

lecture 20.1.2011

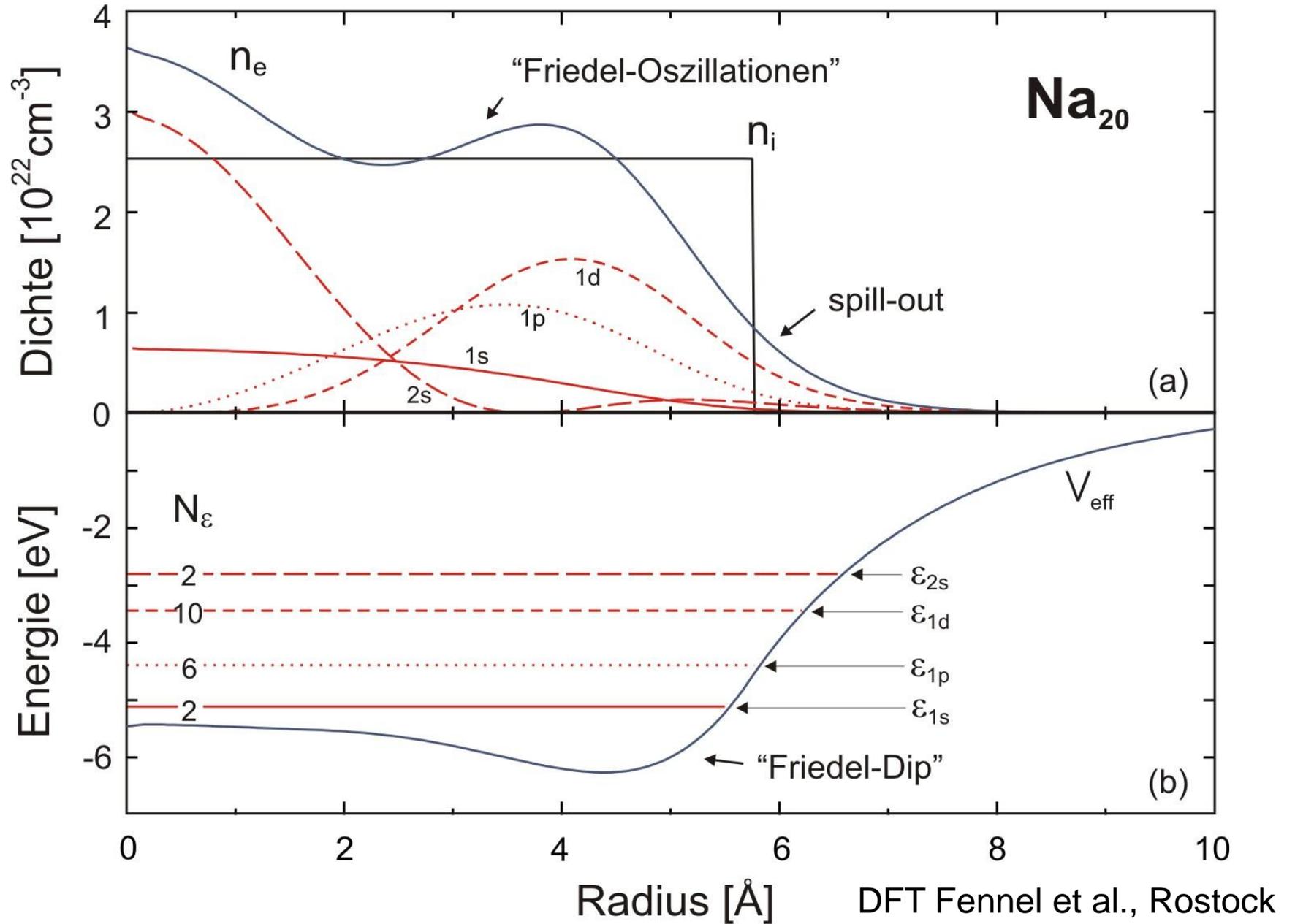
we had so far:

- binding in clusters and their appearances in mass spectra
 - d) metallic bonding
- photoelectron spectroscopy

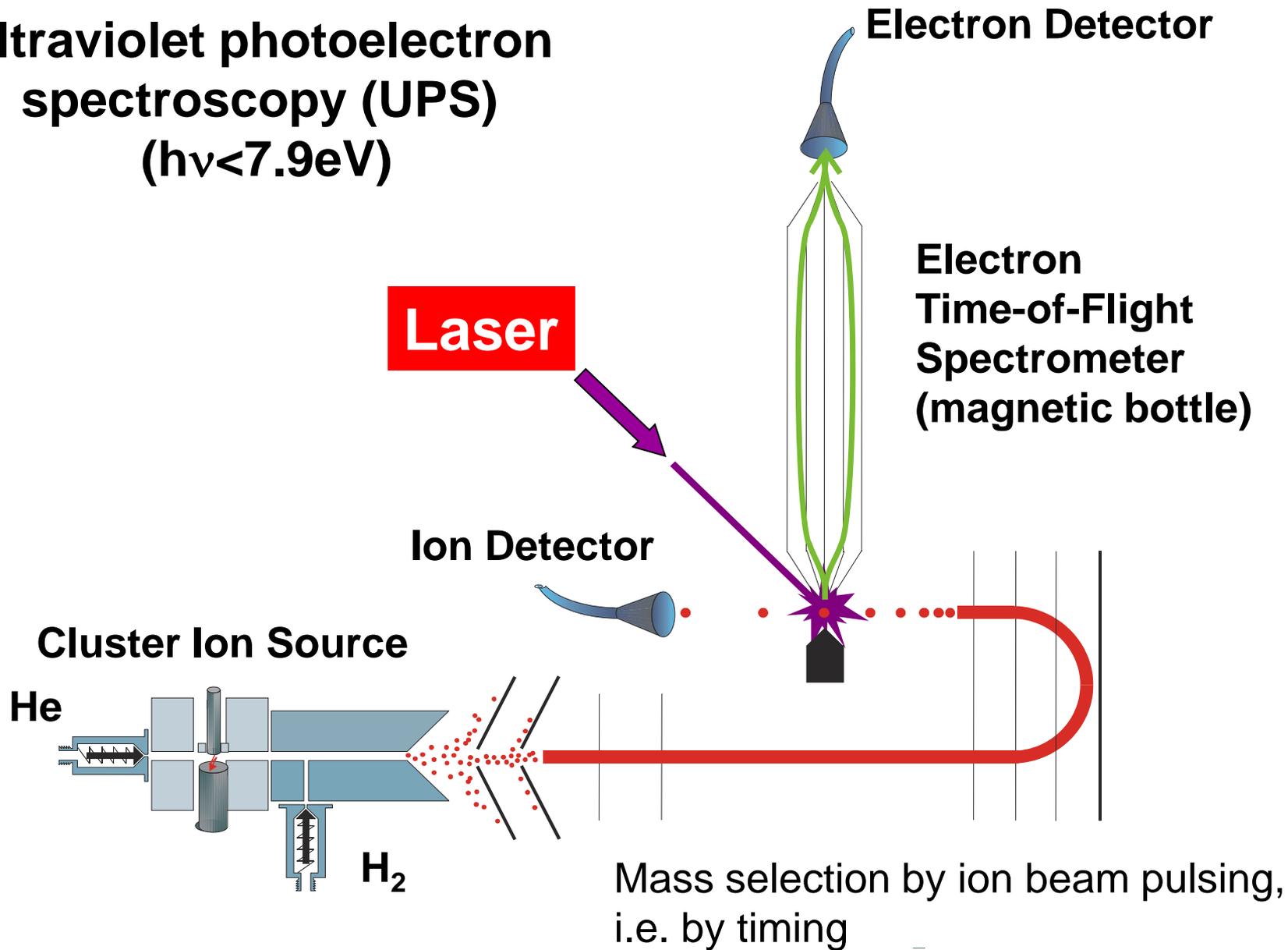
today

- more photoelectron spectroscopy
- optical properties of metal (jellium) clusters

the jellium model

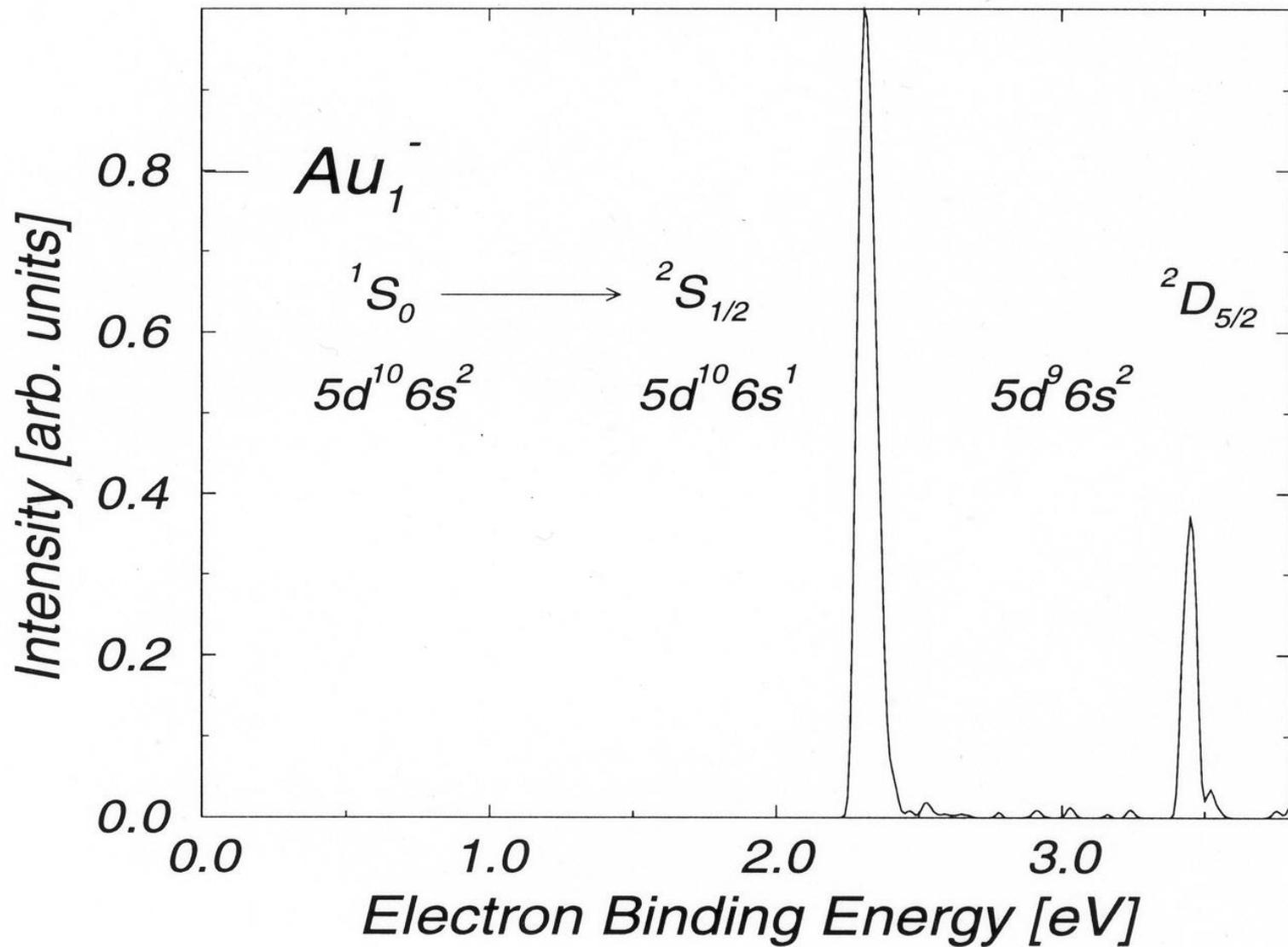


**ultraviolet photoelectron
spectroscopy (UPS)
($h\nu < 7.9\text{eV}$)**

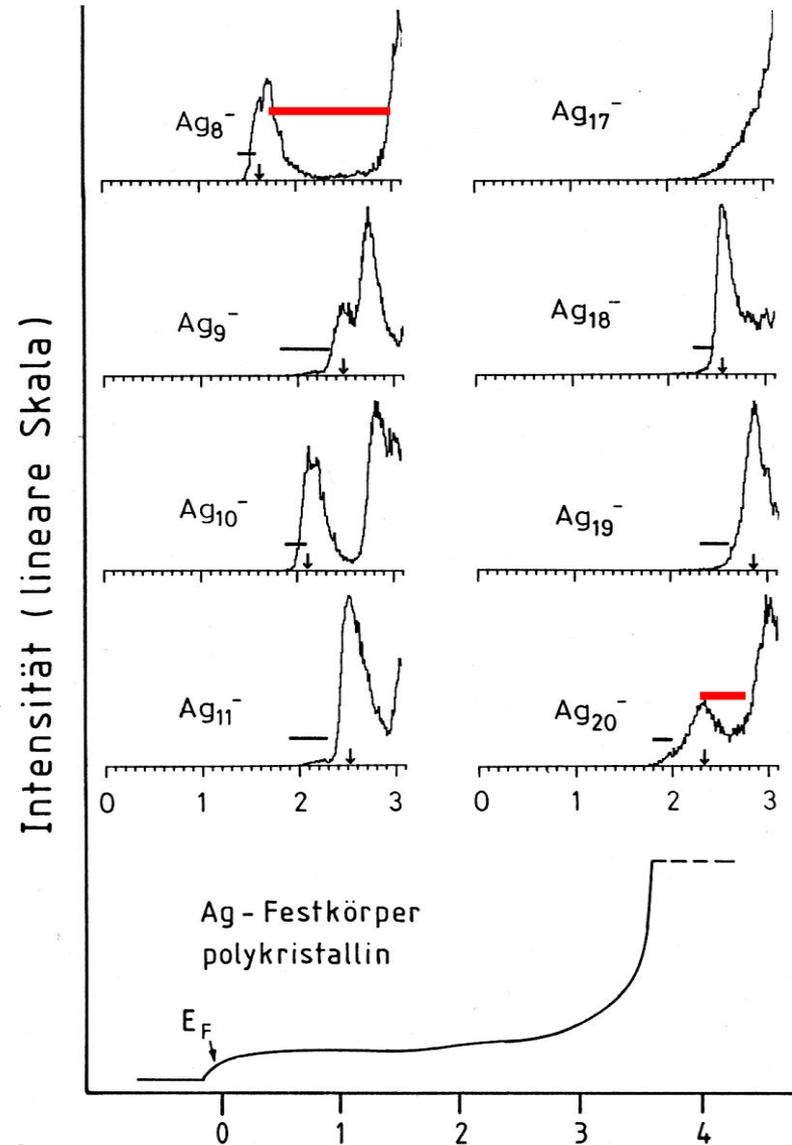
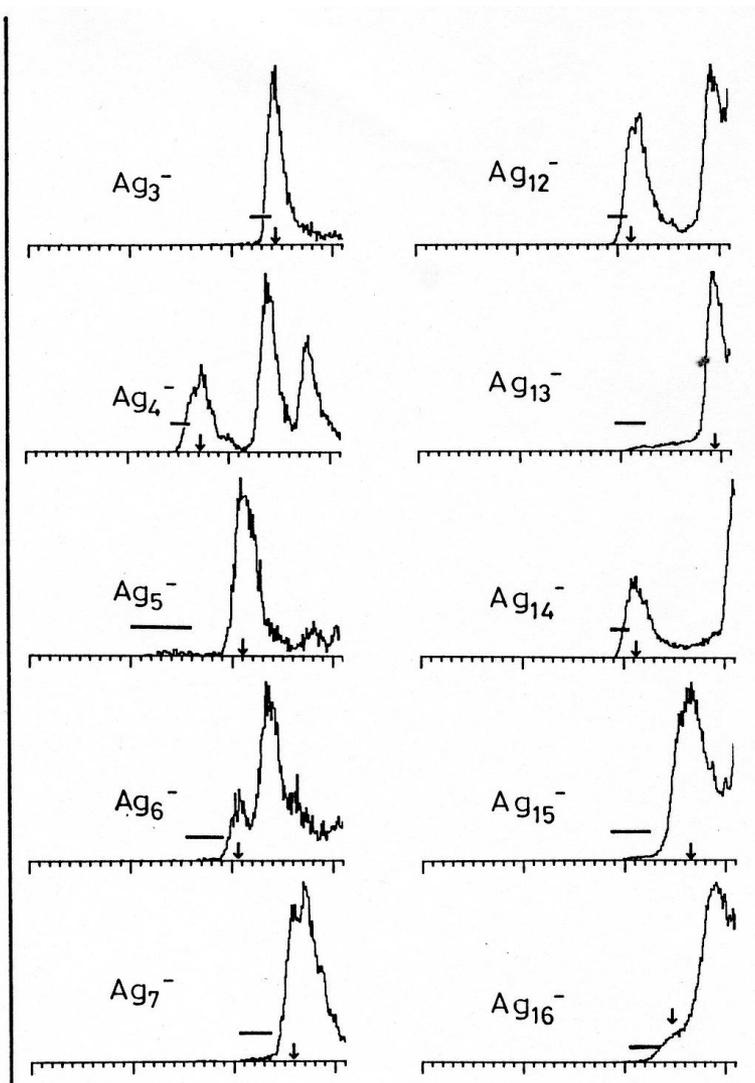


Setup Ganteför group, Konstanz

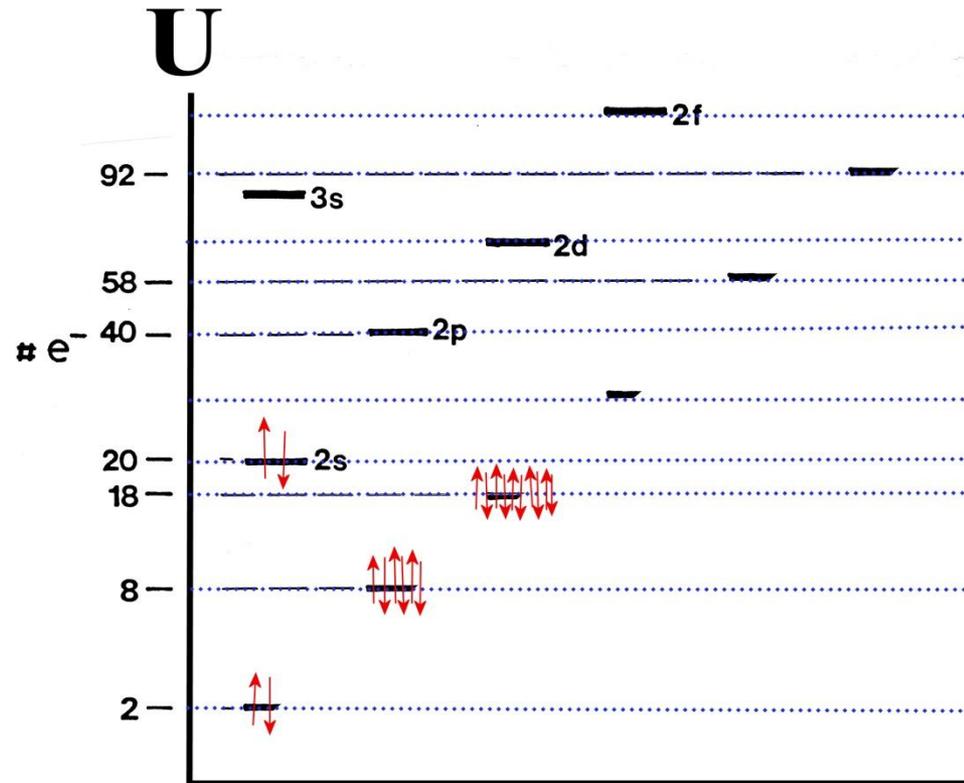
calibration magnetic bottle spectrometer with Au₁⁻



