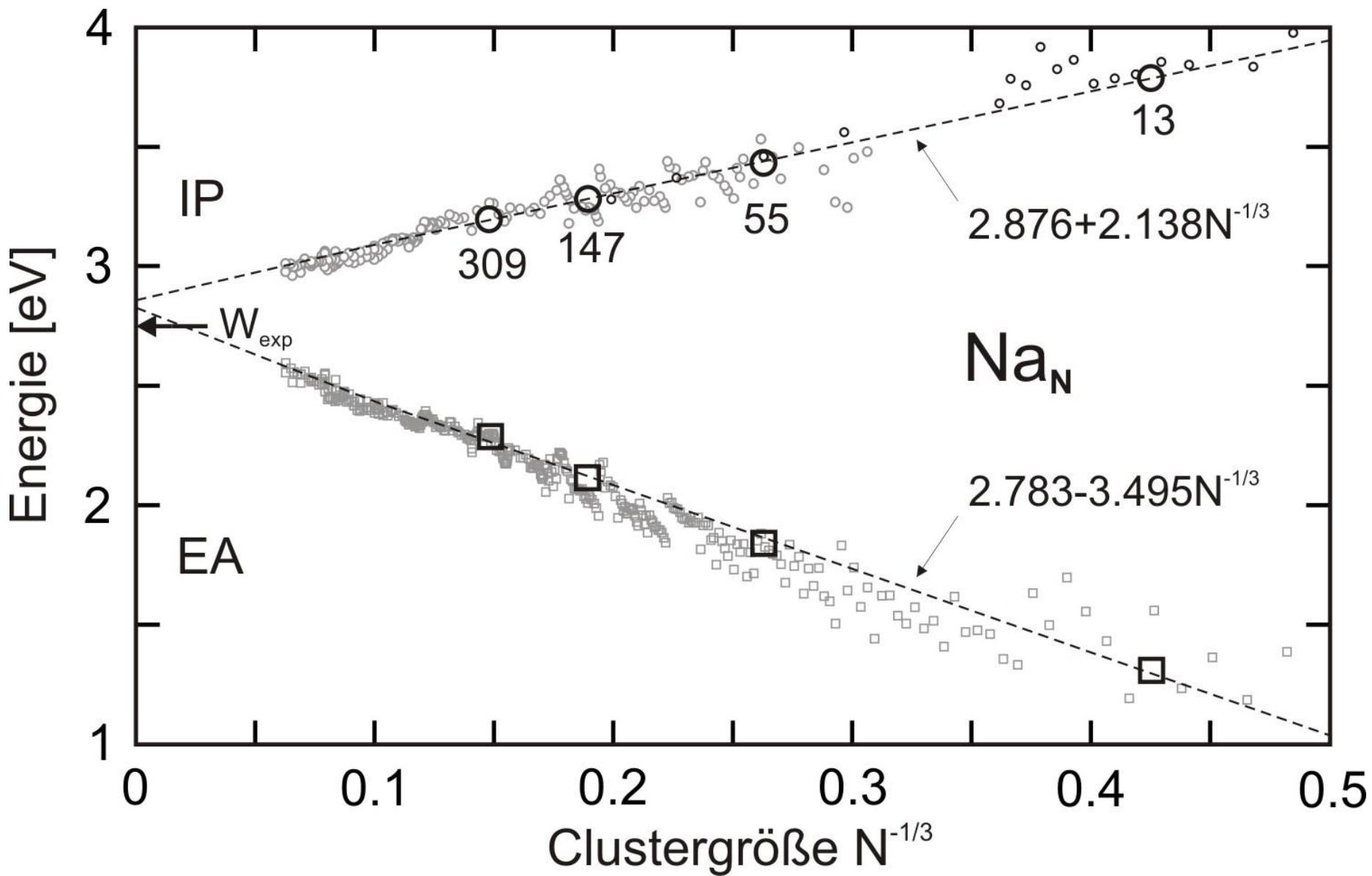
N-dependent shift of low-lying levels: 3d in Cu_N