photoelectron spectra from Ag_N^-

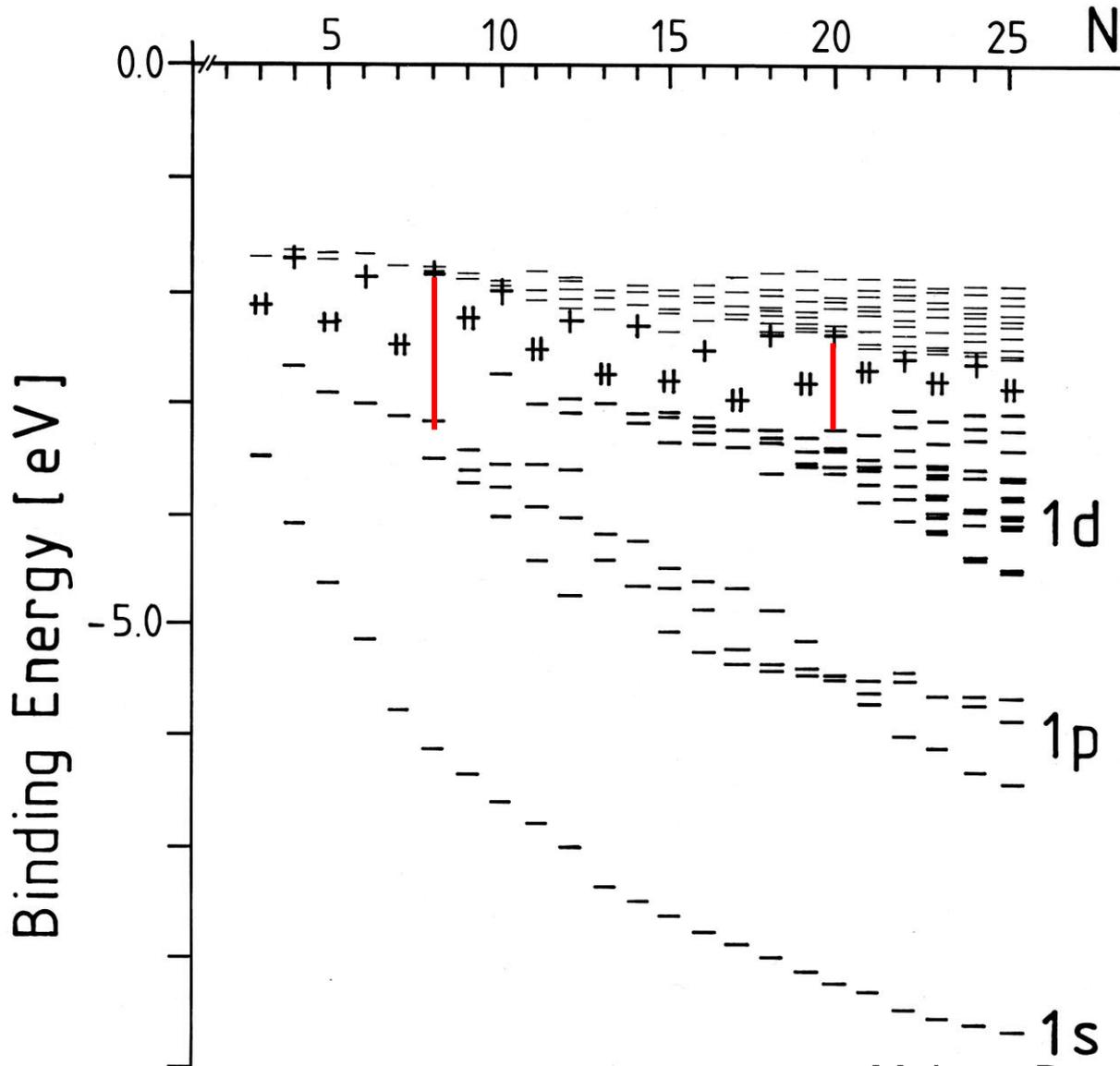


comparison with the jellium model

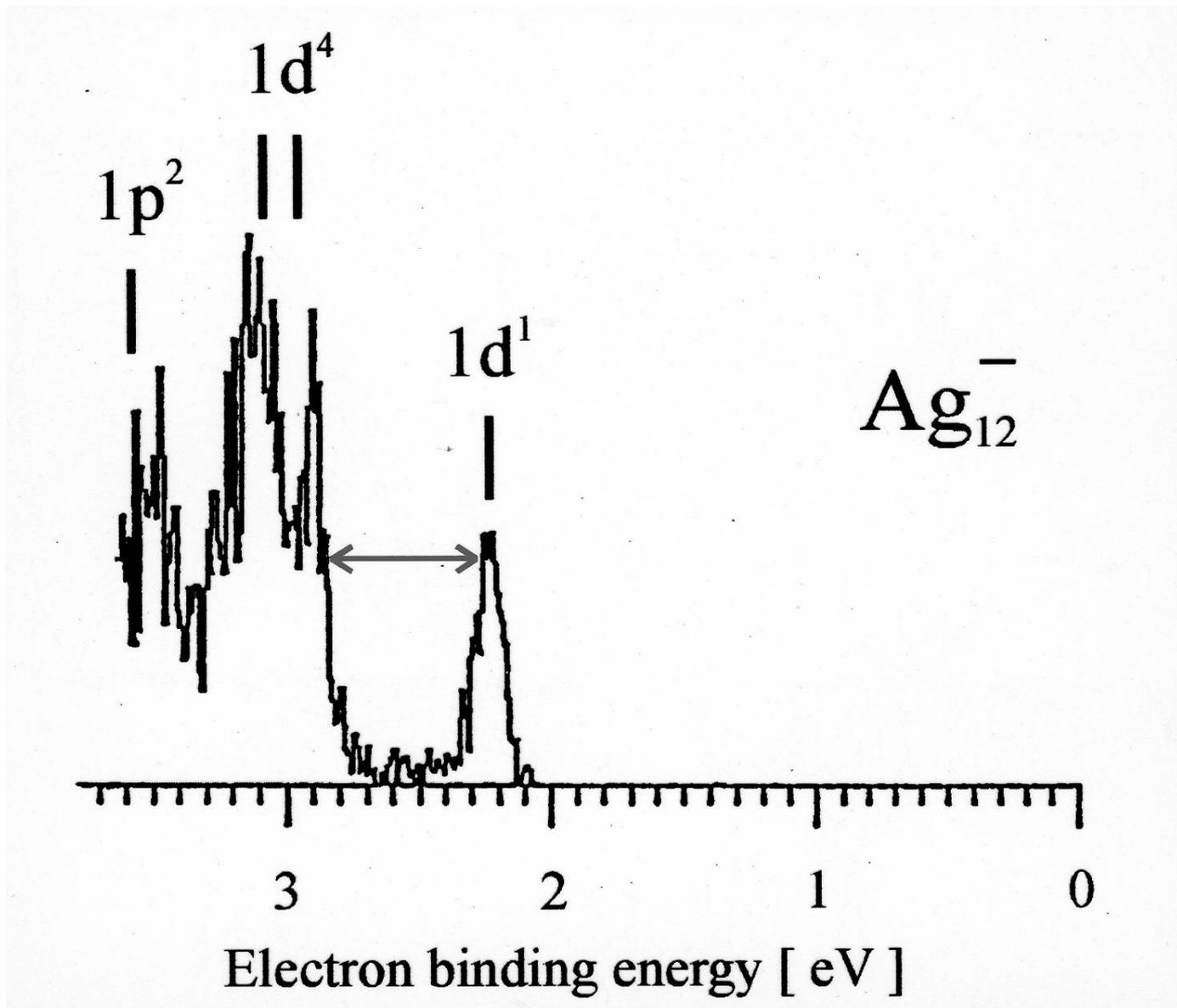


pronounced energy gaps after 8 and 20 electrons, but there are more gaps due to lifting of degeneracy

Ag_N^- effective medium theory



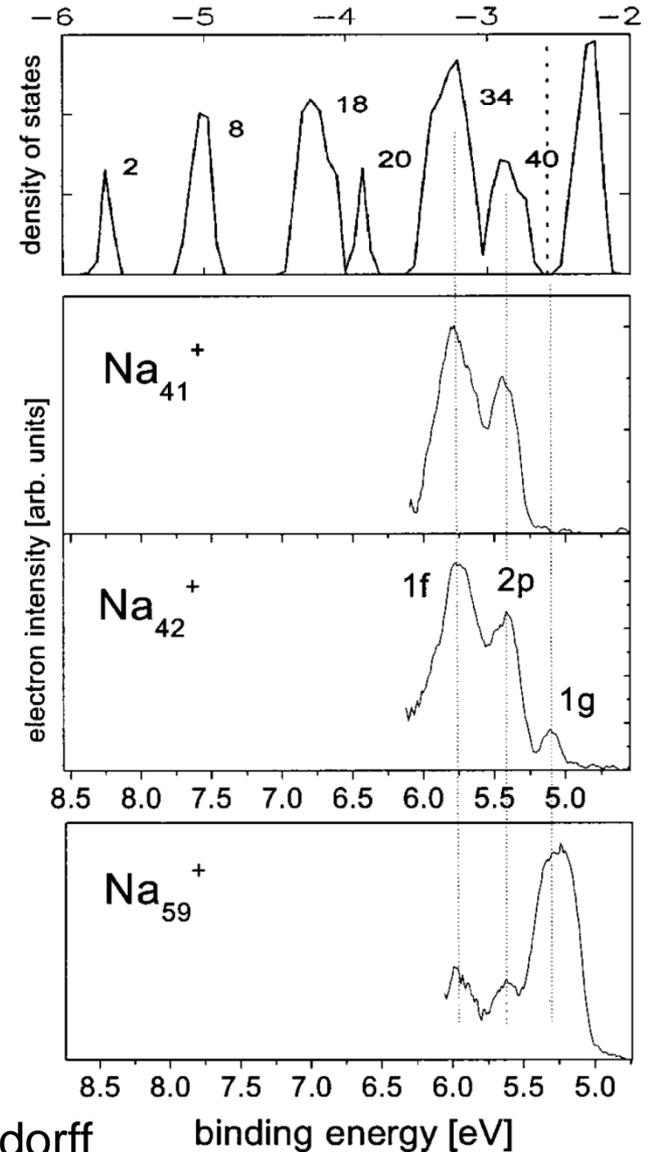
Better theory:
One-electron energy levels
of An_N^- by tight-binding
calculations within the
effective medium theory



fine details of the electronic structure can be resolved

comparison PES with jellium calculations

Density of states from
KS single-particle
energy eigenvalues



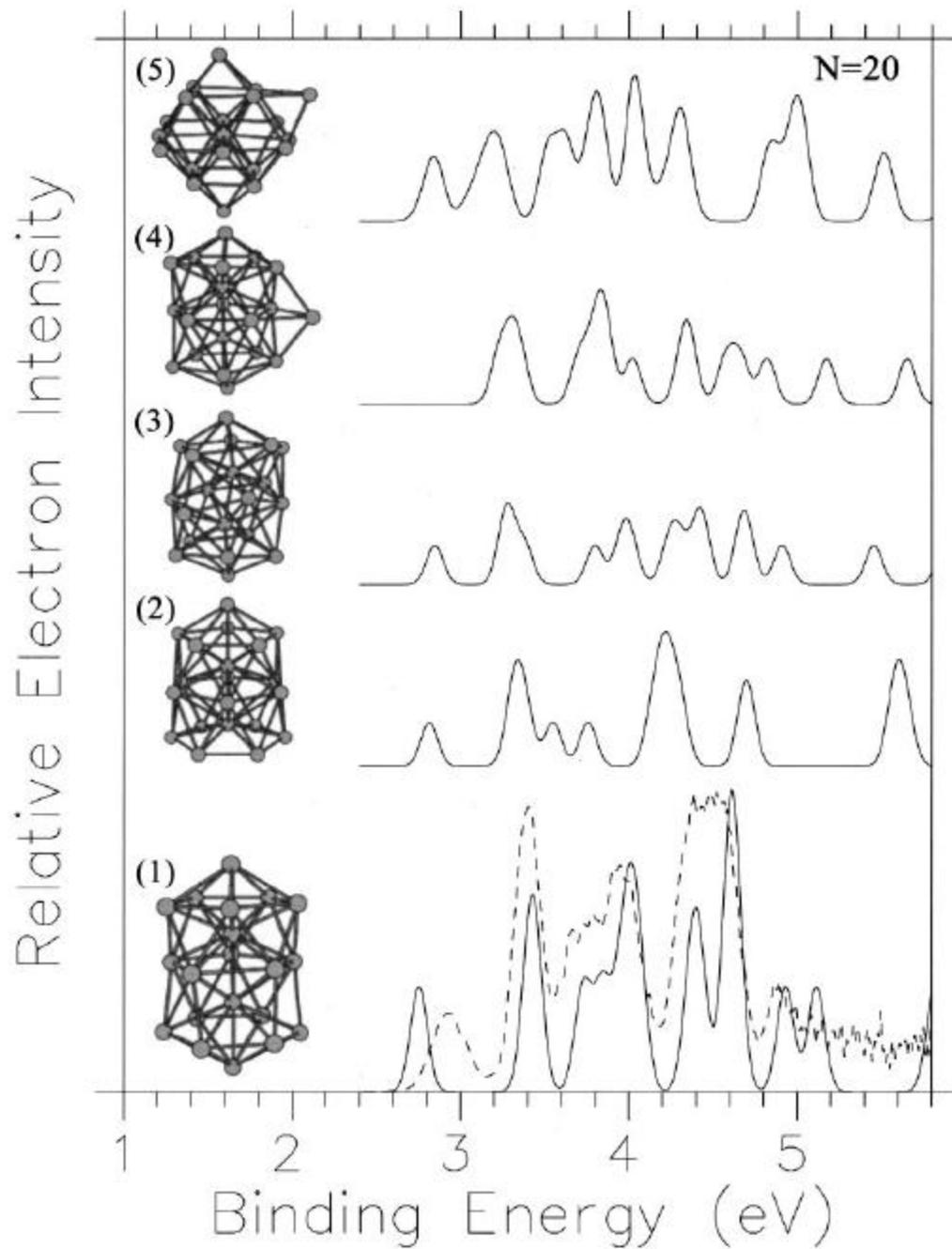
G. Wrigge, M. Astruc Hoffmann, and B. v. Issendorff
PRA65, 063201(2002)

Al₂₀ PES vs. calc.

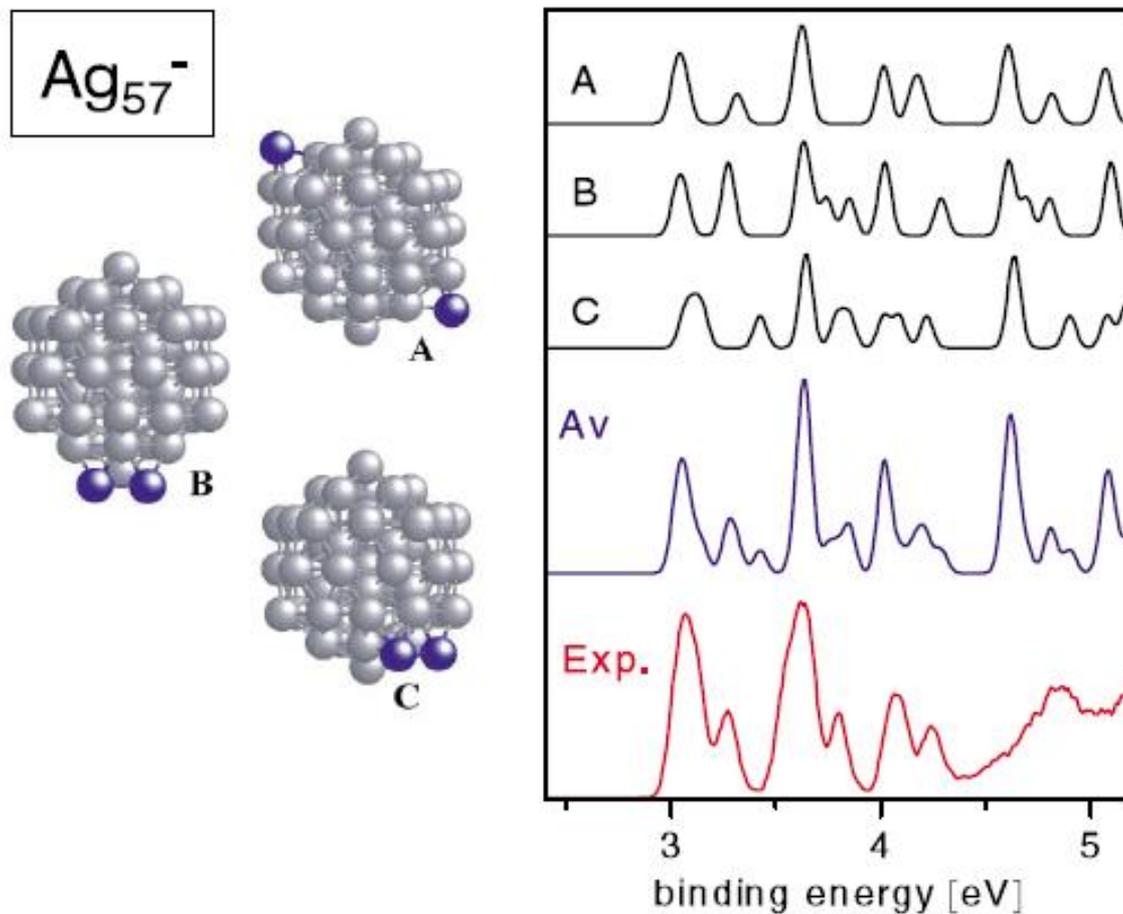
in this case:
mainly one isomer contributes

dashed curve: measured
spectrum

Akola et al., PRB 62, 13 216
(2000)

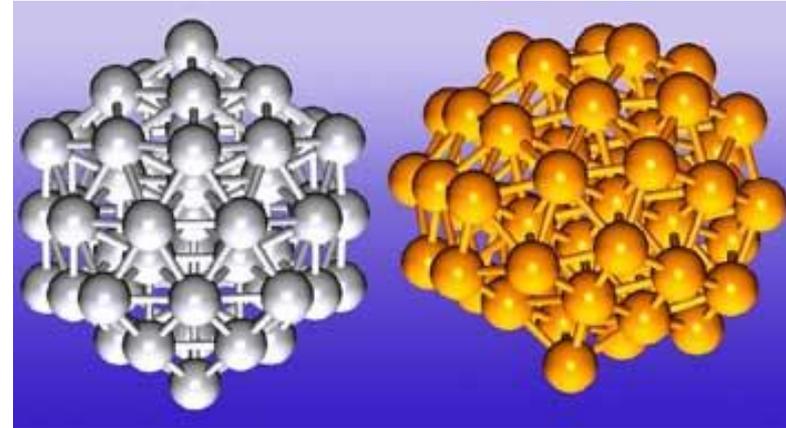
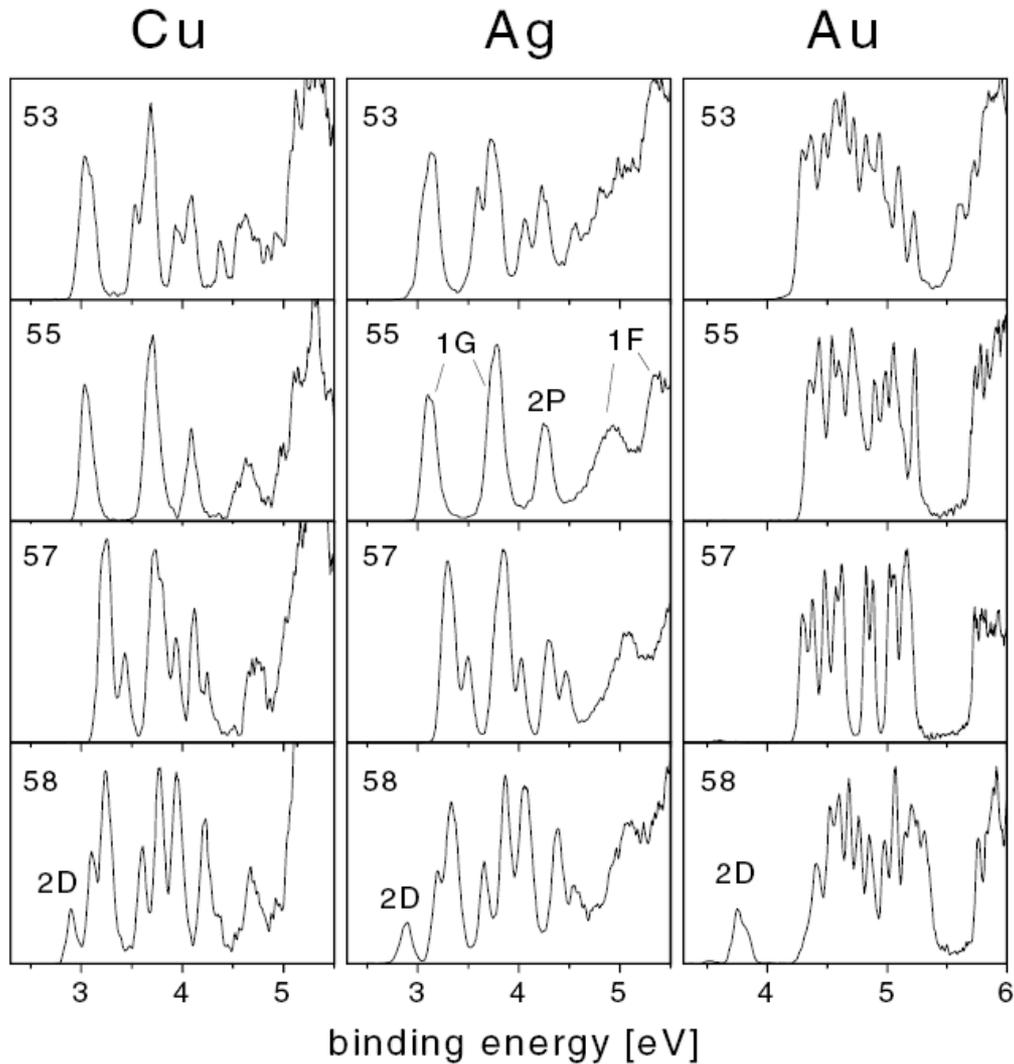


close-lying isomers



here: all three isomers contribute to the experimental spectrum

PES on coinage metal clusters



chemically similar systems may have similar PE spectra.
Exception: Gold, due to relativistic effects

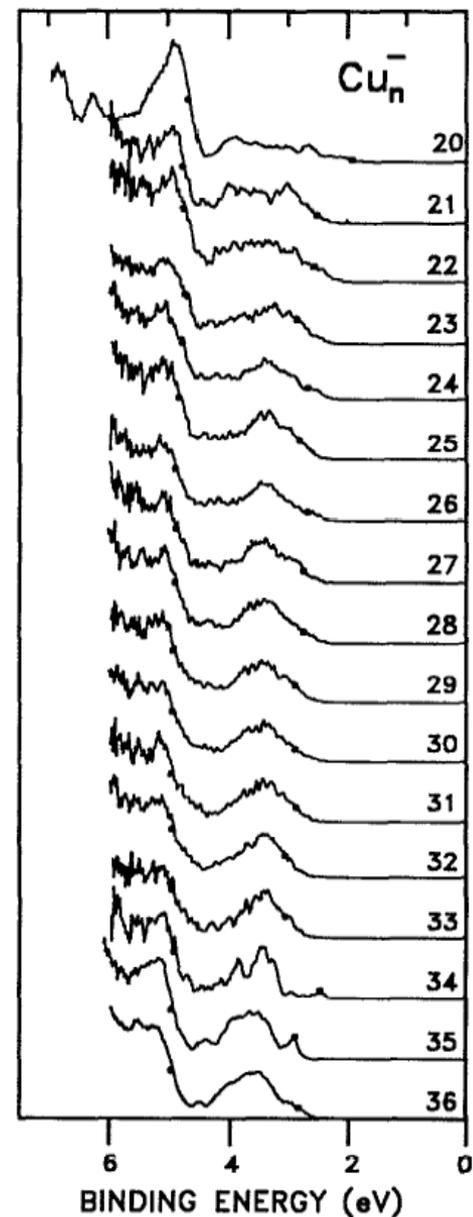
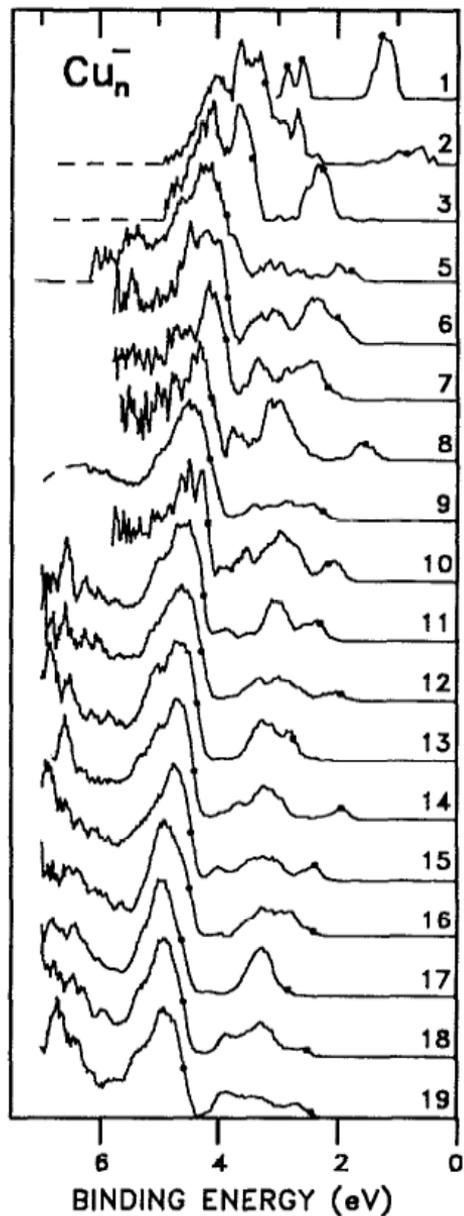
Hannu Hakkinen, Michael Moseler, Oleg Kostko, Nina Morgner, Margarita Astruc Hoffmann, and Bernd v. Issendorff, PRL 93 093401(2004)

FIG. 1. Photoelectron spectra of Cu_n^- , Ag_n^- , and Au_n^- ($n = 53, 55, 57, 58$) obtained at a photon energy of 6.42 eV.

Trends in photoemission threshold energies

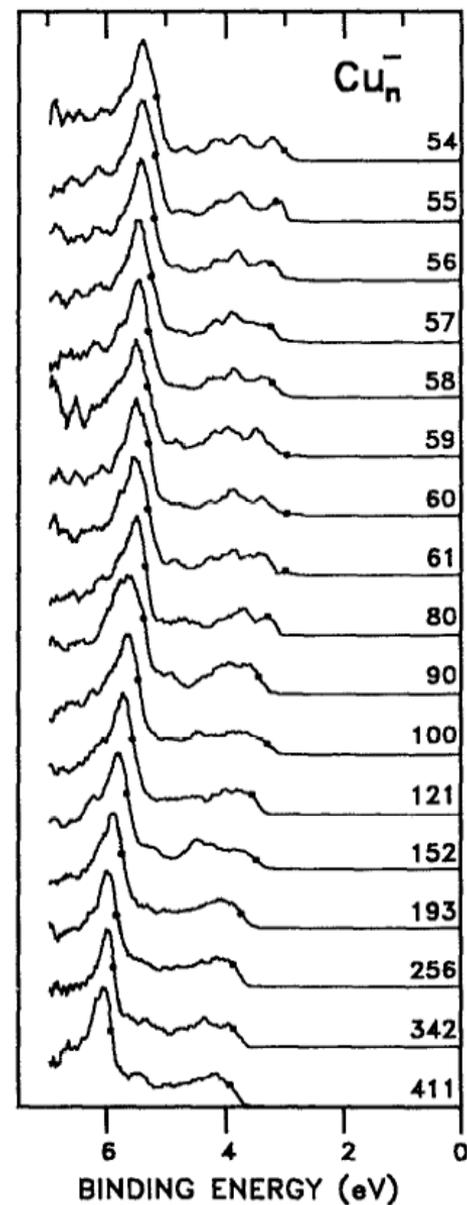
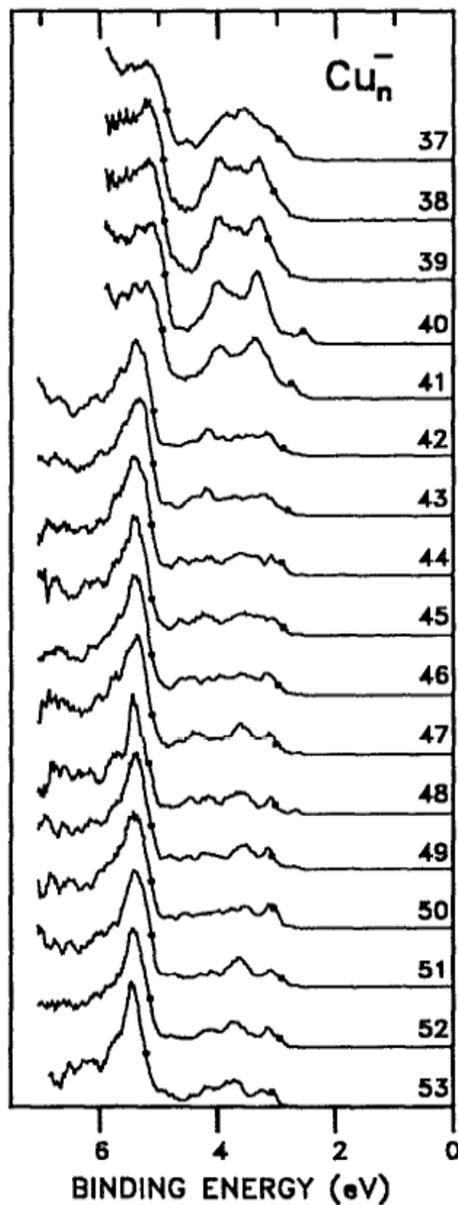
N-dependent trends
in photoemission

Cu_N^- PE threshold
rises with increasing
cluster size

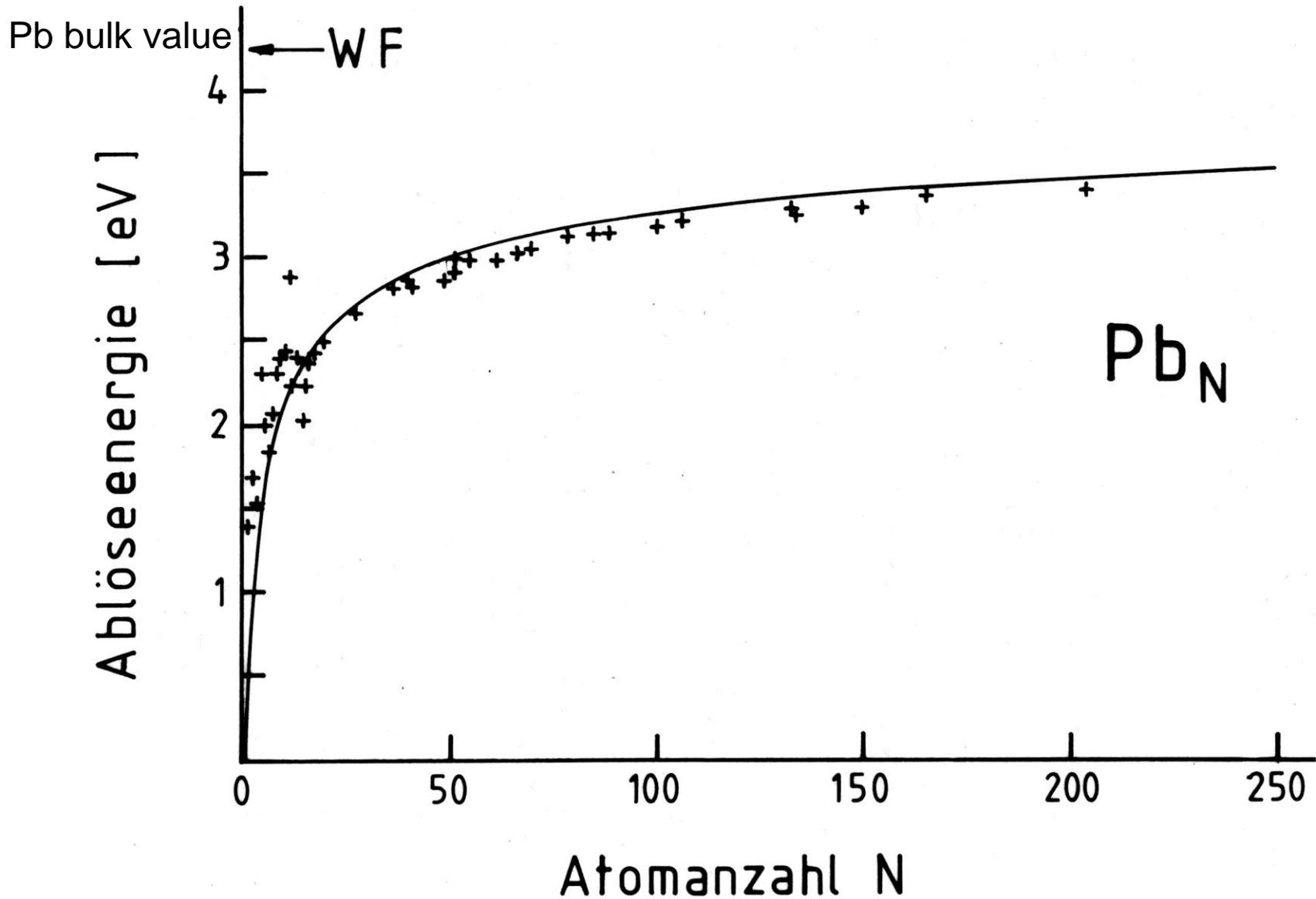


Cu_N^- PES

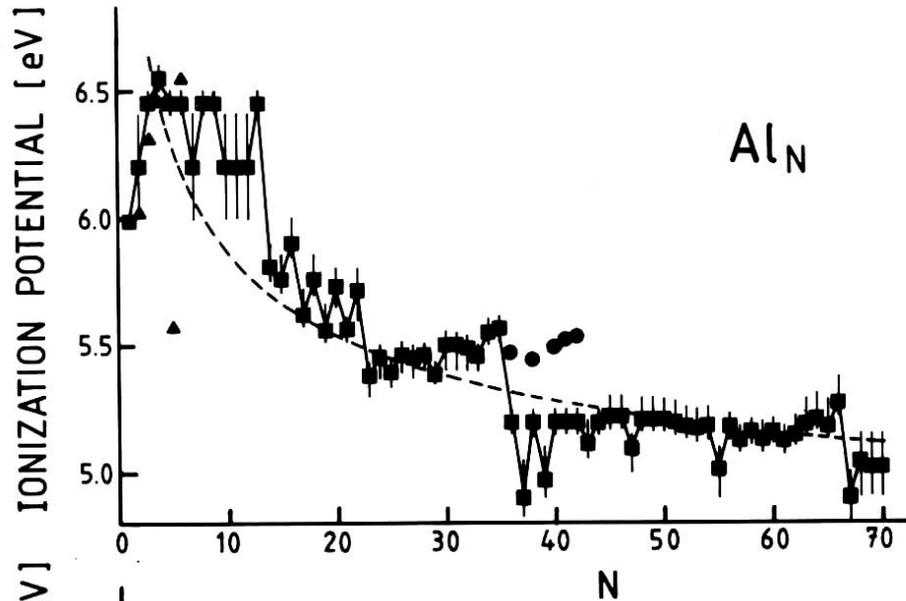
threshold energies
increase with N



threshold energies: electron detachment

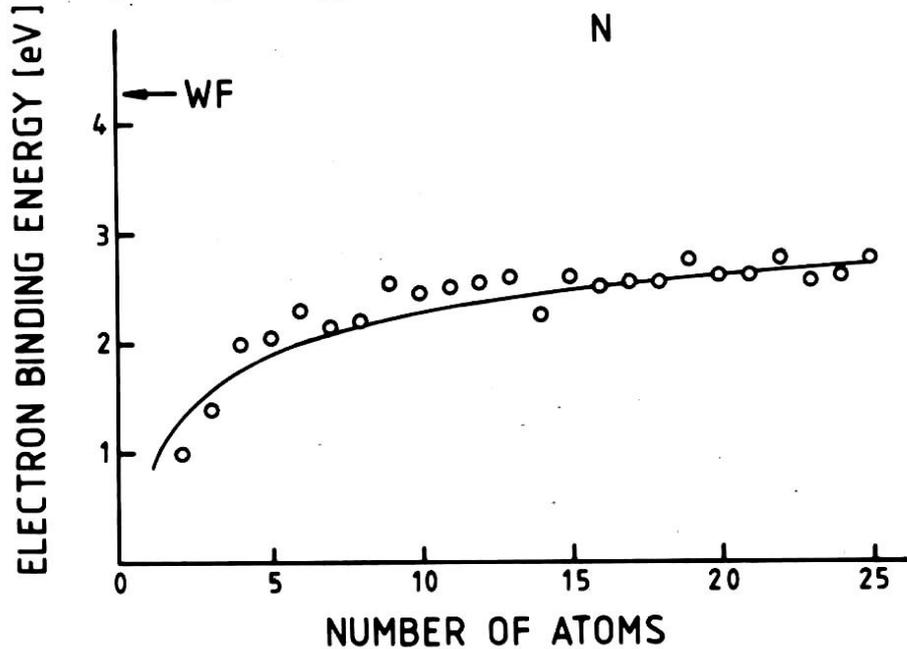


Gausa, Hector, Lüder, Meiwes-Broer



generally:

- IPs decrease with increasing N
- electron detachment en. or EAs rise with increasing N



Ionization potentials (top, by R. Whetten) and electron affinities (bottom, Meiwes-Broer group) of Aluminium clusters

generally:

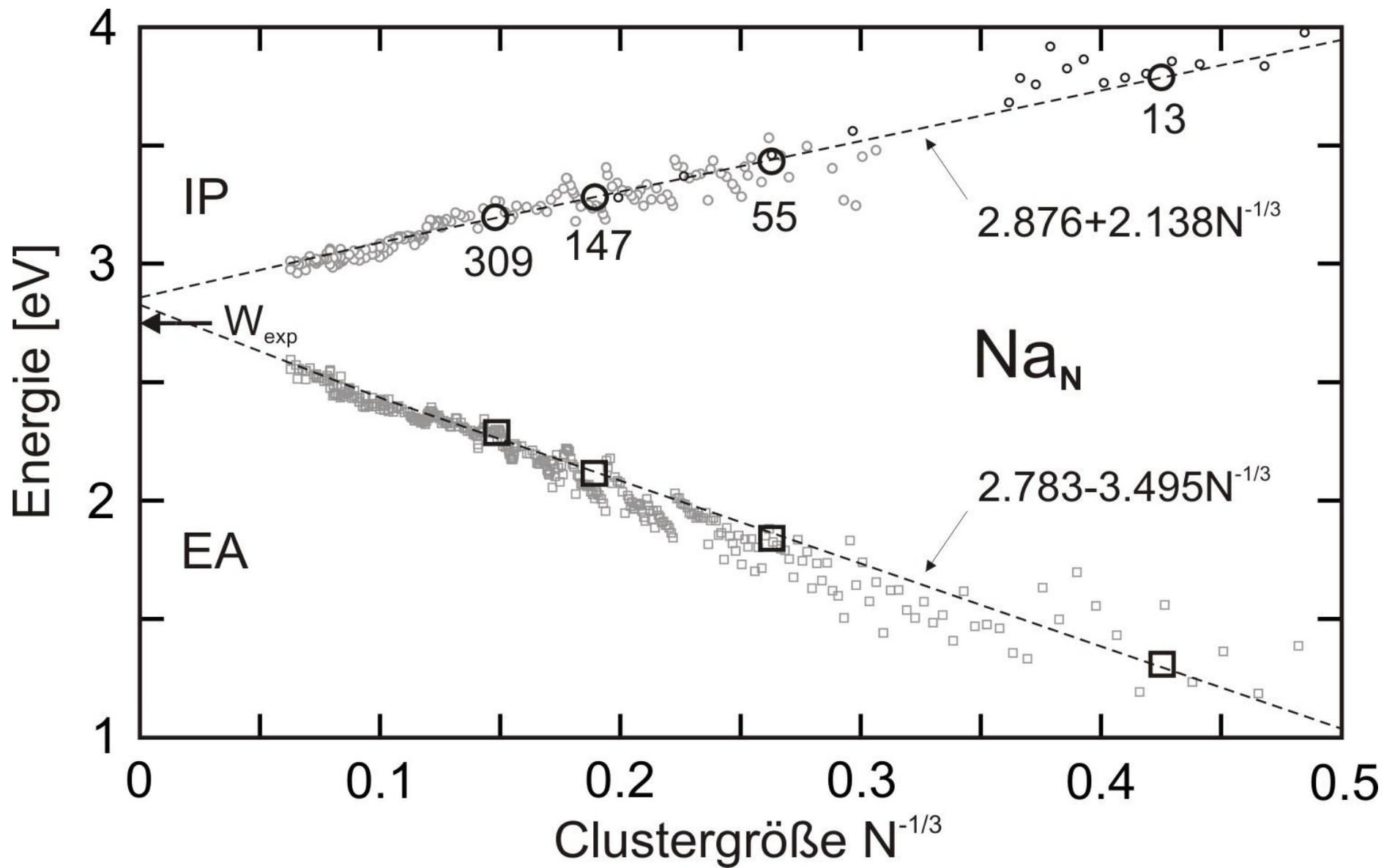
- the IPs decrease with increasing N
- the EAs rise with increasing N

Parametrization:

$$IP(R) = WF + \alpha \frac{e^2}{R} \quad \text{with } \alpha = 3/8 \dots 1/2$$

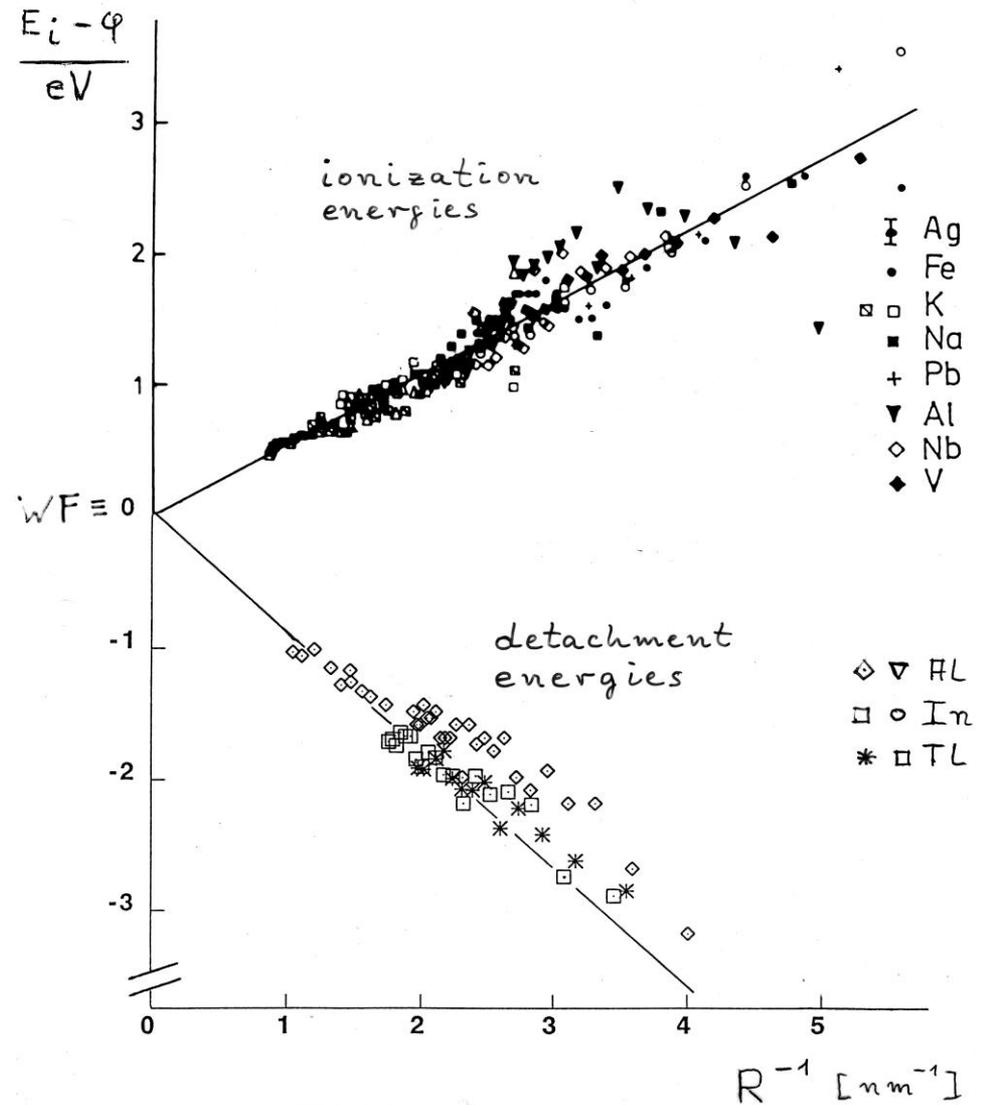
$$EA(R) = WF - \beta \frac{e^2}{R} \quad \text{with } \beta = 1/2 \dots 5/8$$

$\alpha = \beta = 1/2$ corresponds to the charging energy of a jellium sphere, deviations arise from QM exchange and correlation