photoionization thresholds of neutral clusters

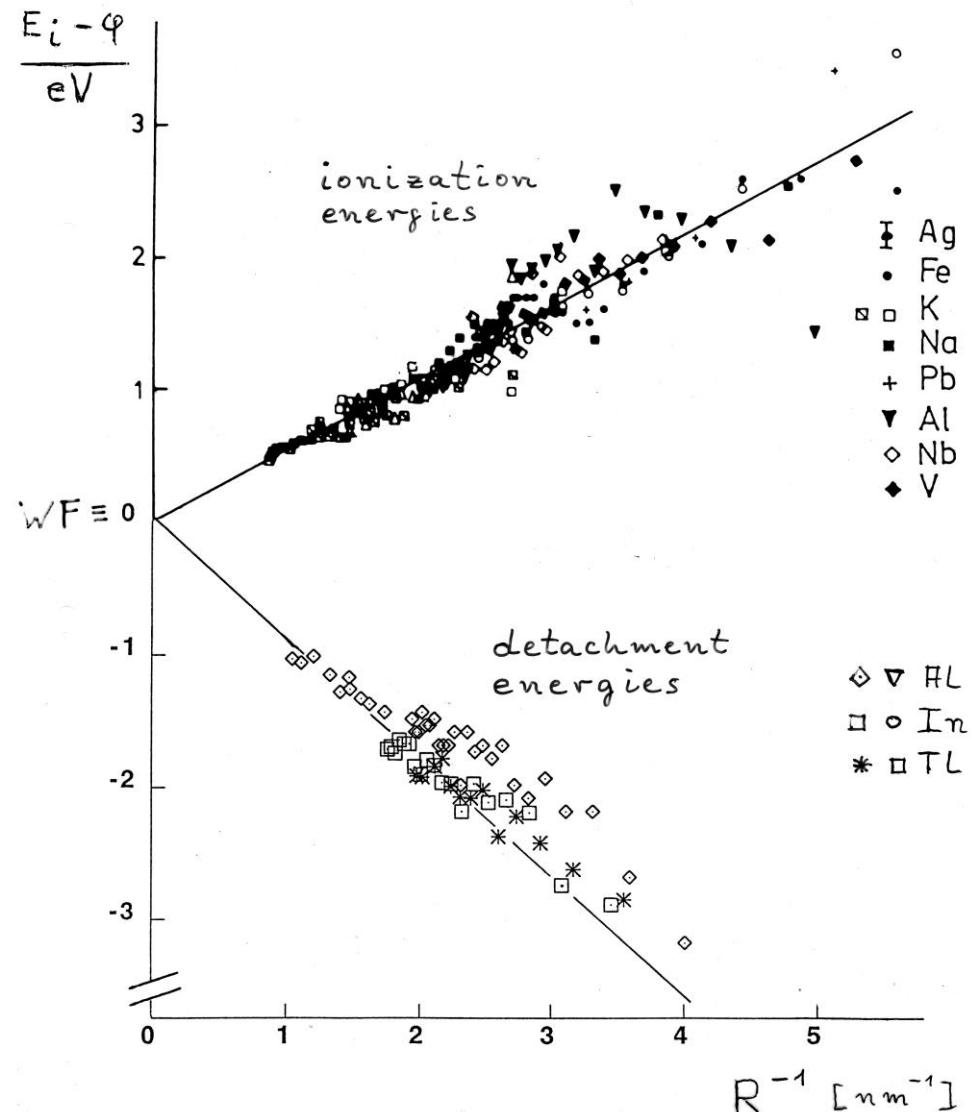
Na⁺ photoelectron spectra





DFT calculations Fennel et al., Rostock, measurements von Issendorff et al., Freiburg

experimental values for the IP and the EA



generally:

- the IPs decrease with increasing N
- the EAs rise with increasing N

Parametrization:

$$IP(R) = WF + \alpha \frac{e^2}{R} \quad \text{with } \alpha = 3/8 \dots 1/2$$

$$EA(R) = WF - \beta \frac{e^2}{R} \quad \text{with } \beta = 1/2 \dots 5/8$$

$\alpha = \beta = 1/2$ corresponds to the charging energy of a jellium sphere, deviations arise from QM exchange and correlation

let us evaluate IP and EA simultaneously

$$IP(R) = WF + \alpha \frac{e^2}{R} \quad \text{with } \alpha = 3/8 \dots 1/2$$

$$EA(R) = WF - \beta \frac{e^2}{R} \quad \text{with } \beta = 1/2 \dots 5/8$$

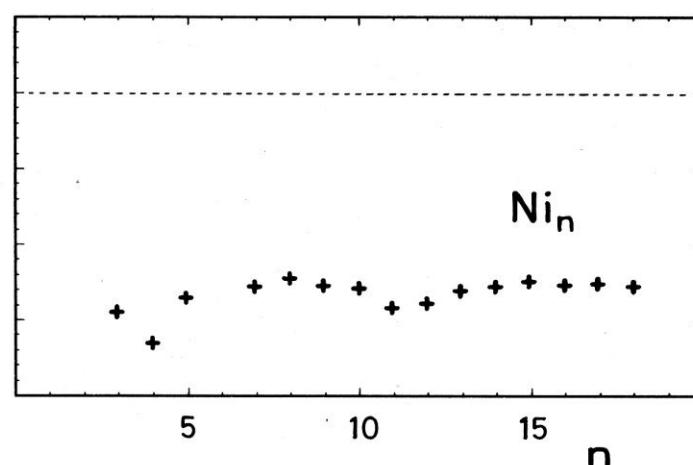