DFT calculations Fennel et al., Rostock, measurements von Issendorff et al., Freiburg

experimental values for the IP and the EA



let us evaluate IP and EA simultaneously

$$IP(R) = WF + \alpha \frac{e^2}{R} \quad \text{with } \alpha = 3/8 \dots 1/2$$

$$EA(R) = WF - \beta \frac{e^2}{R} \quad \text{with } \beta = 1/2 \dots 5/8$$

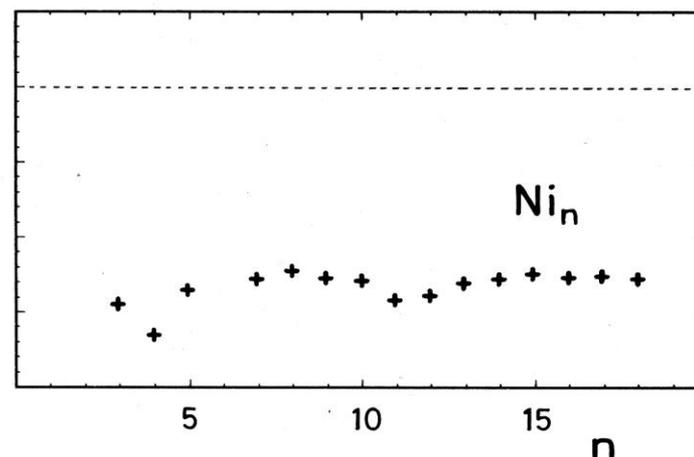
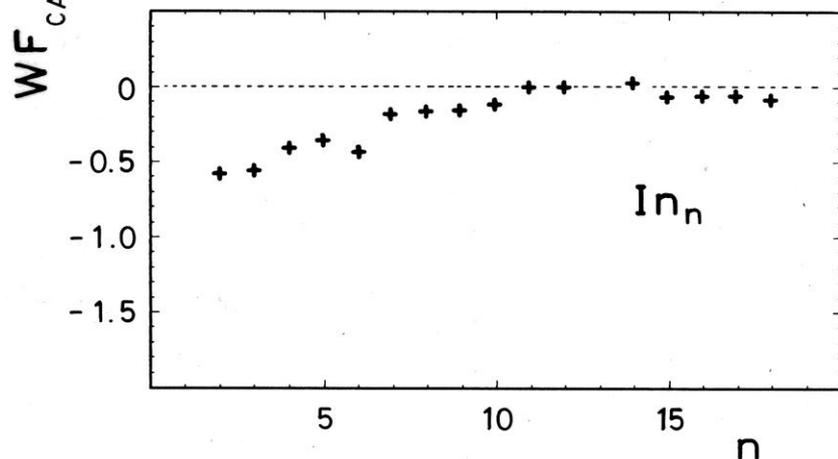
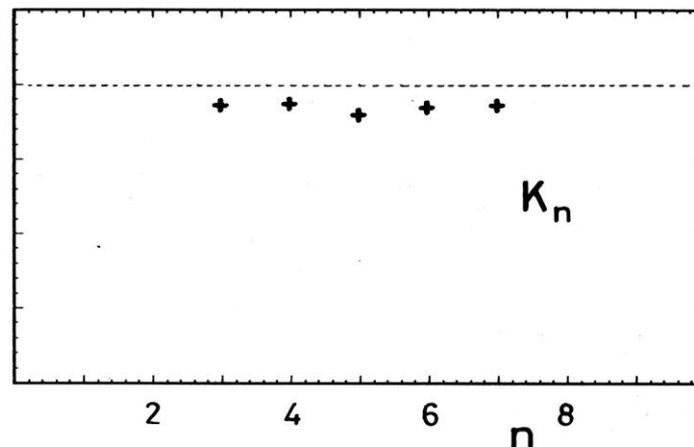
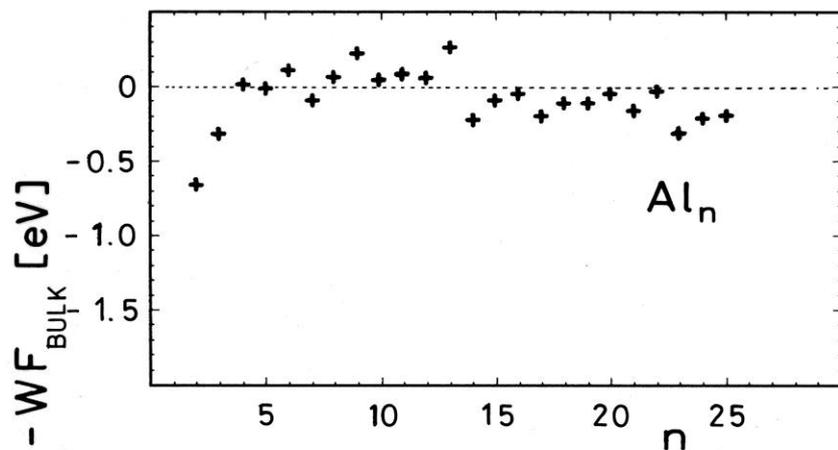
$\alpha - \beta$ is small

solve for WF: $WF_{cal} = \frac{1}{2} (IP + EA) + \frac{1}{2} \frac{e^2}{R} (b - a)$

$$WF_{cal} \approx \frac{1}{2} (IP + EA)$$

thus the work function should be the mean value of IP and EA !

differences between measured IP and EA and bulk values



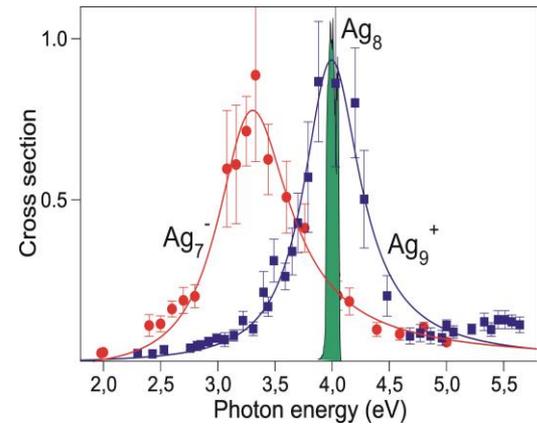
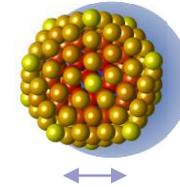
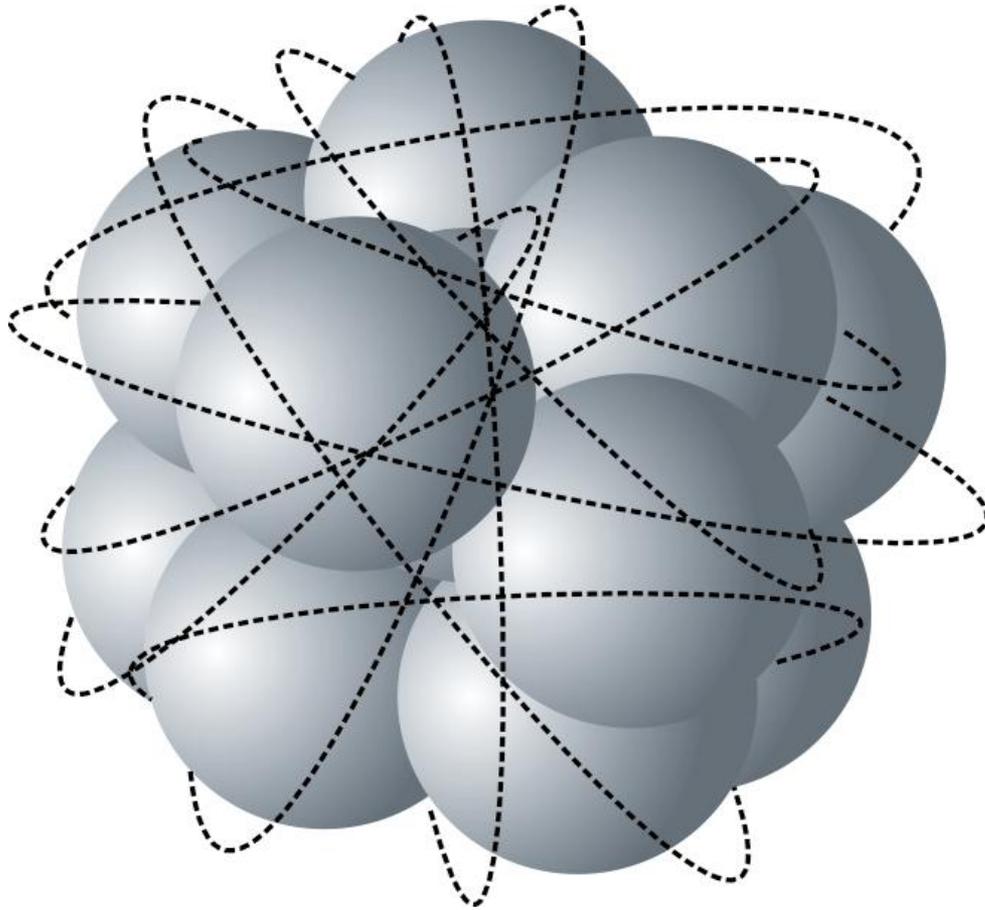
Small or no differences hint at free electron (or: ideal metal droplet) behaviour

Meiwes-Broer in *Advances in Metal and Semiconductor Clusters, Vol. 1*

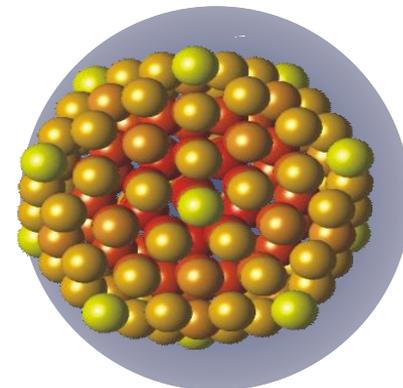
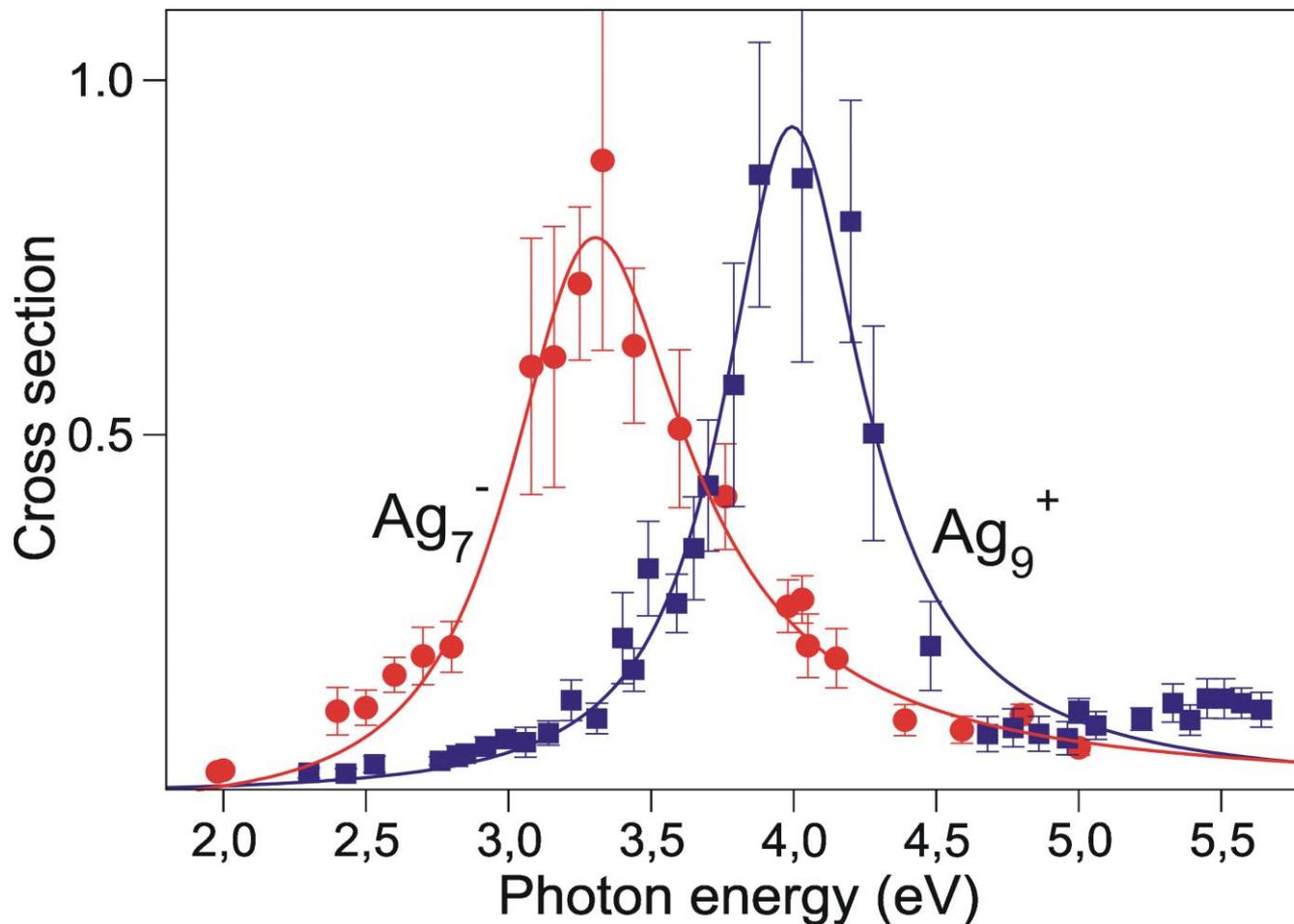
M. Duncan, Ed., JAI Press Inc., 1993

optical properties through confined electrons

... schwingen
gemeinsam im
Laserlicht wie ein
angetriebenes Pendel



photofragment spectroscopy on mass-selected silver clusters



„cold plasmon“

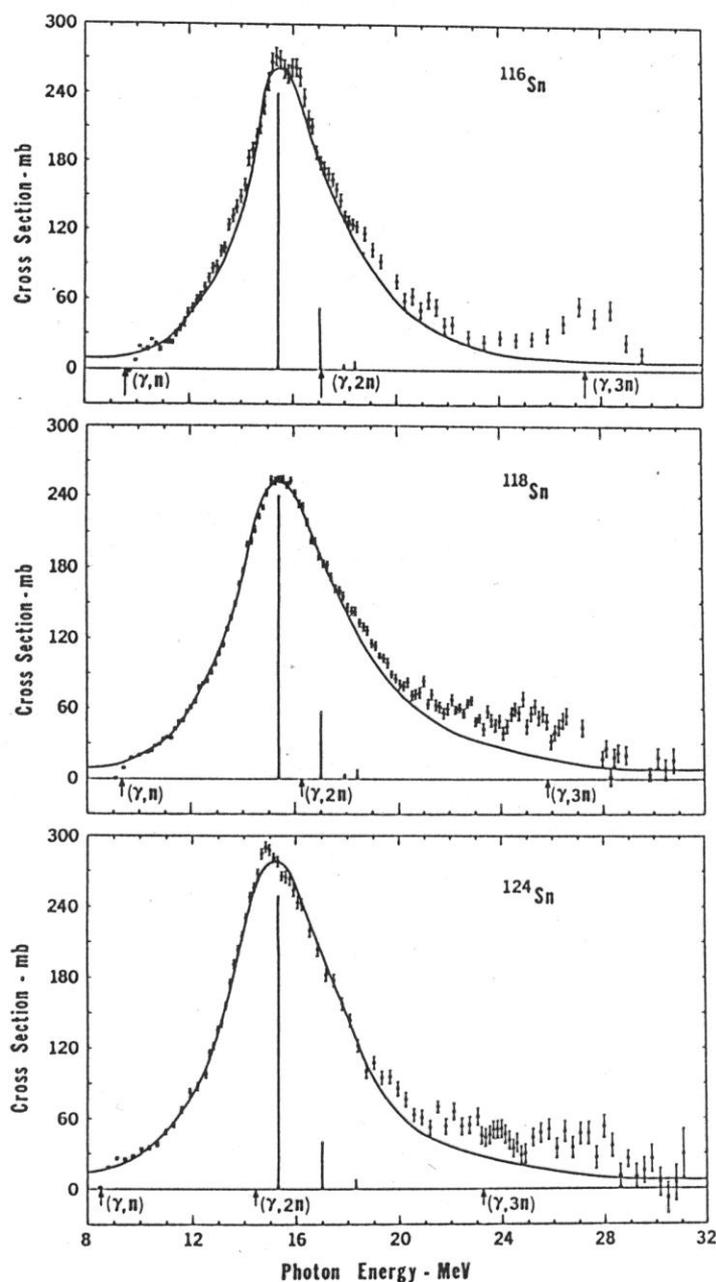
**only in metals with
delocalized electrons**

also see:

Kreibig and Volmer, Springer

**Tiggsebäumker et al., Phys. Rev. A 48, R1749 (1993);
Chem. Phys. Lett. 260, 428 (1996)**

similar: Giant resonances in spherical nuclei



- electrons in metal clusters and the nuclear particles are fermions. Both oscillate in the confining potential

- therefore the same model can be used in order to describe the optical properties, e.g. the random phase approximation (RPA)

- closed-shell nuclei also show only a single absorption

- in the nuclei however the excitation energies are much higher, i.e., in the MeV range

Fig. 1: Showing total photoneutron cross sections for different isotopes of tin, together with theoretical fits based on a dynamical collective model. (After reference 5)

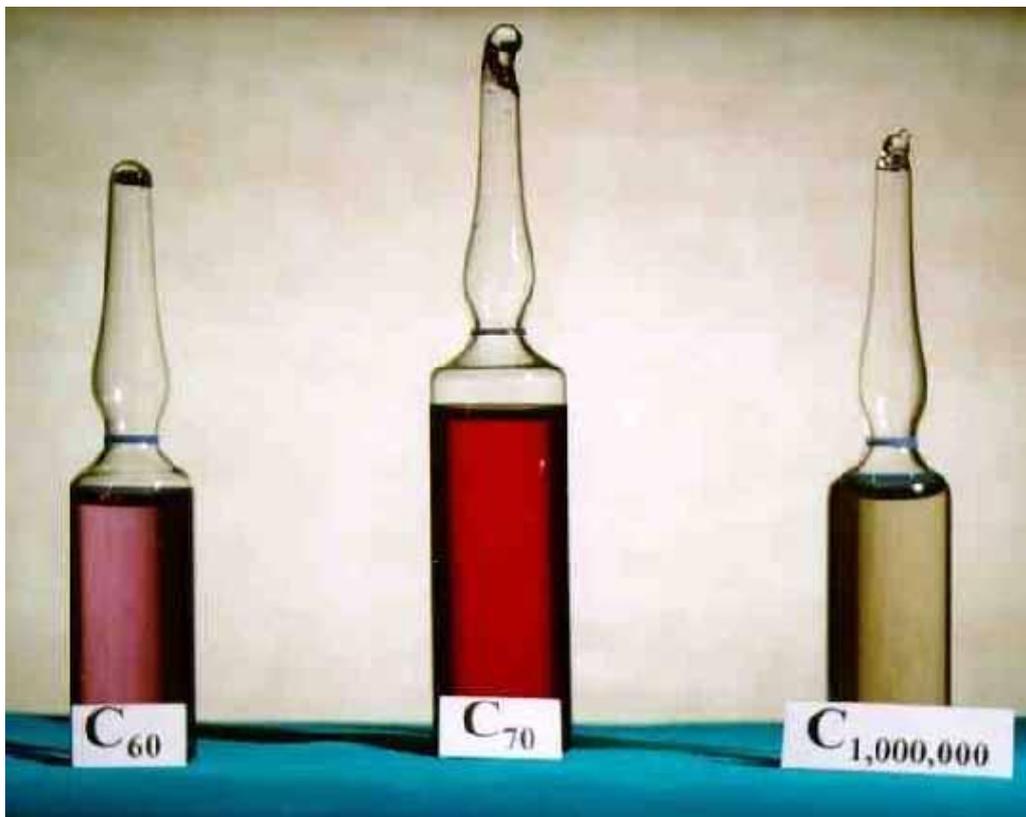
“Labors of the Months” (Norwich, England, ca. 1480).