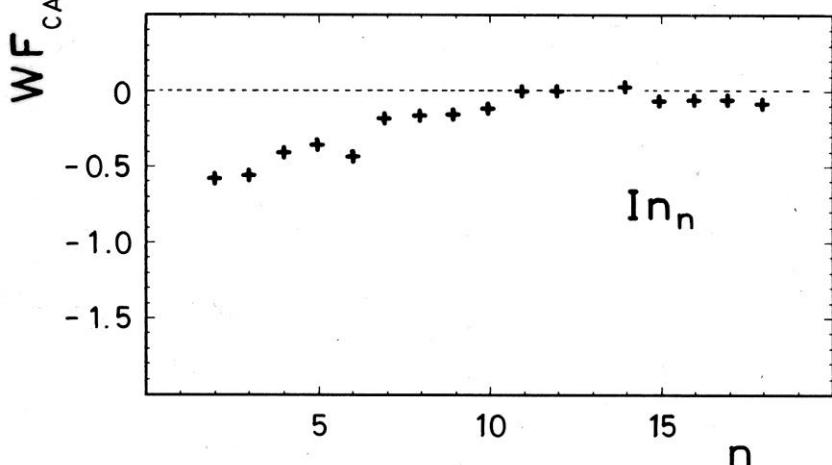
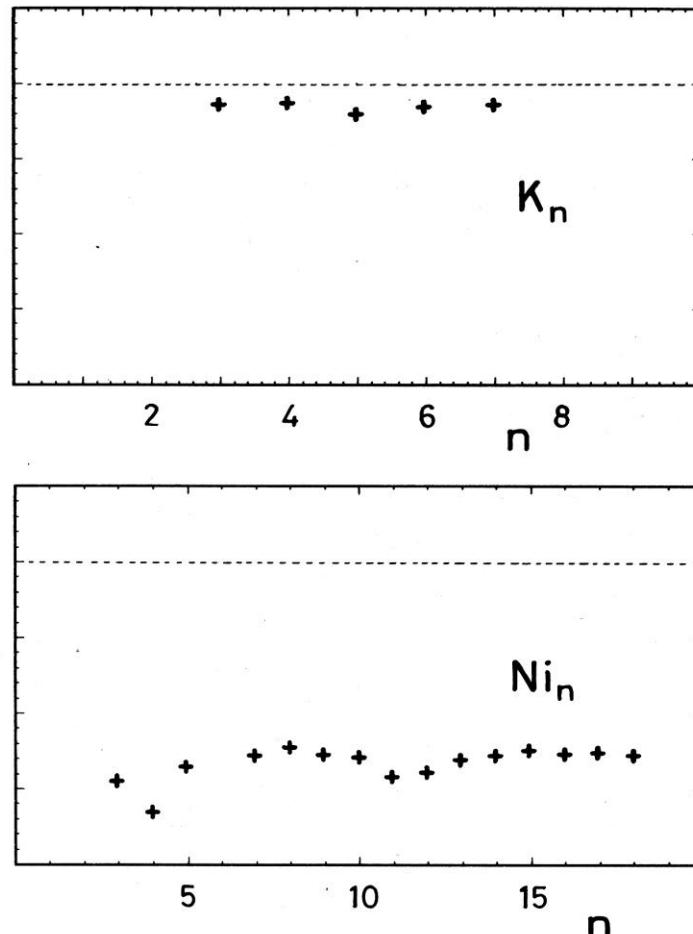
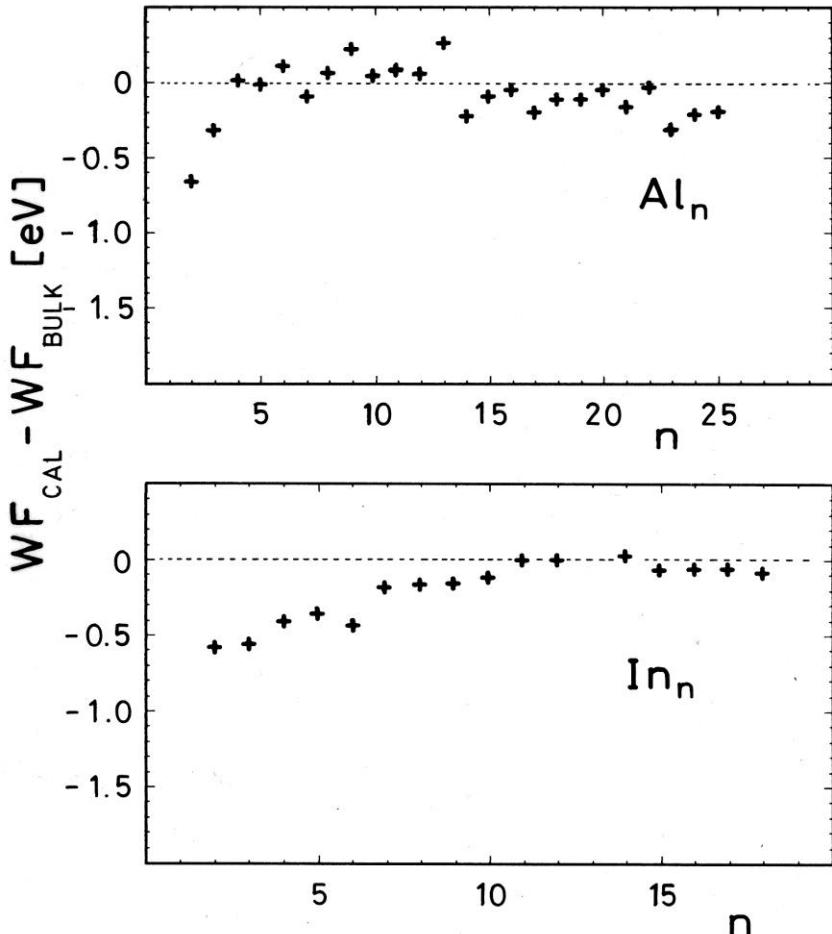
$\alpha - \beta$ is small

solve for WF: $WF_{cal} = \frac{1}{2}(IP + EA) + \frac{1}{2} \frac{e^2}{R} (b - a)$

$$WF_{cal} \approx \frac{1}{2}(IP + EA)$$

thus the work function should be the mean value of IP and EA !

differences between measured IP and EA and bulk values



Small or no differences hint at free electron (or: ideal metal droplet) behaviour
Meiwes-Broer in *Advances in Metal and Semiconductor Clusters*, Vol. 1
M. Duncan, Ed., JAI Press Inc., 1993