The ruby color is probably due to embedded gold nanoparticles

Fullerenes and quantum dots

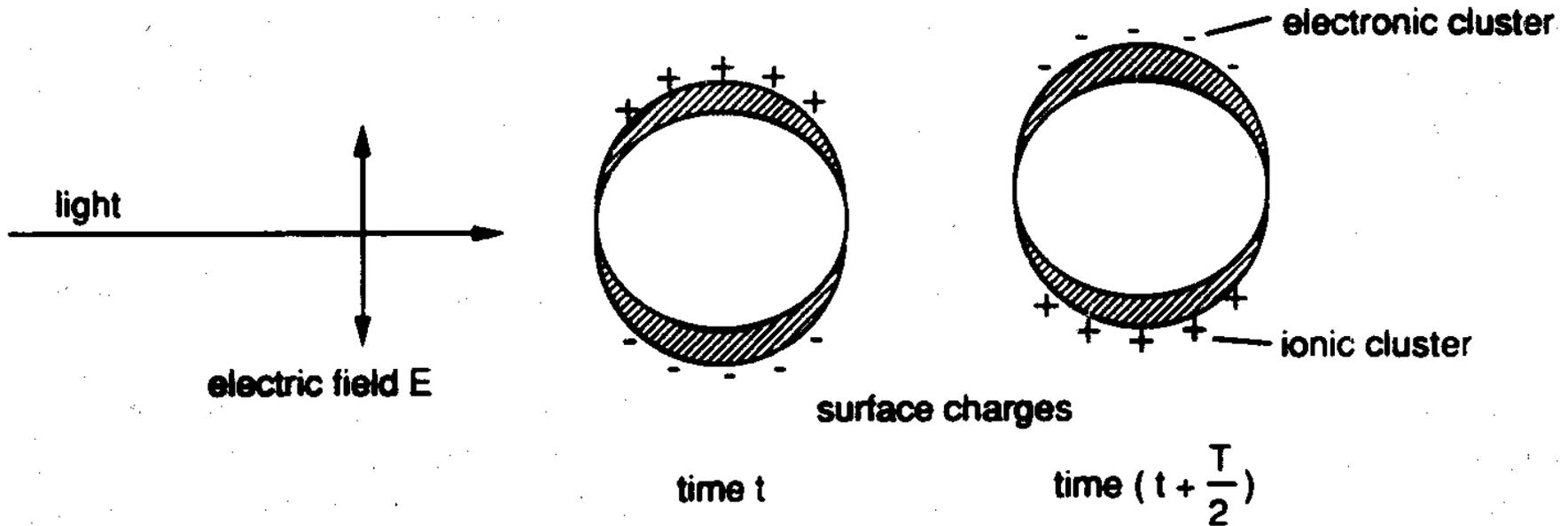
- Such absorption features can also be found in other small particles
- It is therefore not restricted to metal particles but occur also in particles like fullerenes or semiconductor quantum dots
- It turns out that we only need to know the optical properties of the material in order to calculate the optical properties



CdSe

quantum dots

excitation of the electron cloud in a small particle



- Since the ion cores are much heavier than the electrons the positive charges stay more or less at their position when a light field interacts with the particle
- The electric field of the light moves the electron cloud out of the positive background
- Below the resonance the electrons move with the direction of the electric field
- At resonance the movement of the cloud has a $\pi/2$ phase difference to the electric field.
- This is called the plasmon resonance
- Above resonance the phase is 180 degrees



Gustav Mie 1868-1957
born in Rostock

**Gustav Mie, Beiträge zur
Optik trüber Medien,
speziell kolloidaler
Metallösungen
Ann. Phys. 25, 377 (1908)**

absorption and scattering of light by small particles

**C.F. Bohren and D.R. Huffman
Wiley, NY 1983**

$$\omega_{Mie} = \left(\frac{1}{3} \frac{e^2 n_o}{\epsilon_o m_e} \right)^{1/2}$$

**plasmon frequency of a
small particle**

$$\omega_{Mie} = \left(\frac{e^2 N_e}{\alpha \cdot m_e} \right)^{1/2}$$

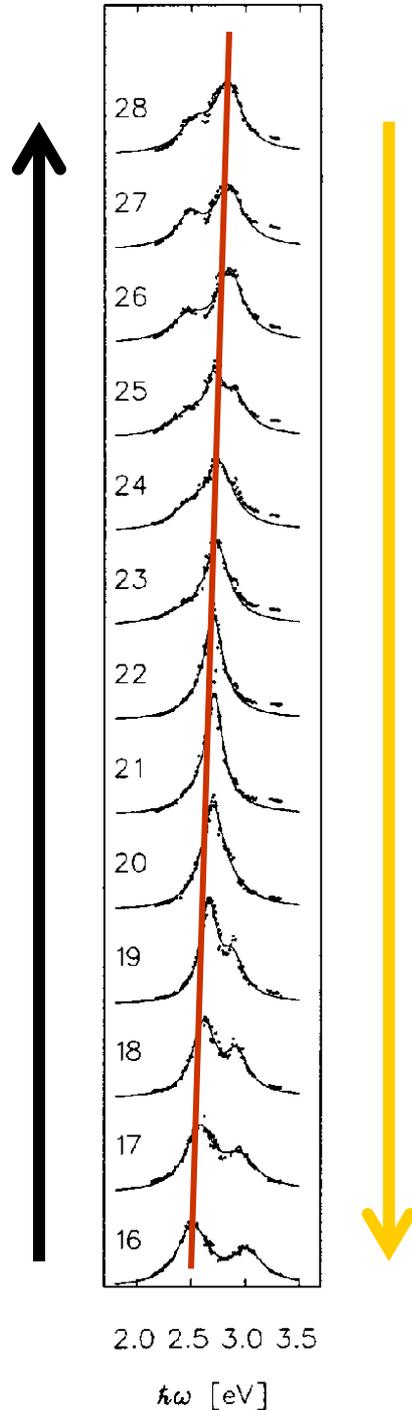


static polarizability

**-Everything gets
simplified when the
size of the particle is
much smaller than the
wavelength of the light**

**- The relevant value is
the size R compared to
the wavelength λ of
the light, i.e. R/λ**

increasing size



Trend with small alkalis

For decreasing cluster size the plasmon energy shifts to lower values. This is called the red-shift.

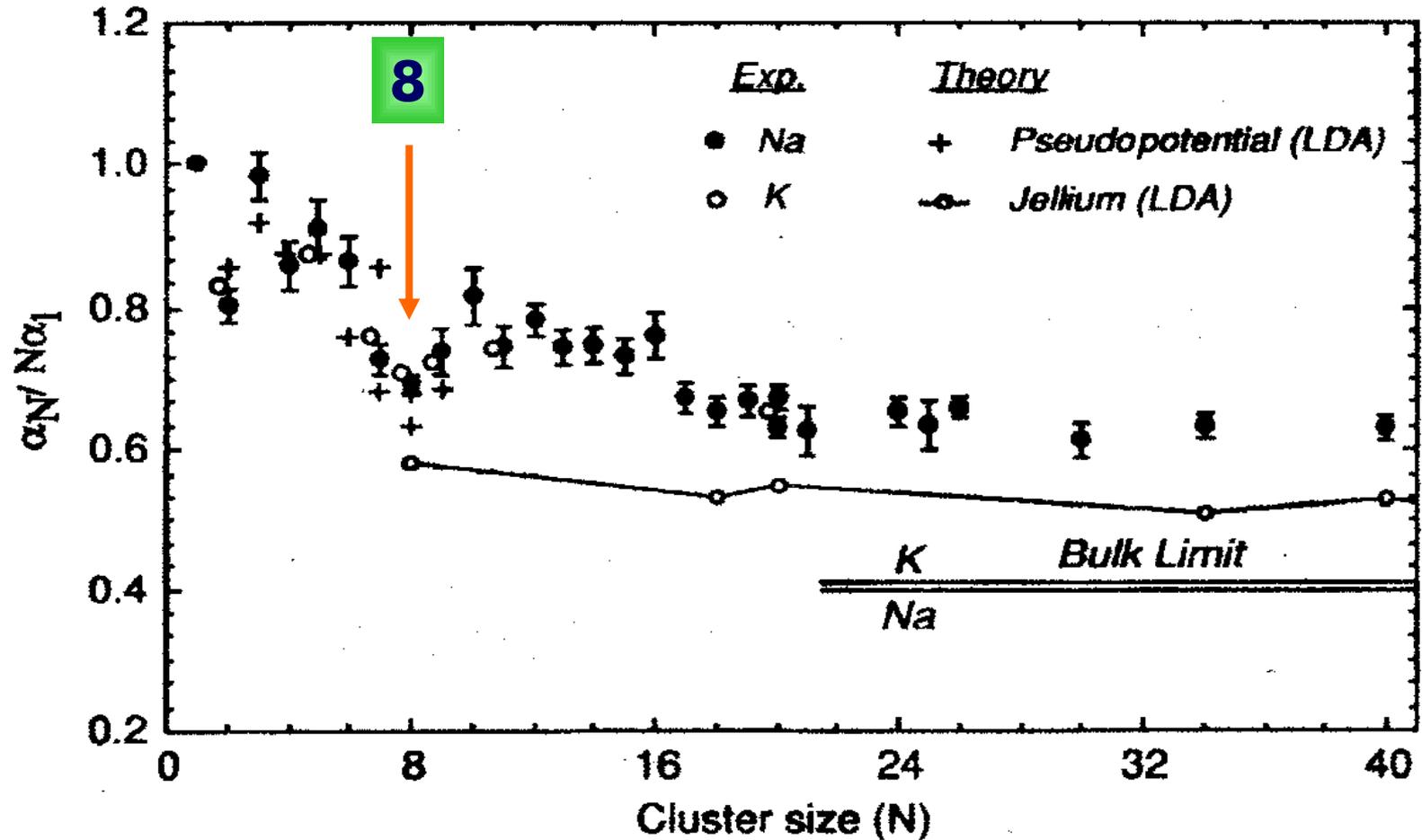
Reason: influence of the spill-out

$$\omega_{Mie} = \sqrt{\frac{n_{bg} e^2}{3m\epsilon_0}} = \frac{\omega_p}{\sqrt{3}}$$

Mie – Plasmon

or: increasing polarizability

polarizabilities of alkali clusters



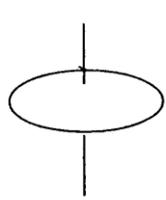
not all clusters are spherical

ellipsoidal shell model

Problems with the spherical jellium model :

- fine structure of mass spectra (even-odd alternation)
- diamagnetism of even-electron clusters with formally open jellium shells (breaking of Hund's rule)

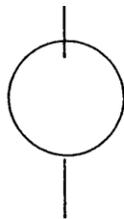
Unlike an atom, the positively charged background can deform !



oblate

$$I_x = I_y < I_z$$

$$k_x = k_y < k_z$$



spherical

$$I_x = I_y = I_z$$

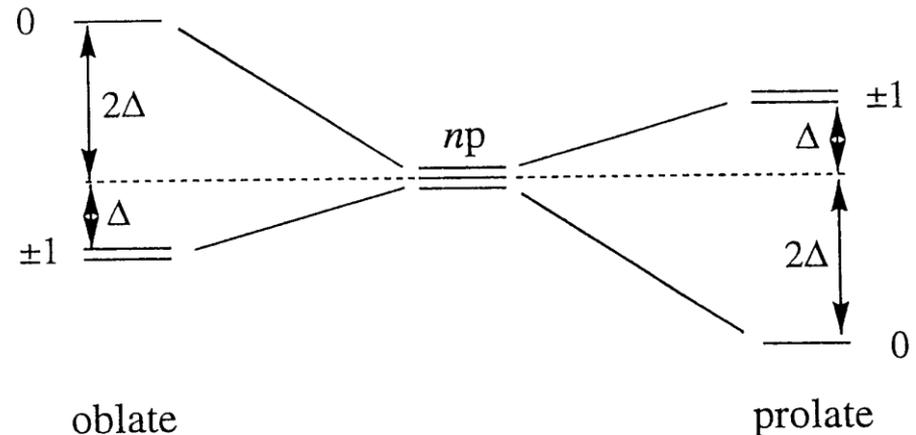
$$k_x = k_y = k_z$$



prolate

$$I_x = I_y > I_z$$

$$k_x = k_y > k_z$$



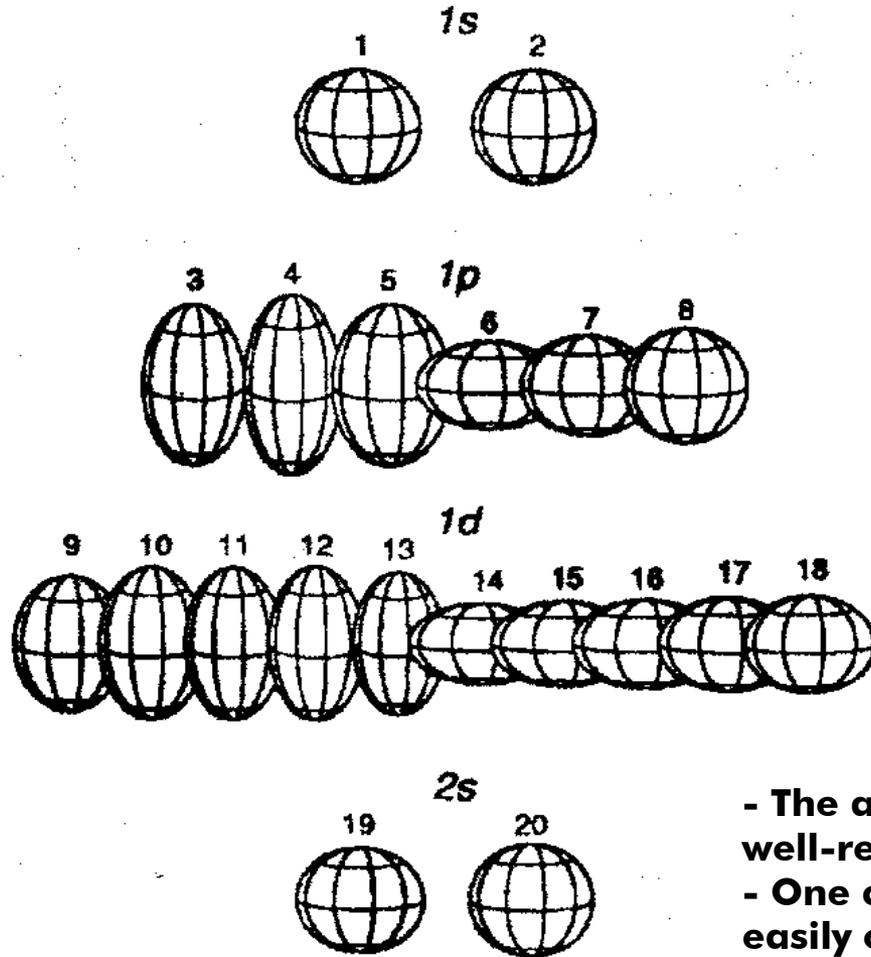
oblate

prolate

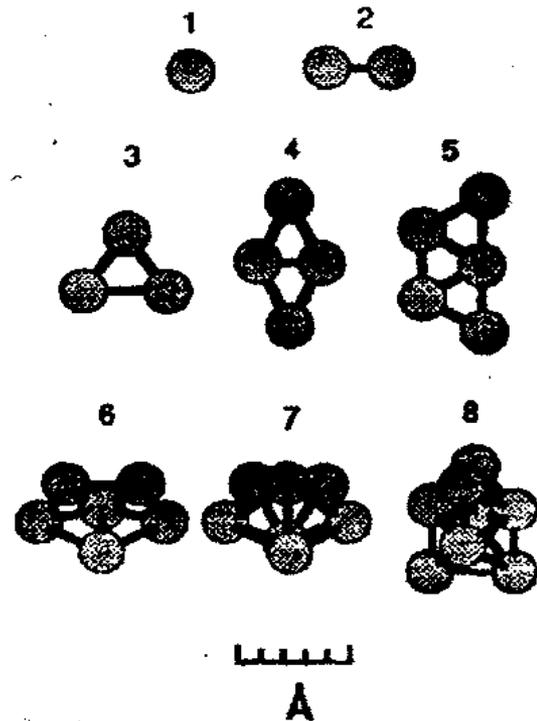
Nielsson model

not all clusters are spherical

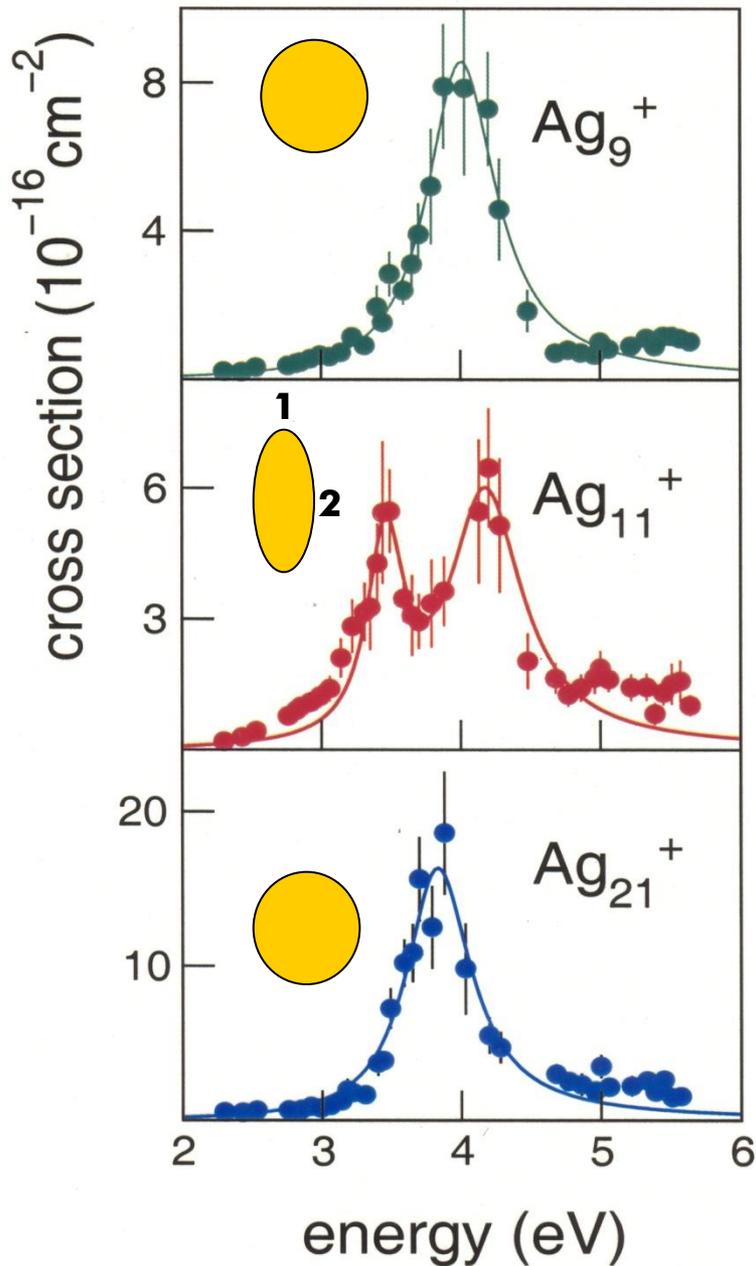
Ellipsoidal shell model



Quantum chemical calculations



- The ab-initio cluster structures are in first order well-reproduced by the ellipsoidal shell model.
- One can calculate the plasmon profiles more easily on the basis of this model.

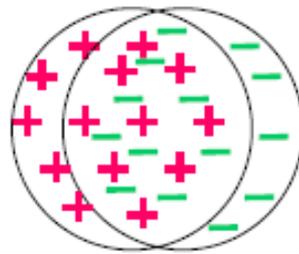
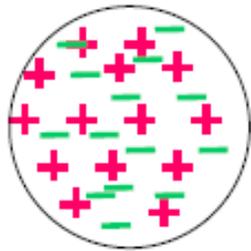


Tiggesbäumker et al.

role of deformation

- In cluster ions the number of electrons is $N-1$
- Closed-shell cluster therefore appear at M_{N+1}^+
- Ag_9^+ and Ag_{21}^+ are closed-shell clusters and only a single absorption line appear in the optical spectra.
- In Ag_{11}^+ the prolate deformation of the particle results in a splitting of the absorption into two components.
- According to the ellipsoidal shell model the lower energy peak should have half the oscillator strength.

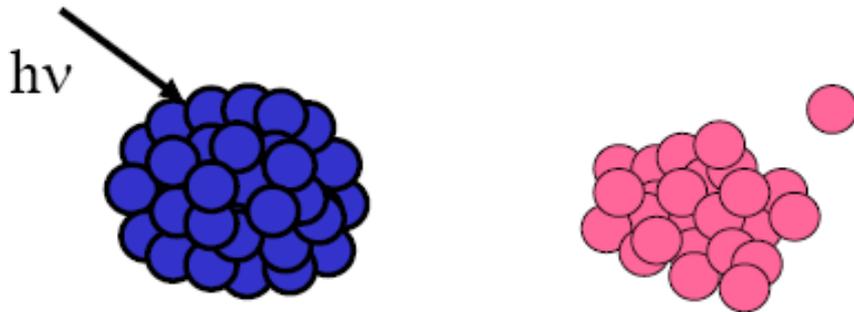
Optical response of mass-selected free metallic clusters



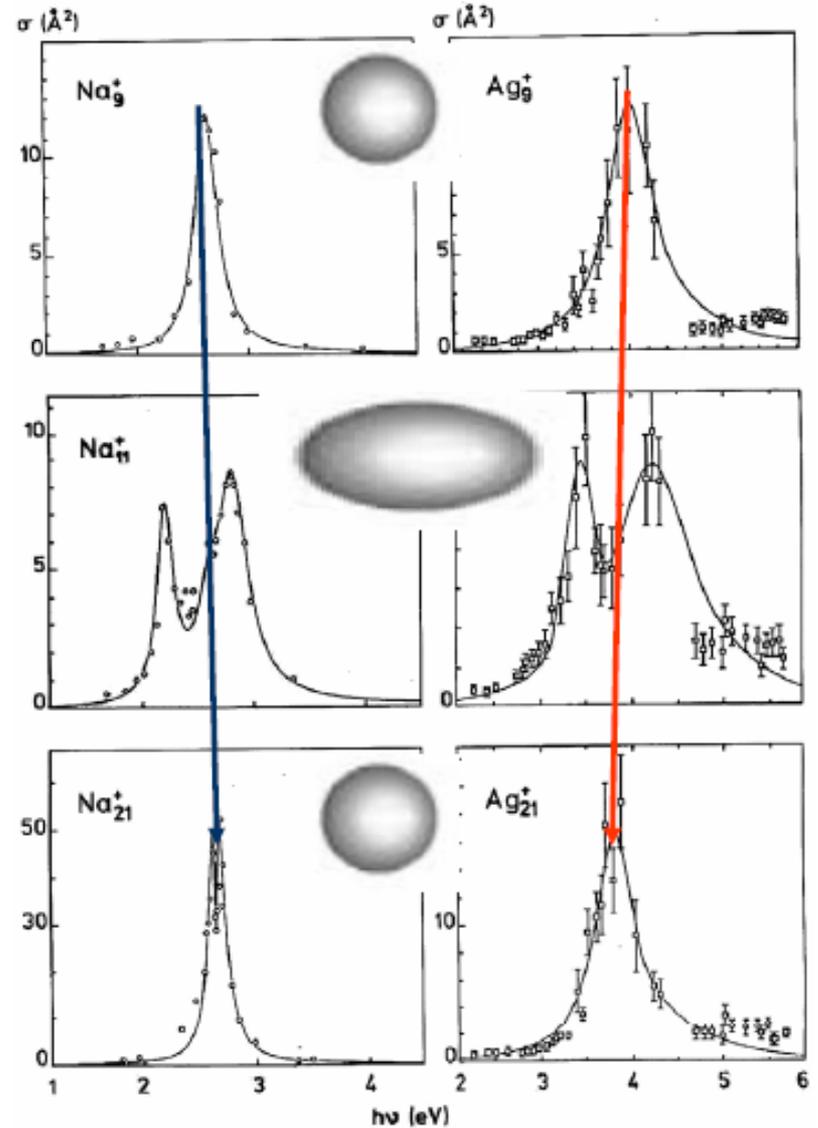
$$\lambda \gg R$$

Mie resonance

Photo-absorption depletion spectroscopy



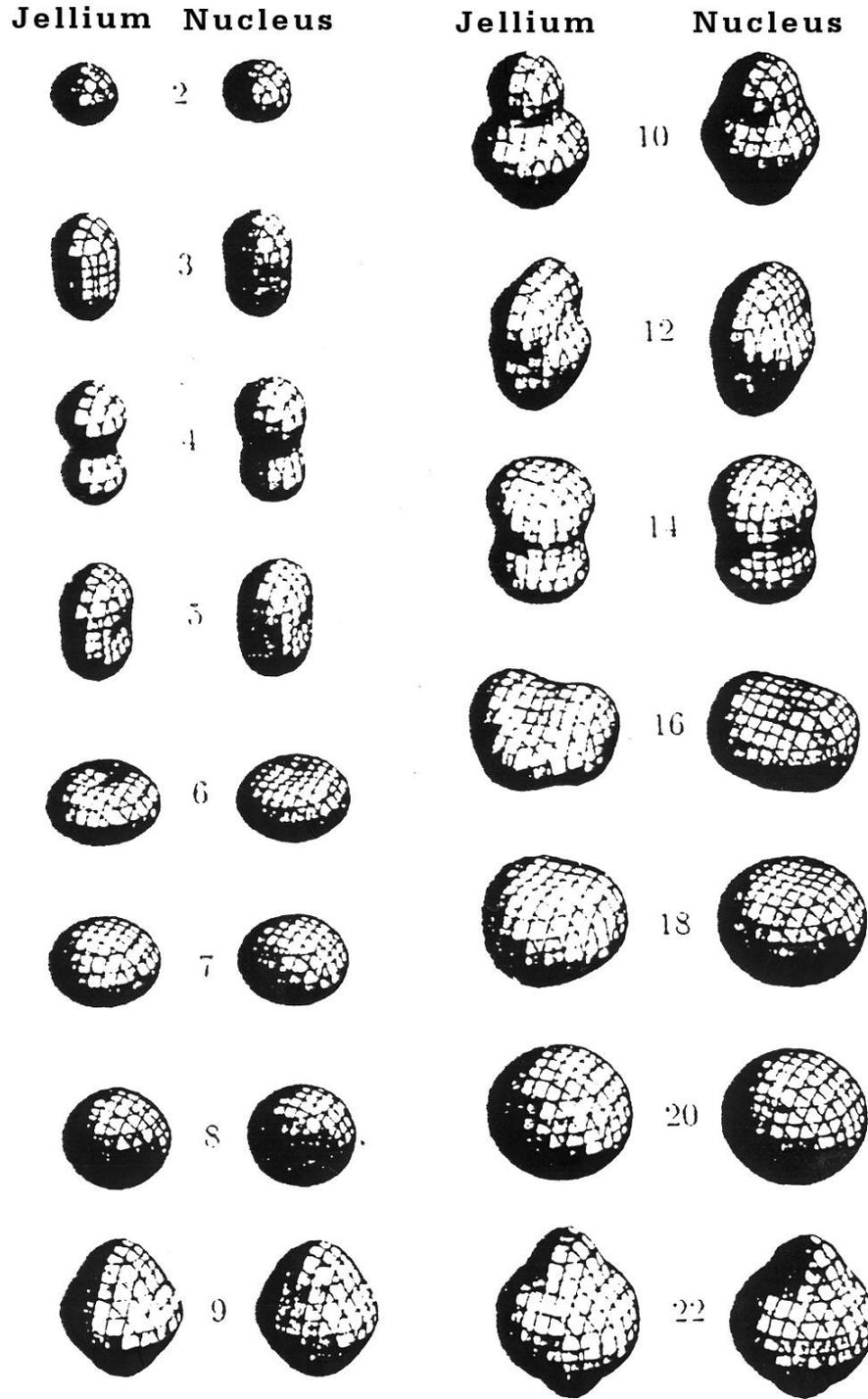
The absorption cross section probes the shape of the particle



Chem. Phys. Lett. **189**, 28 (1992); **190**, 42 (1992)

constant-density surfaces

for electron clusters and nuclei. The density of the surface is 0.00125 atomic units (or scaled units for nuclei), which corresponds to 38% of the bulk density



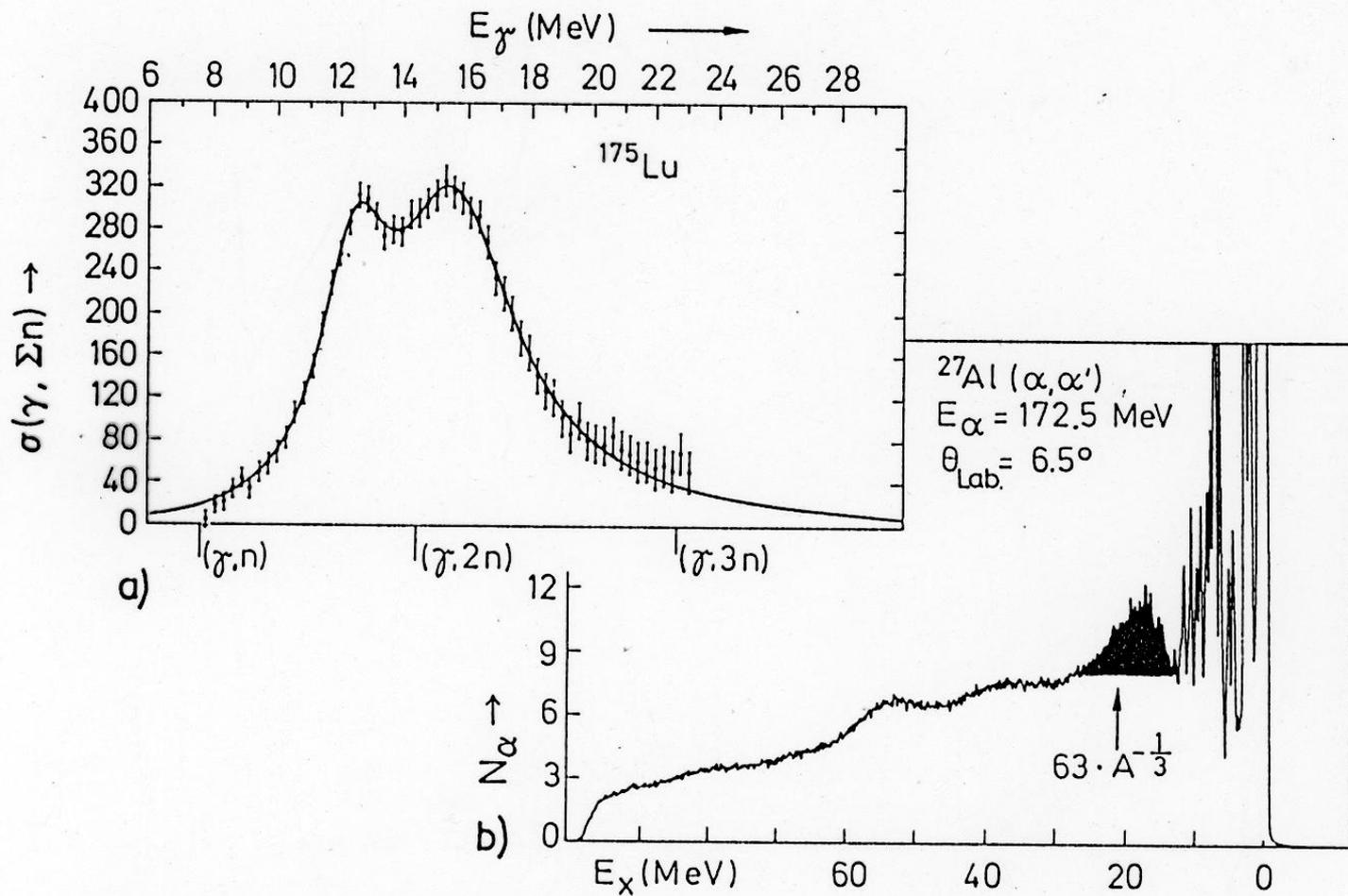
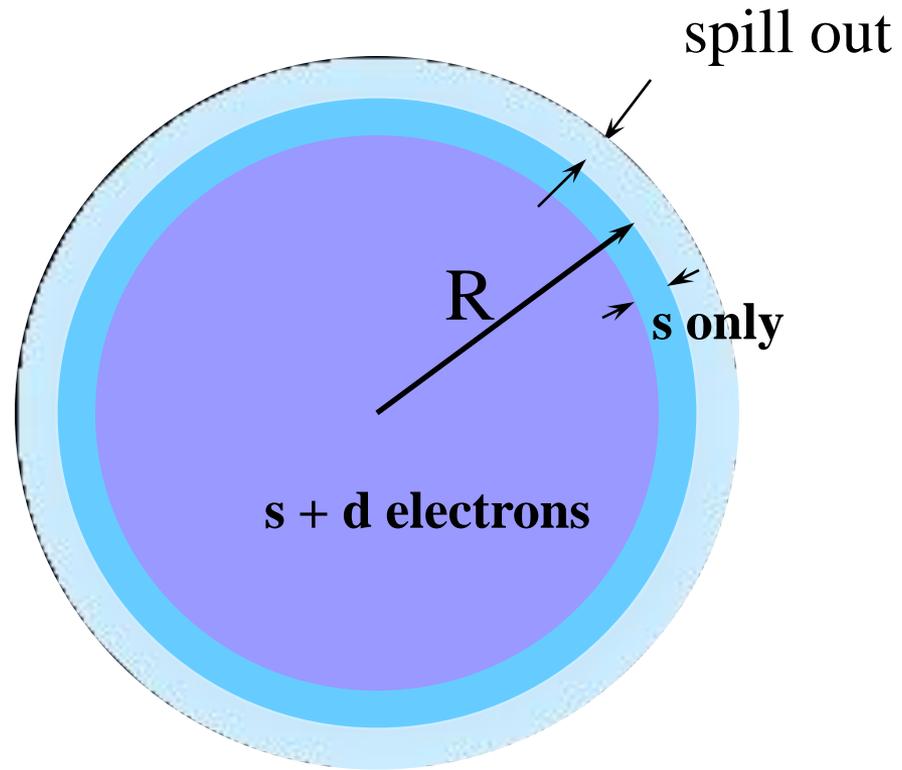
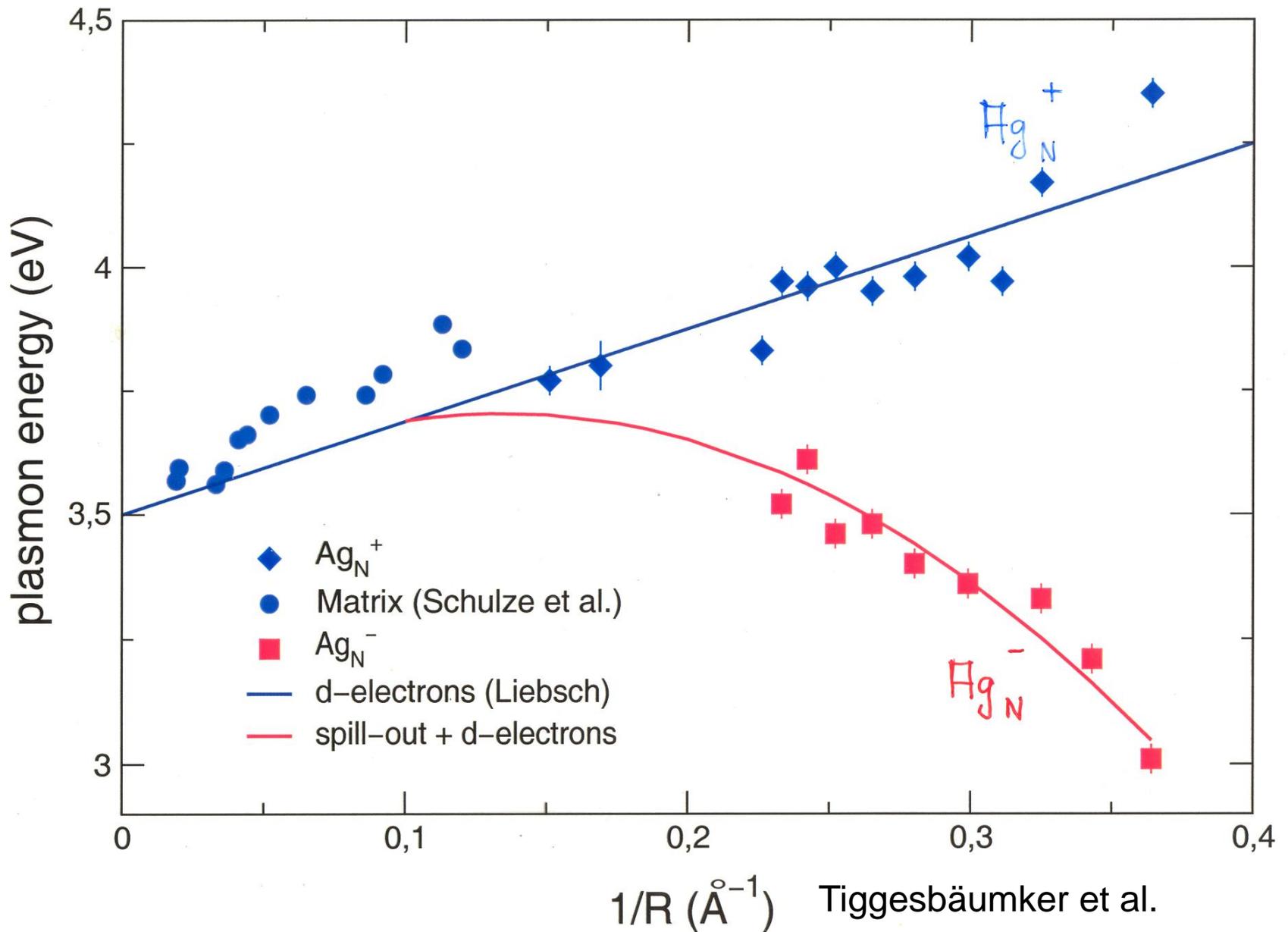


Fig. 99 Beispiele für Riesenresonanzen: a) In der Anregungsfunktion für (γ, n) -Prozesse an ^{175}Lu . Für deformierte Kerne ist der doppelte Höcker charakteristisch, da in der Deformationsachse eine andere Schwingungsfrequenz auftritt als senkrecht dazu [nach Ber 75a]; b) im Spektrum von unelastisch an Aluminium gestreuten α -Teilchen [Kis 76]

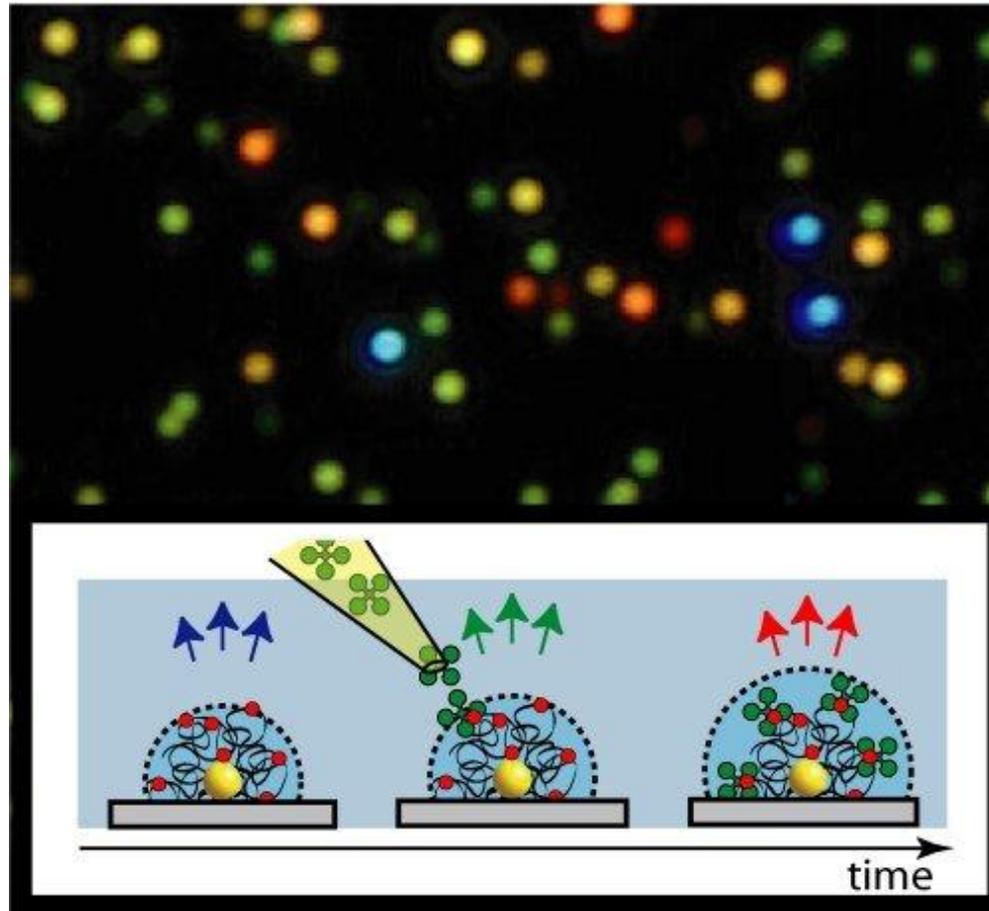
Silver clusters: s- and d-electrons



complex situation in Ag clusters



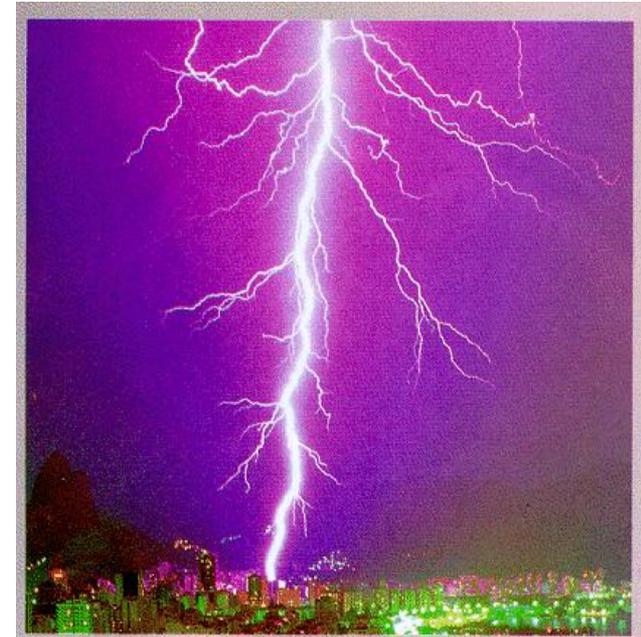
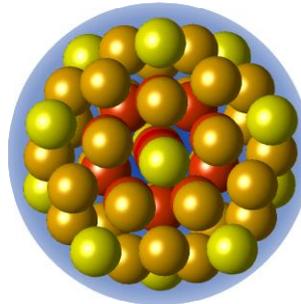
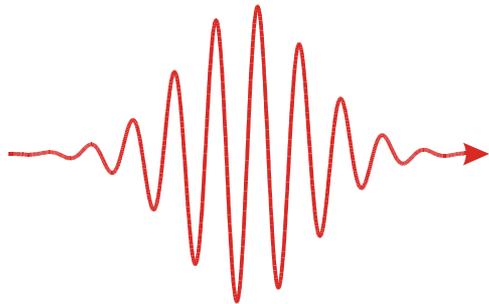
technical application as fluorescent labels



the following slides on clusters in strong laser fields have not been presented in the lecture. This subject is an important topic in the Sonderforschungsbereich SFB 652.

in strong laser pulses: clusters act as strong nano antennas

Gigawatt laser pulse



Pulse length: 100 femto seconds
power densities up to 10.000 Gigawatts per cm²



→ minuatere plasmas

clusters in intense laser fields: nanometer-sized plasmas far from equilibrium

properties of the radiation field

10^{16} W/cm^2 means about 10^{11} V/m

Energy flux at 100 fs pulse length: 624 keV/\AA^2 electrons

Ponderomotive Potential: 0.6 ... 600 eV

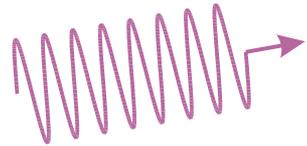
$10^{13-16} \text{ W/cm}^2$

800nm

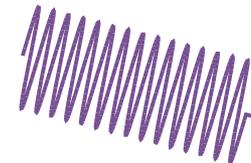
100fs

femtosecond
light pulse

metal
cluster

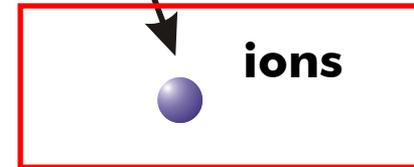


VUV
light



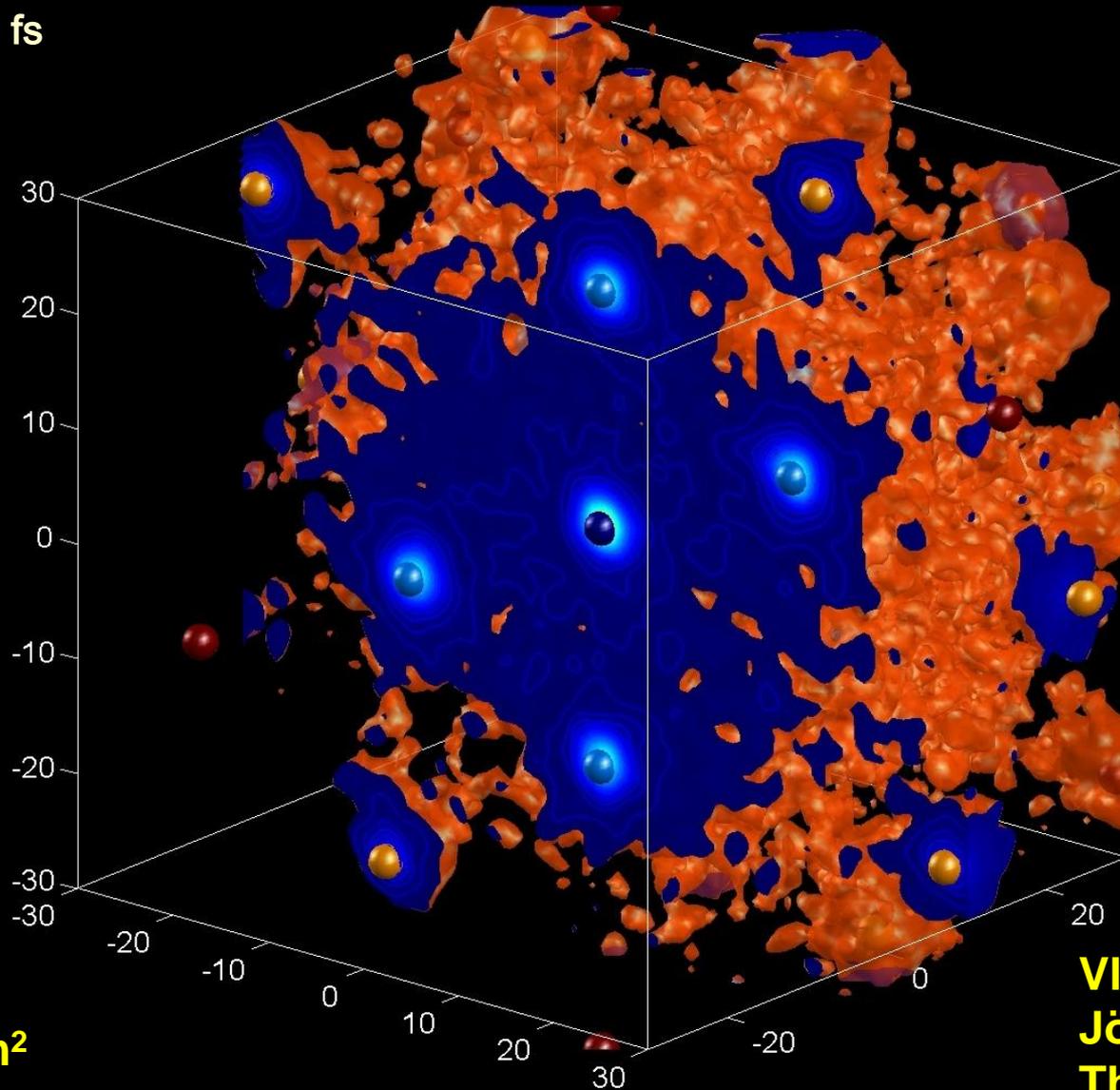
X-rays

ions



simulated Coulomb explosion Na_{55}

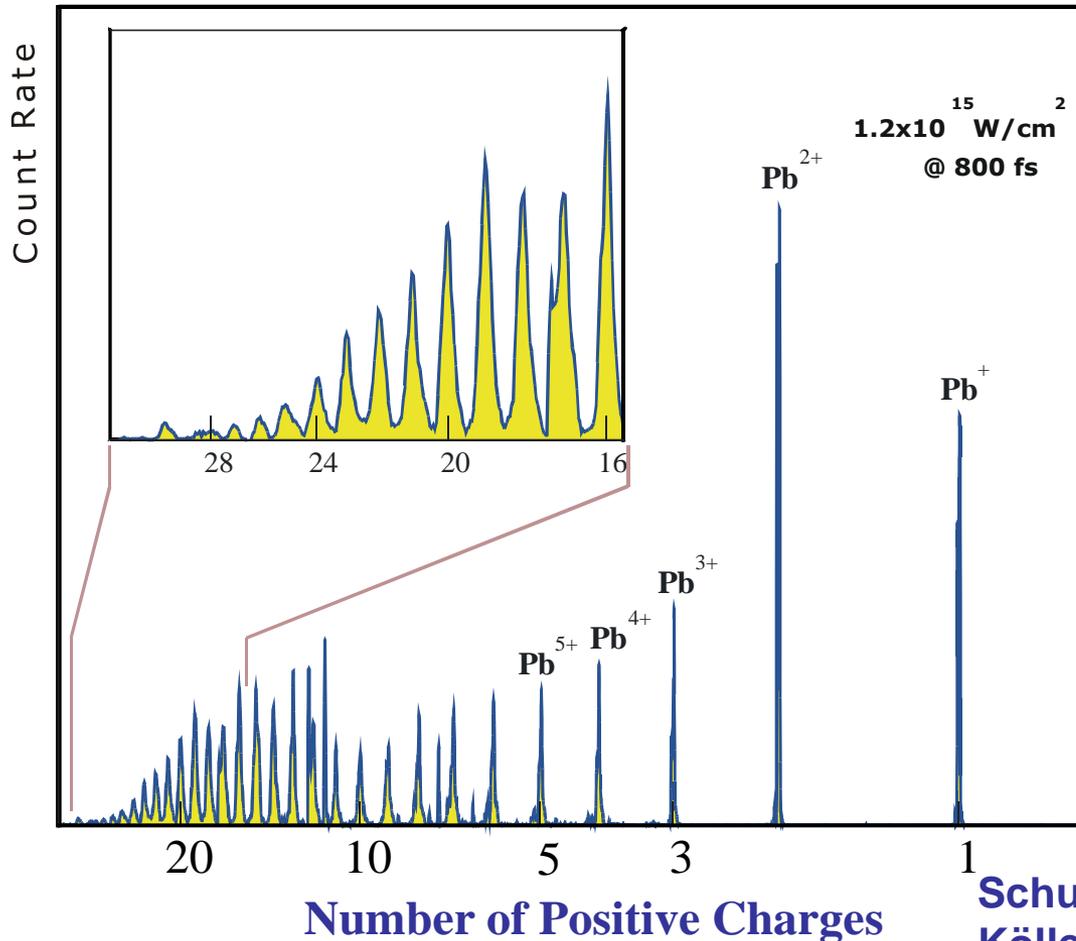
Modellzeit: 350 fs



$E_{\text{Photon}} = 2.7 \text{ eV}$
 $t = 50 \text{ fs}$
 $I = 4 \times 10^{12} \text{ W/cm}^2$

Vlasov-VUU
Jörg Köhn
Thomas Fennel

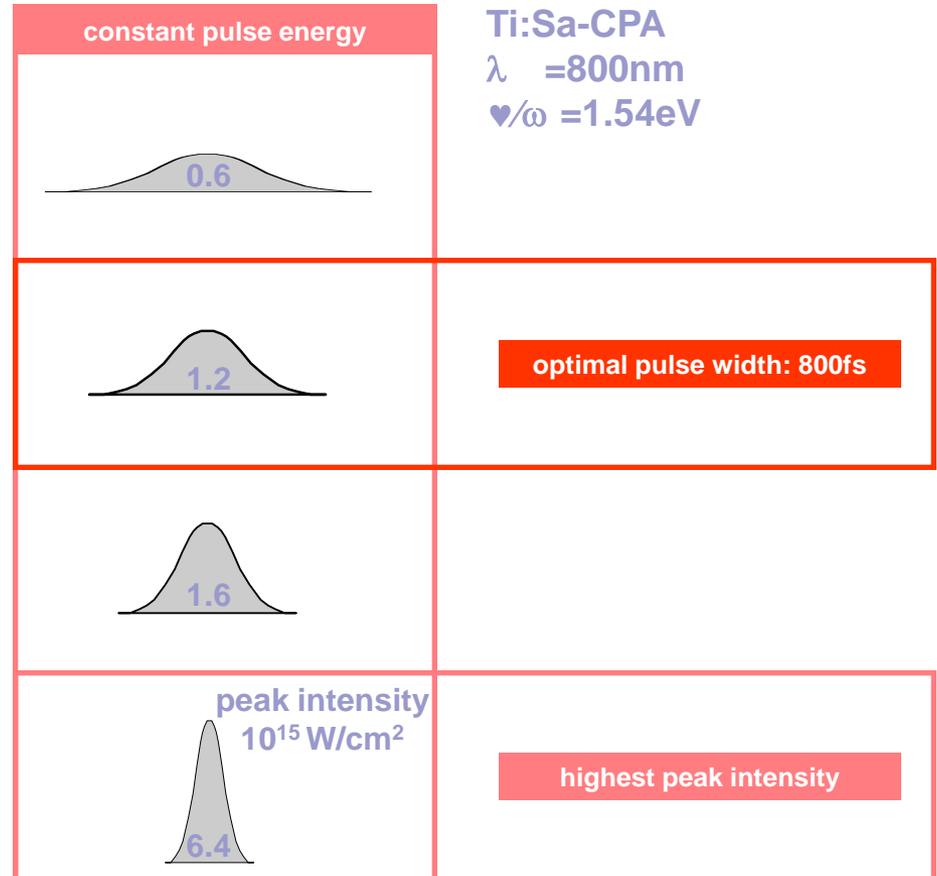
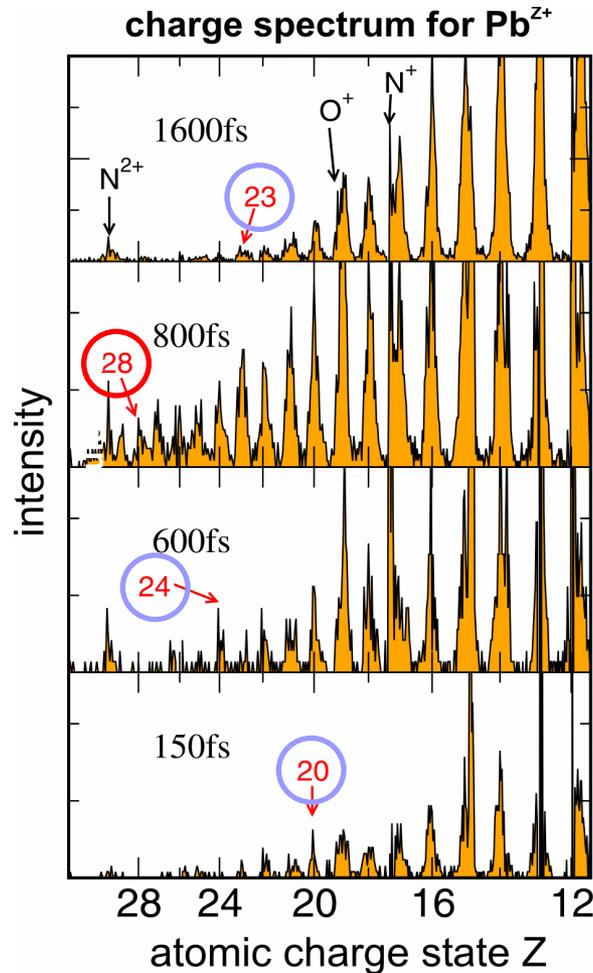
Charge distribution of Pb ions from Coulomb explosion



- Max. charge state $z=30!$
- Highest charging at 800 fs
- Max recoil energy $E_{\text{max}} = 180 \text{ keV}$

Schumacher et al., EPJD 9, 411-414 (1999)
Köller et al., PRL 82, 3783-3786 (1999)

Coulomb explosion Pulse width dependence

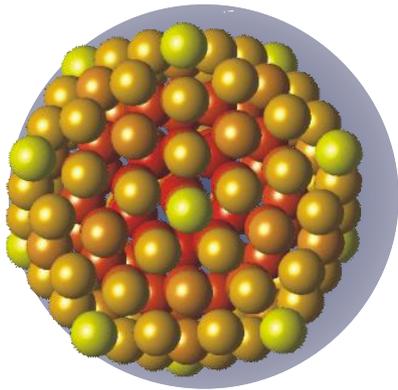


Döppner et al., Appl. Phys. B **71**, 357 (2000)

Köller et al., Phys.Rev. Lett. **82**, 3783 (1999)

mechanism for the high absorption

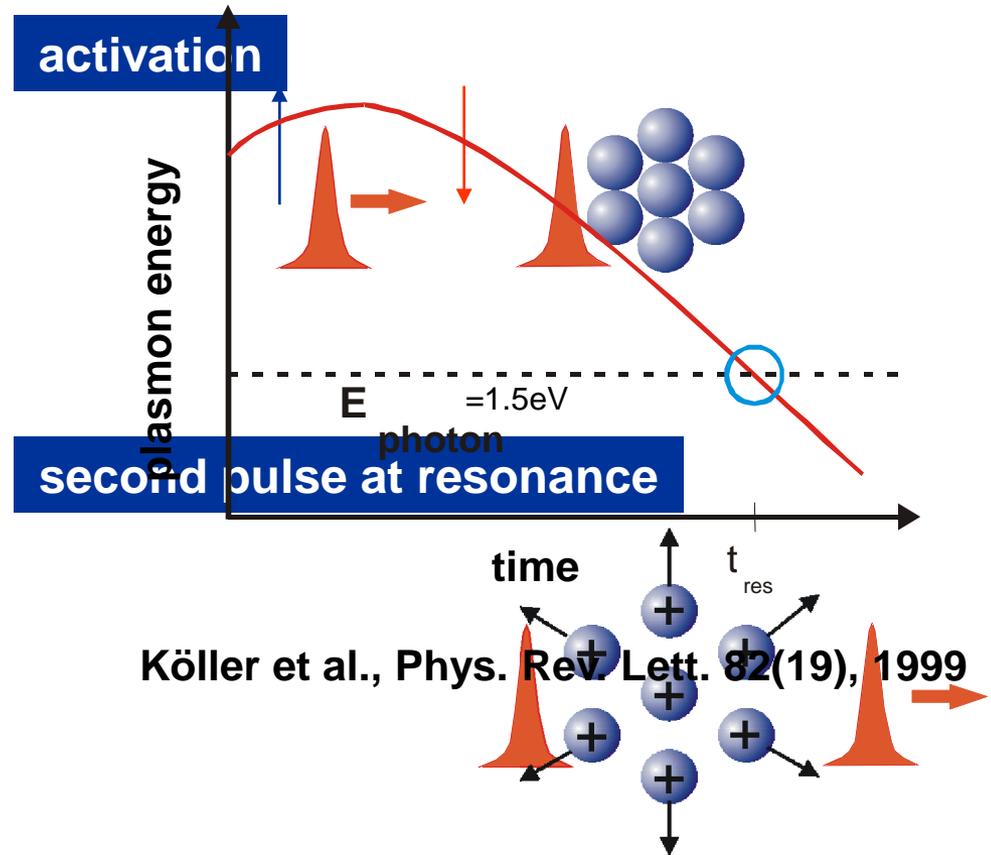
plasmon-enhanced ionization



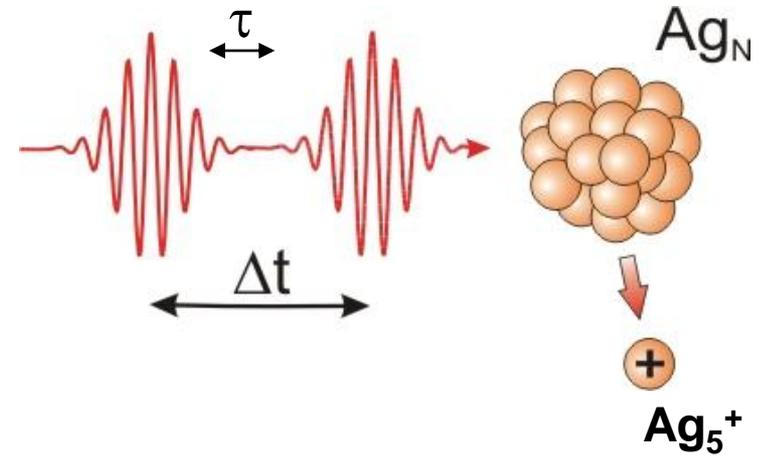
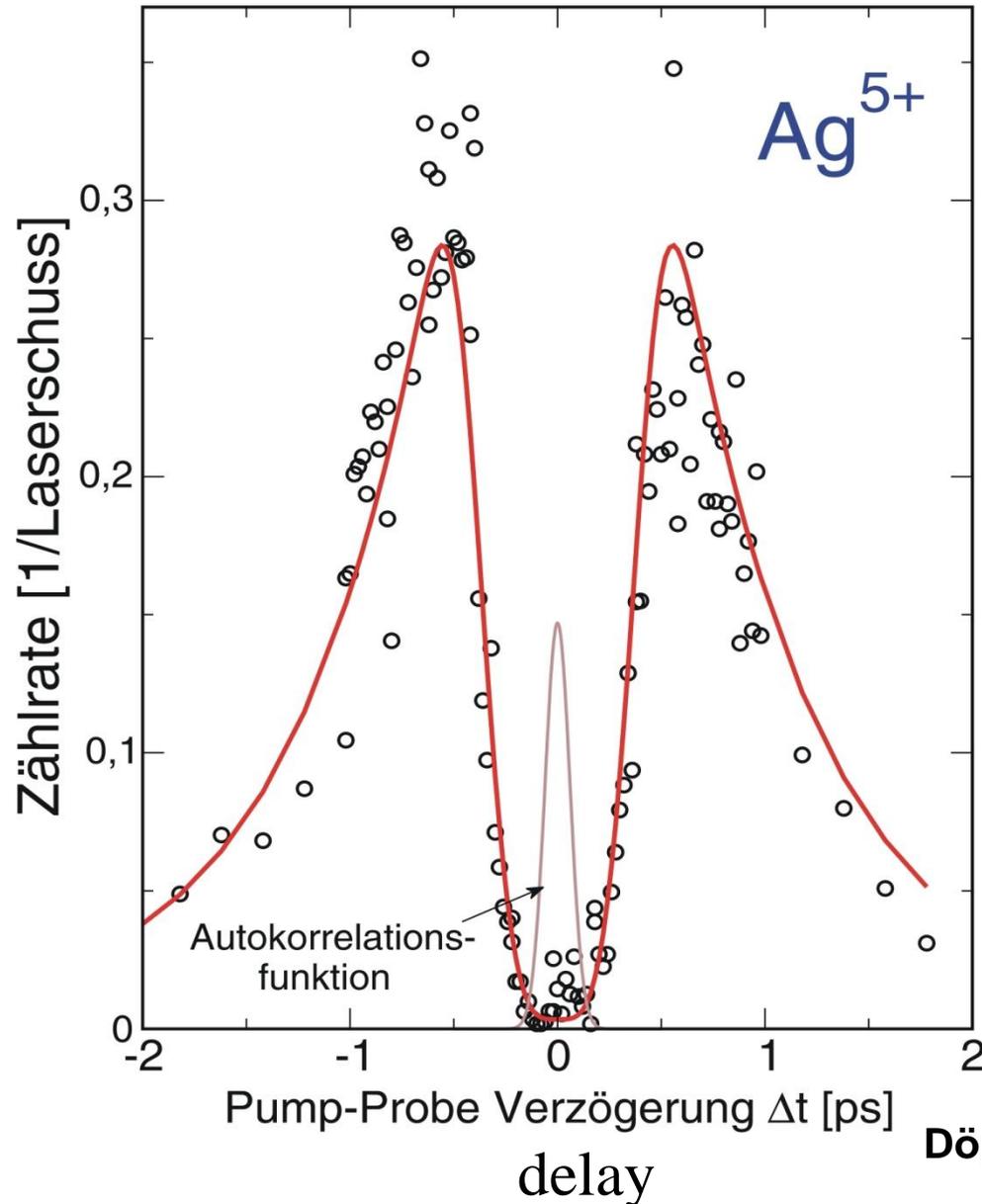
$$\omega_{Mie} = \sqrt{\frac{n_{bg} e^2}{3m\epsilon_0}} = \frac{\omega_p}{\sqrt{3}}$$

Mie - Plasmon

demonstration: dual-pulse technique
time dependent plasmon



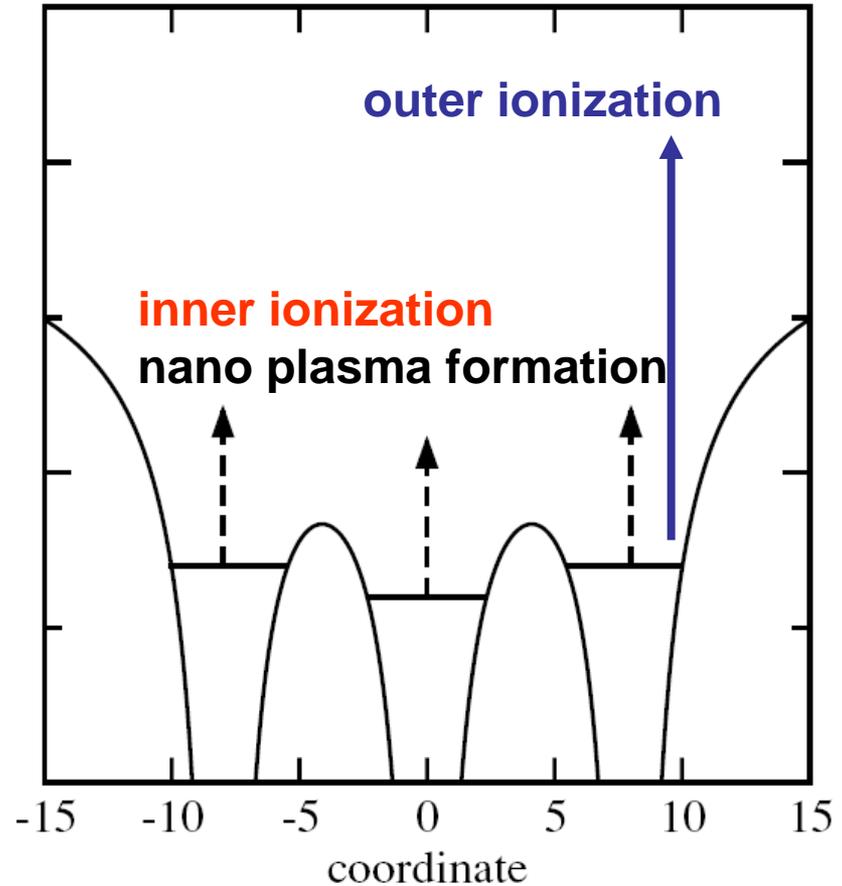
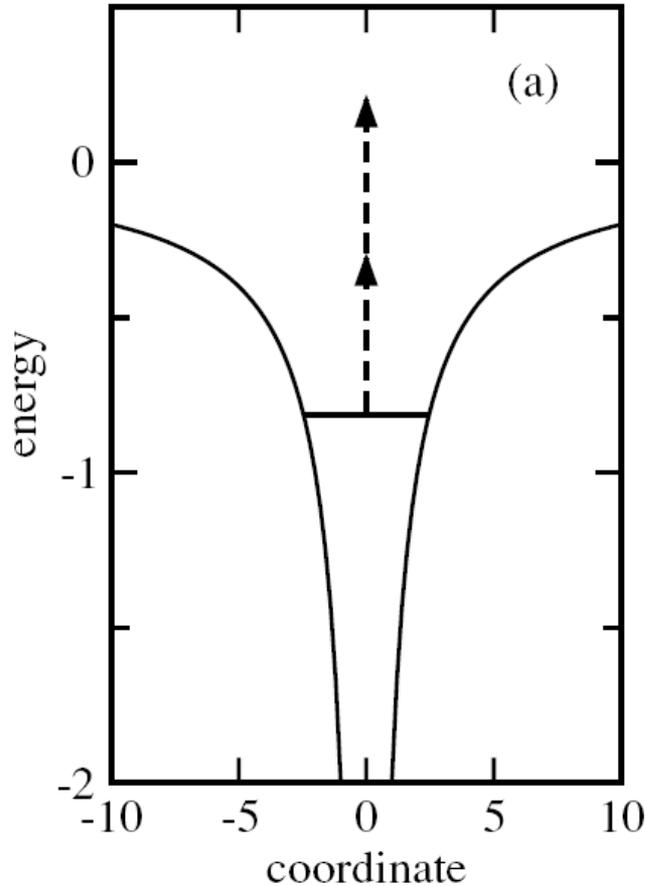
dual-pulse excitation of Ag_N @He-droplet



Laser parameters:

- $\lambda = 800 \text{ nm}$
- $\tau = 120 \text{ fs}$
- $I = 1.8 \times 10^{13} \text{ W/cm}^2$

inner vs. outer ionization



several heating mechanisms:

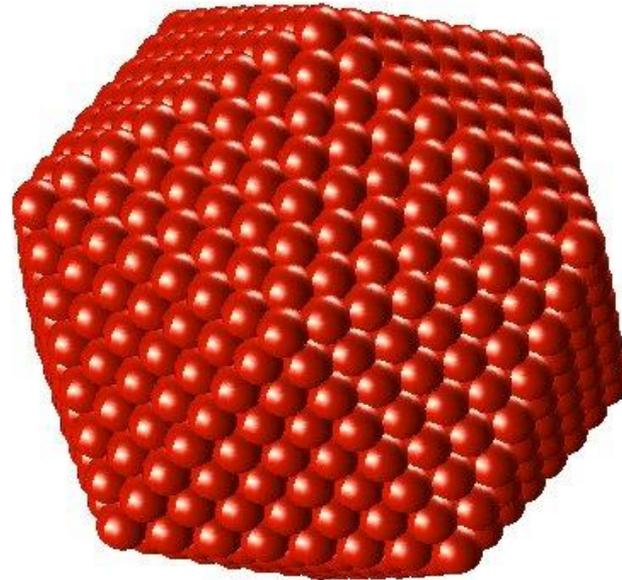
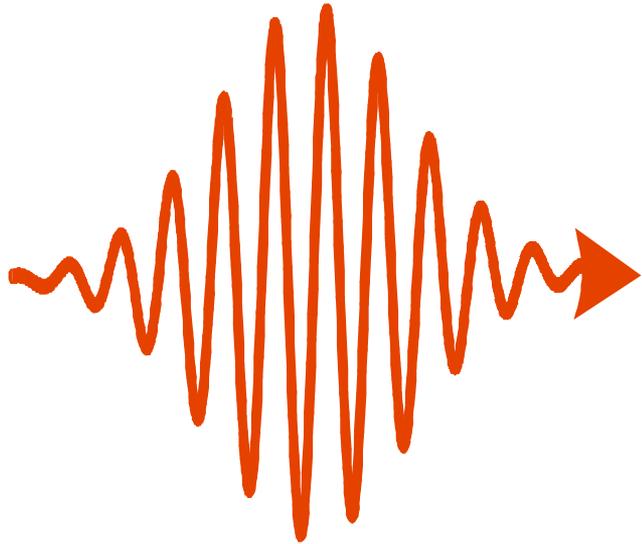
inverse bremsstrahlung

laser driven electron-ion collisions

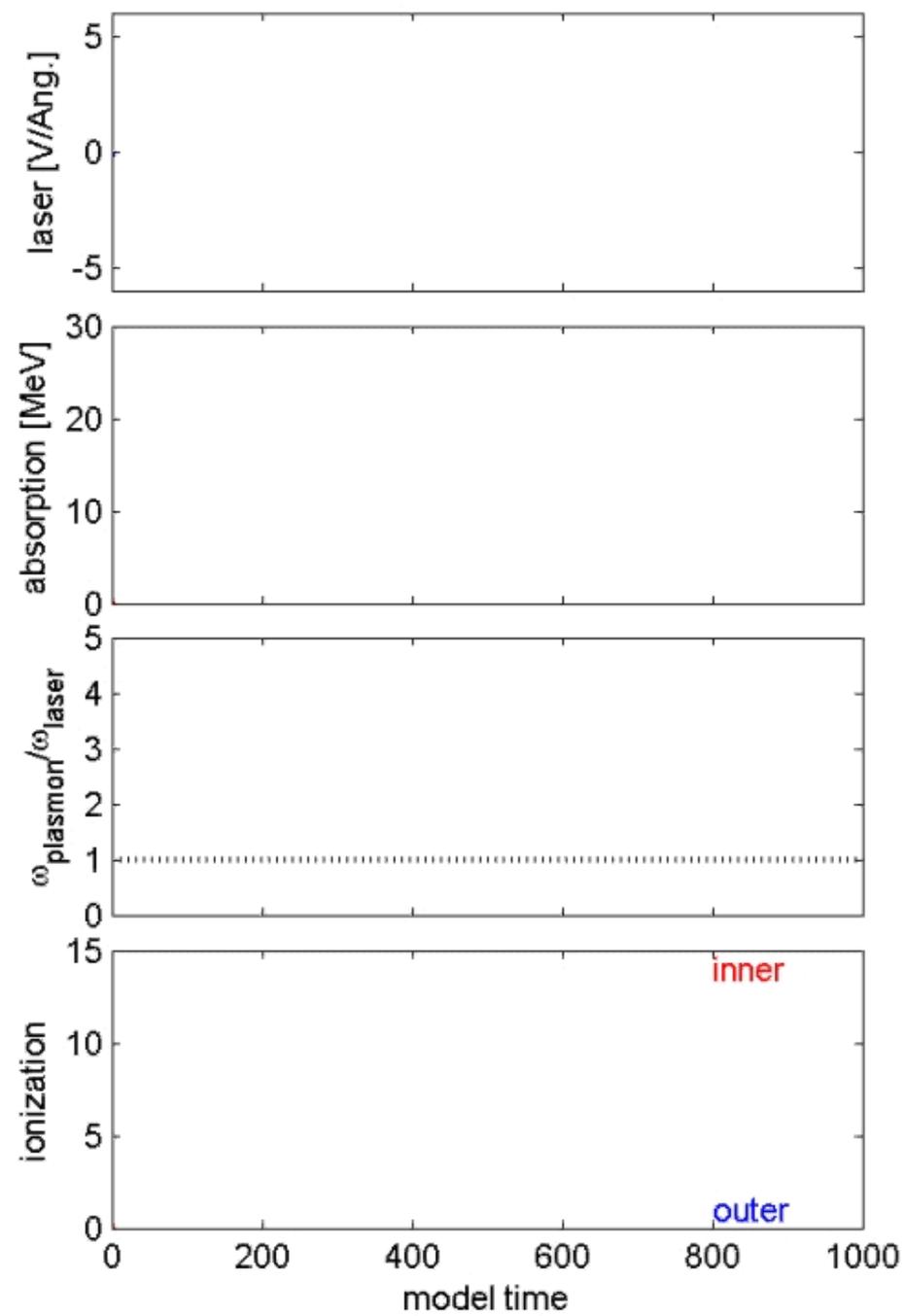
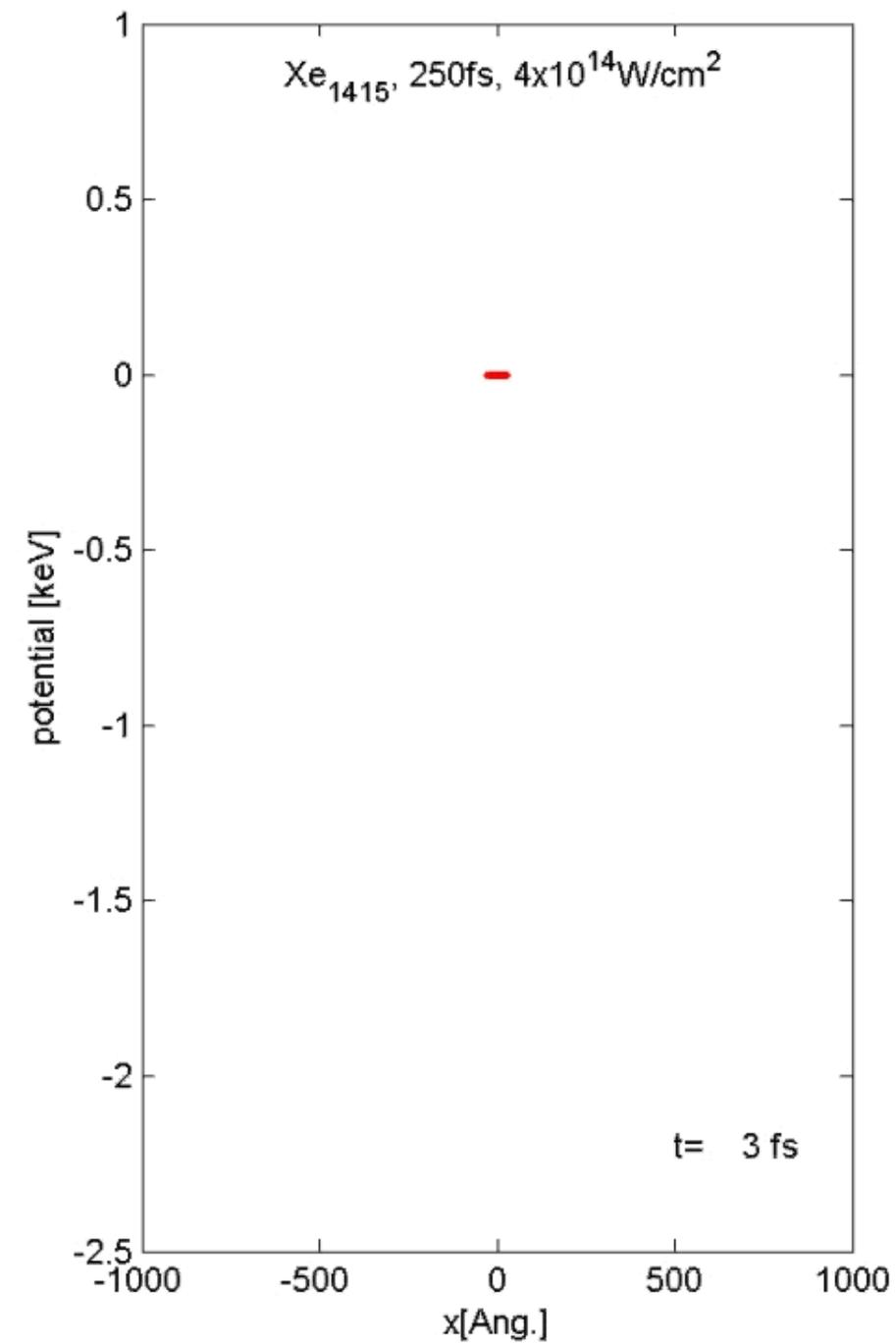
after: Ch. Siedschlag and J M. Rost *PRL* **93** 043402 (2004)

computer experiment: laser excitation of Xe clusters

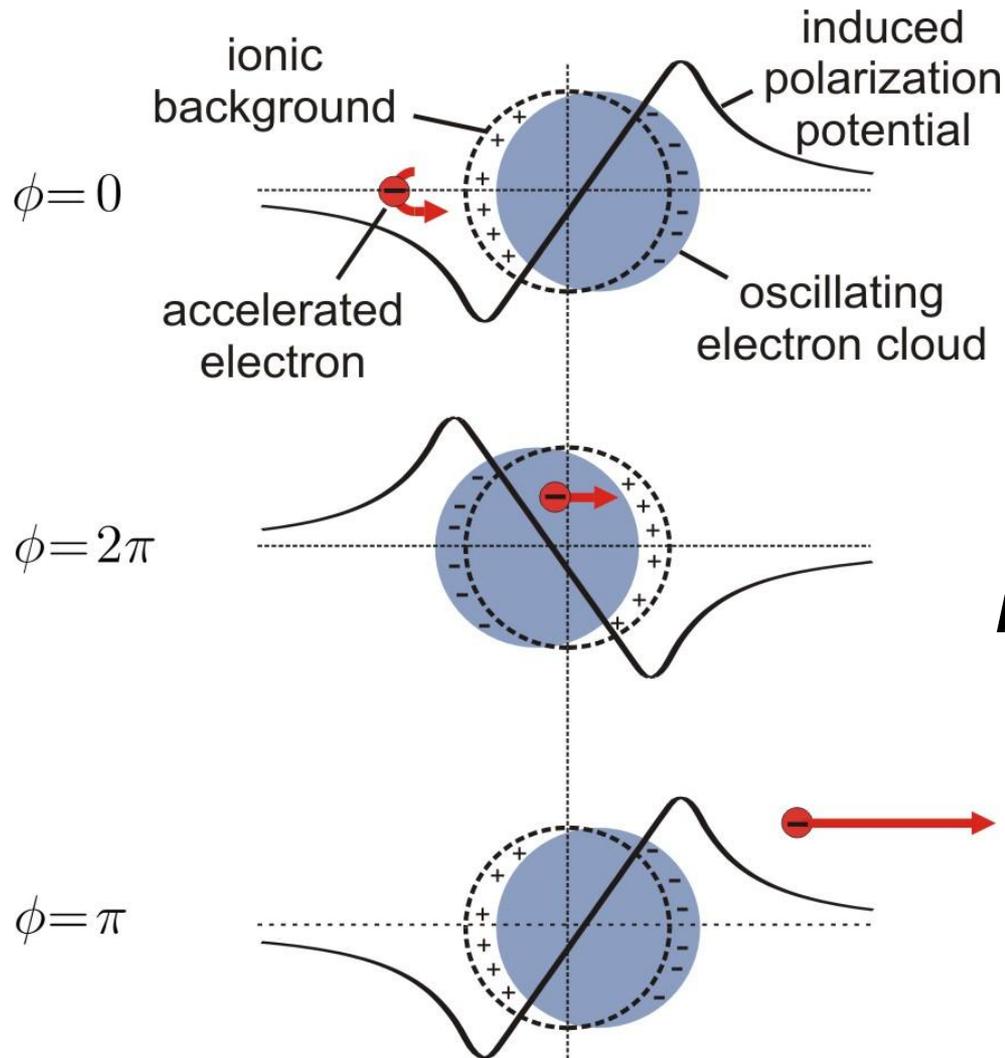
250fs, 800nm,
 $4 \times 10^{14} \text{ W/cm}^2$



Xe₁₄₁₅



on plasmon resonance: dynamic electron acceleration



field strength for $N = 500$:

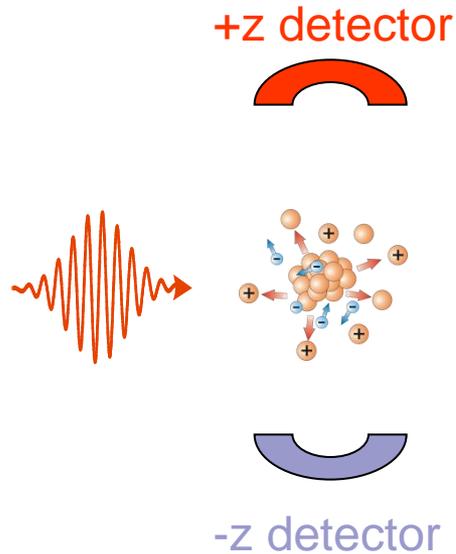
140 GeV/m

***Surface-Plasmon Assisted
Resonant electron acceleration
in Clusters SPARC***

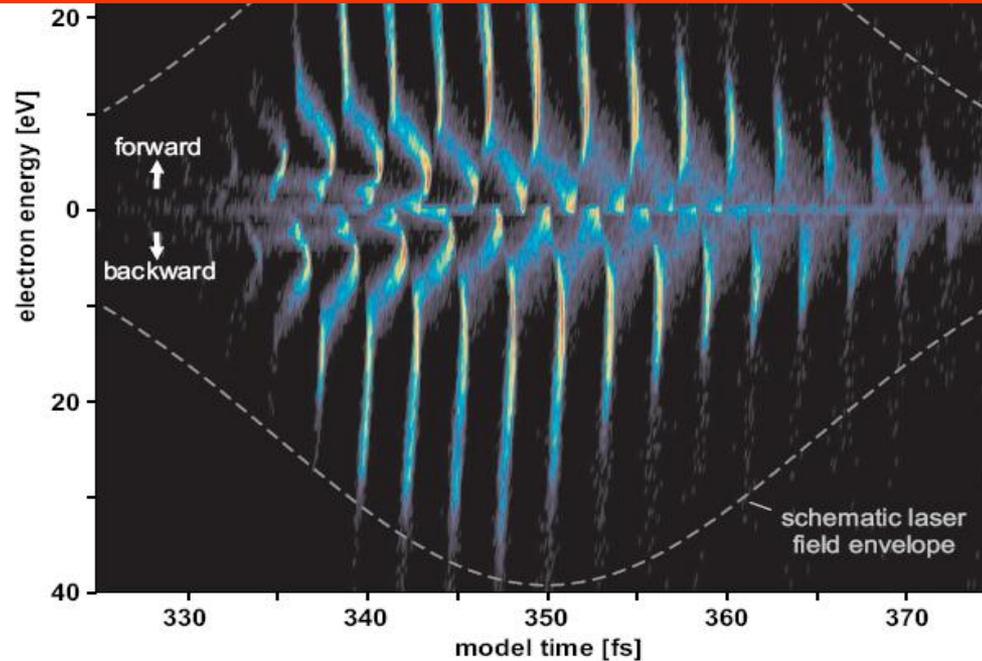
Nano electron accelerator

attosecond electron bursts

numerical experiment

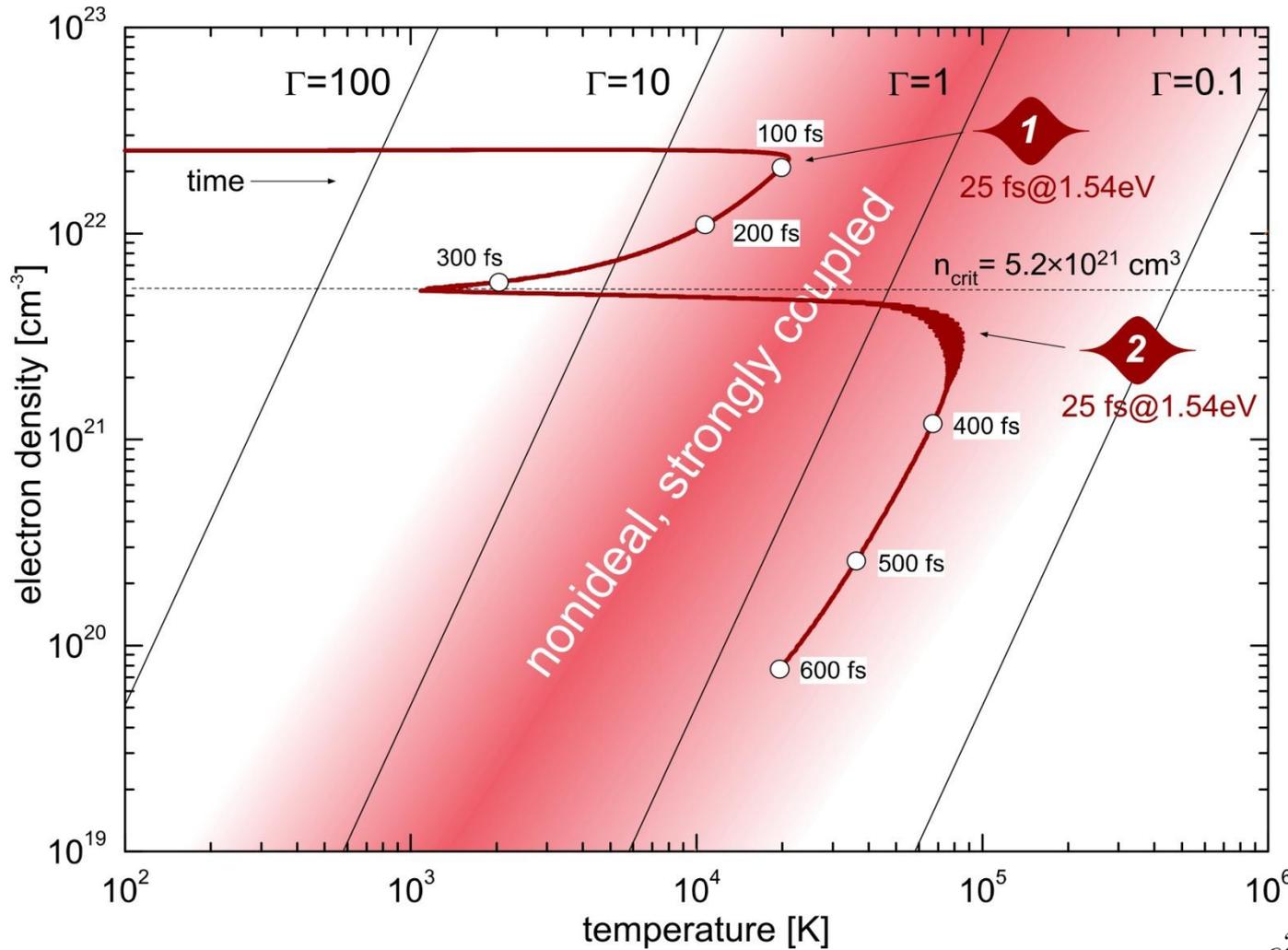


➤ interesting playground for future few-cycle and attosecond physics



Fennel et al., PRL 98, 143401 (2007)

density-temperature plane



$$\Gamma = \frac{e^2}{4\pi\epsilon_0 k_B T} \left(\frac{4}{3} \pi n_e \right)^{1/3}$$

plasma physics on the nm scale

coupling parameter